

ProDiGen: a genetic algorithm for process discovery guided by completeness, precision and simplicity

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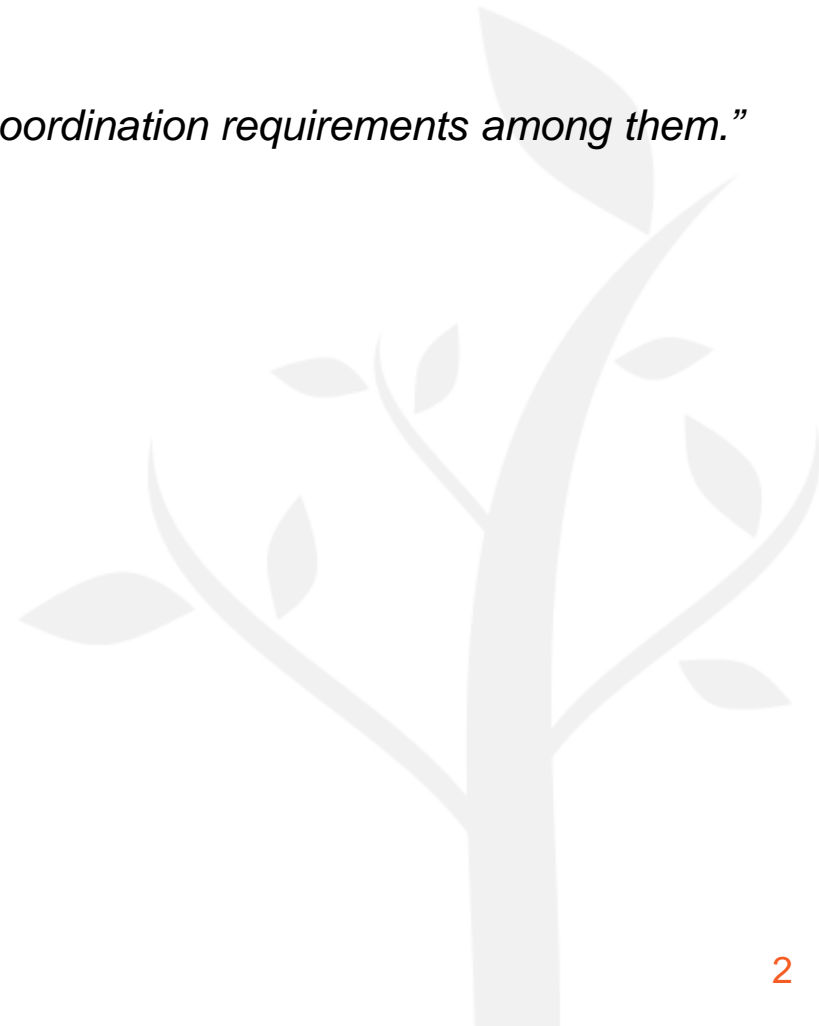
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WHAT IS A PROCESS?

“[...] a collection of tasks ---or activities--- with coordination requirements among them.”
- Wil van der Aalst

EXAMPLE

1. A teacher uploads an exercise
2. A learner makes the exercise
3. The teacher grades it



AND WHAT IS A WORKFLOW?

“The automation of a business **process**, in whole or part, during which documents, information or tasks are passed from one participant to another for action, according to a set of procedural rules.”

-Workflow Management Coalition

EXAMPLE

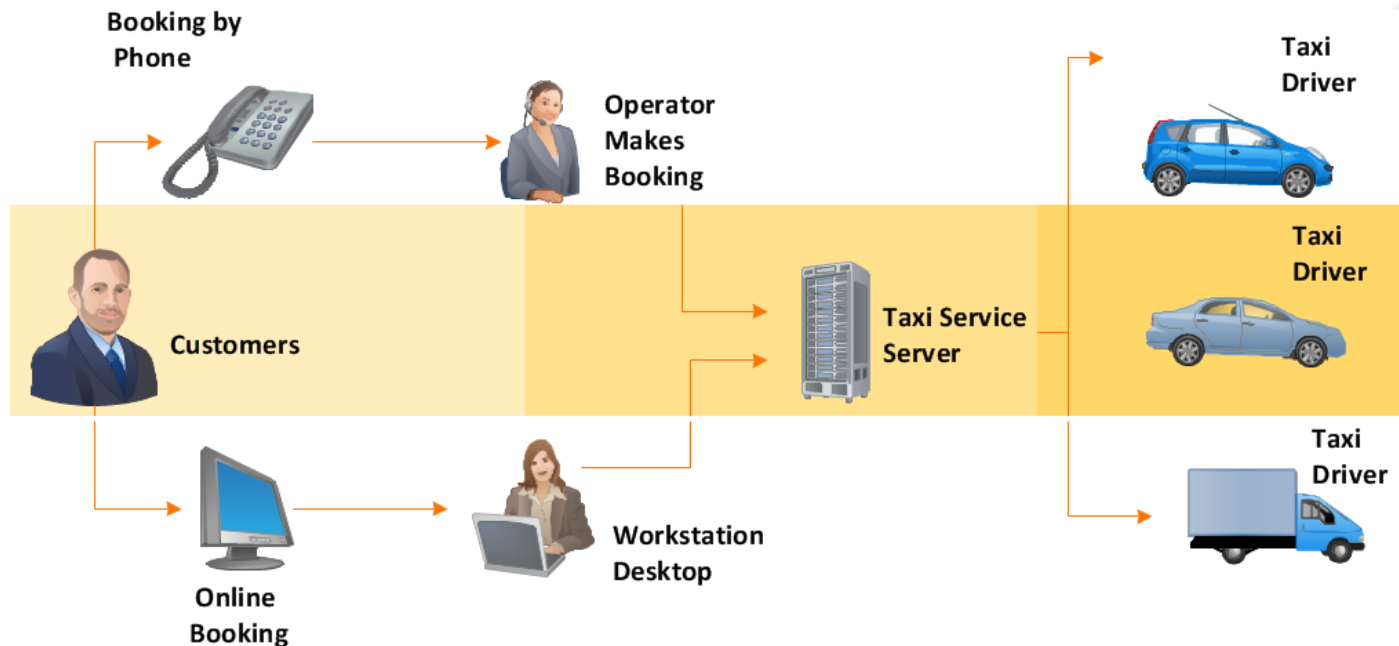
1. A teacher uploads an exercise
2. A learner makes the exercise
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Workflow

Provides useful information:

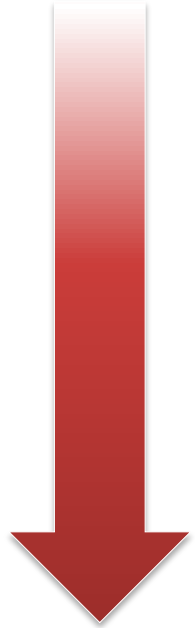
- **What** is happening on a process.
- **How** is that process being executed.
- **Who** is involved in the execution of the process.



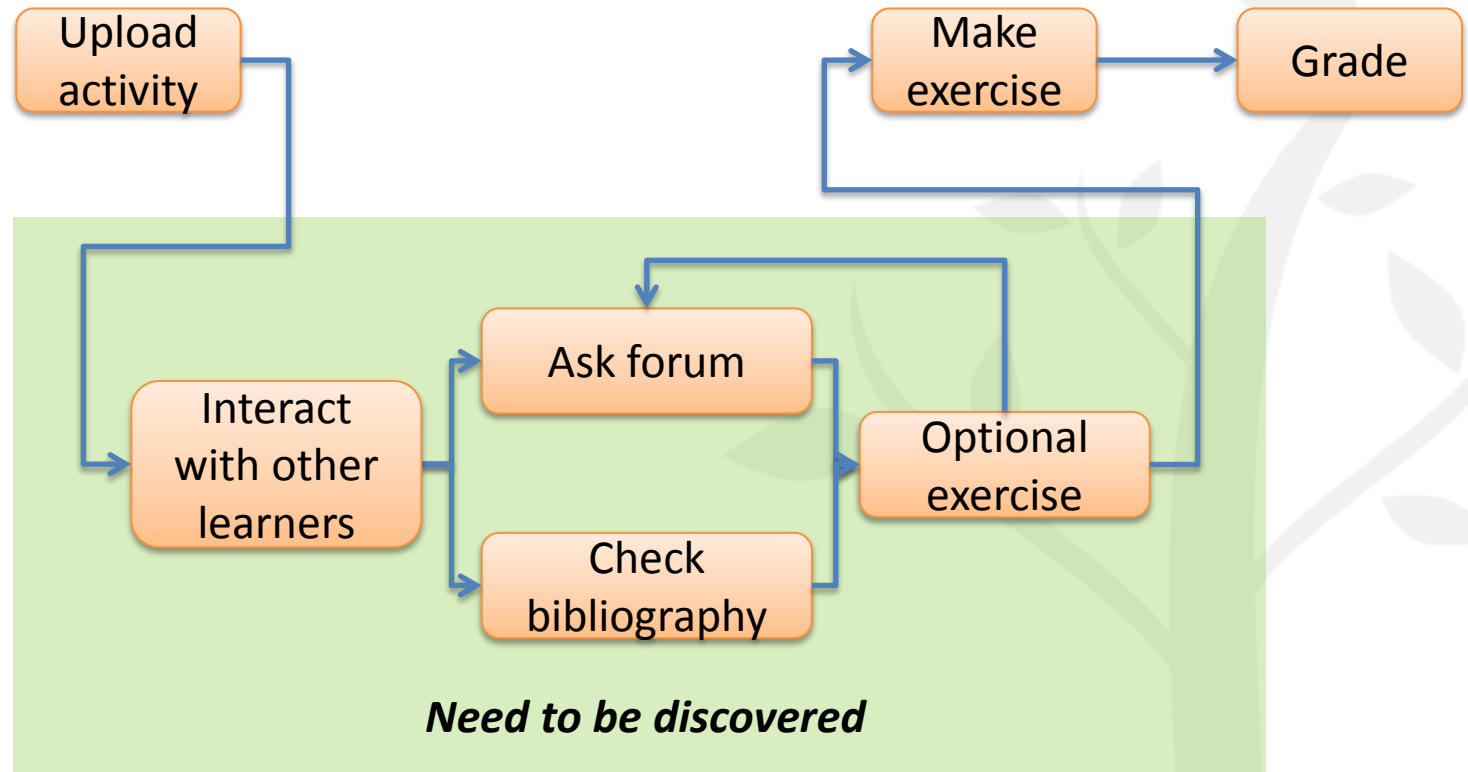
Workflow

Issues

What we think
is going on



What is actually
happening

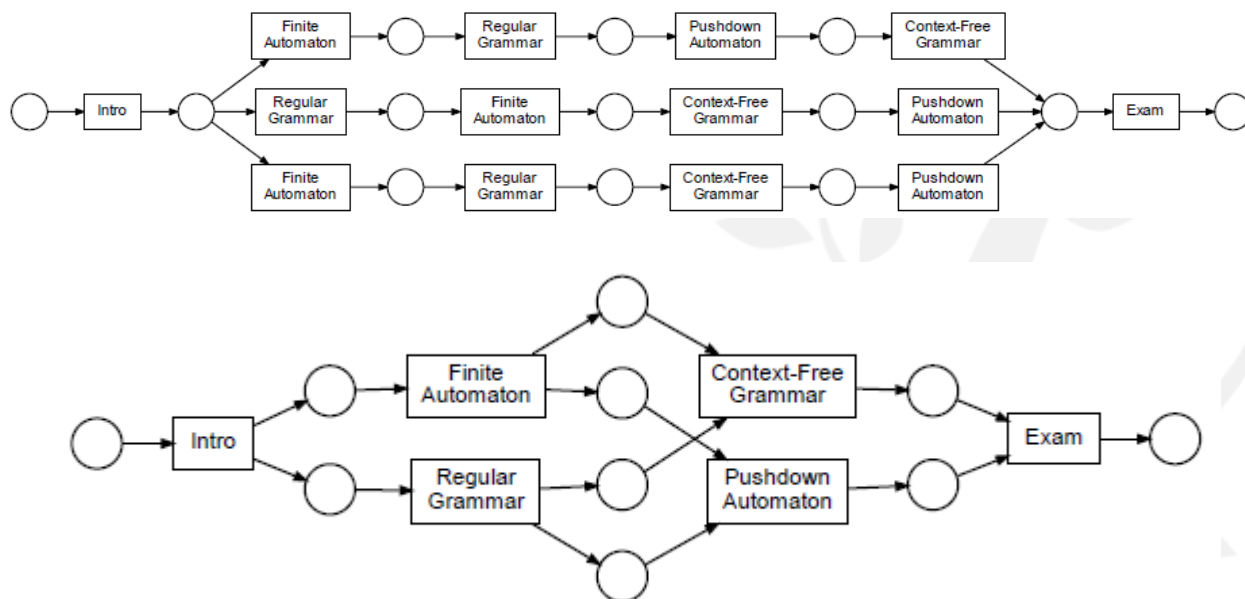


Process mining

DEFINITION

The goal of **process mining** is to automatically discover the models that better fit the process, *taking as a starting point the logs*.

case ID	task
Saul	Intro
Walter	Intro
Saul	Finite Automaton
Saul	Regular Grammar
Walter	Finite Automaton
Walter	Regular Grammar
Saul	Context-Free Grammar
Walter	Pushdown Automaton
Saul	Pushdown Automaton
Walter	Context-Free Grammar
Saul	Exam
Walter	Exam



What is actually happening, and not what the people think it is


WE WANT MODELS WITH SOME CHARACTERISTICS...

- **Completeness:** model all the behavior shown in the log.
- **Precision:** avoid overly general models.
- **Generalization:** avoid overly precise models.
- **Simplicity:** Occam's razor.

WE WANT MODELS WITH SOME CHARACTERISTICS...

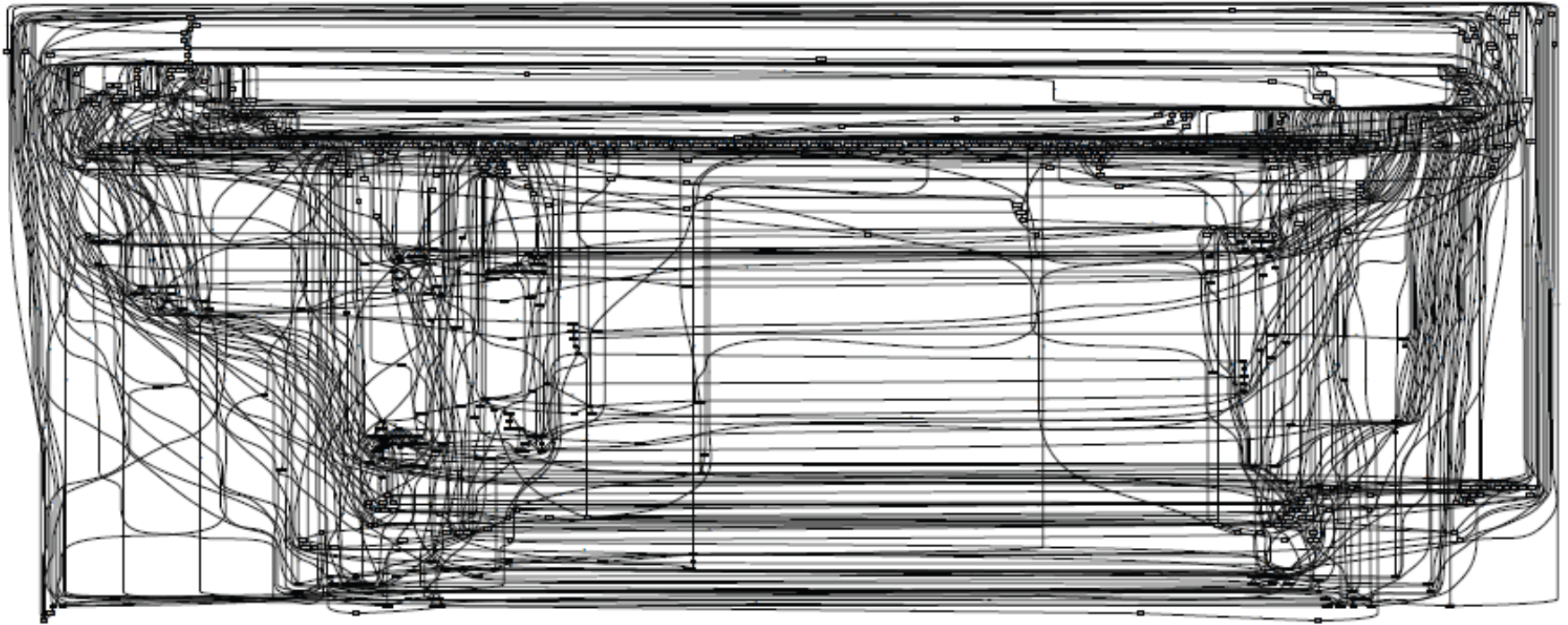
- **Completeness:** model all the behavior shown in the log.
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 - **Simplicity:** Occam's razor.
- Bias-variance tradeoff*

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Process mining

Spaghetti models



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- **Completeness:** model all the behavior shown in the log.
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 - **Generalization:** avoid overly precise models.
 - **Simplicity:** Occam's razor.
 - **Robust to noise**
- Bias-variance tradeoff
- 

State of the art

- **Abstraction based** : Poor completeness
 - ▷ *α -algorithm (and extensions)*
- **Heuristics based**: Cannot handle all the constructs at once
 - ▷ *Heuristics Miner*
- **Search based**: Do not consider simplicity
 - ▷ *Genetic Miner*
- **Based theory of regions**: Cannot handle noise and infrequent behavior
 - ▷ *ILP*

Objectives

1. An algorithm that retrieves ***complete, precise*** and ***simple*** models.

2. Robust to noise

3. Application in different domains

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1. An algorithm that retrieves ***complete, precise*** and ***simple*** models.
2. Robust to noise
3. Applicable in different domains

1. ProDiGen
2. SoftLearn
3. Future work
4. Publications



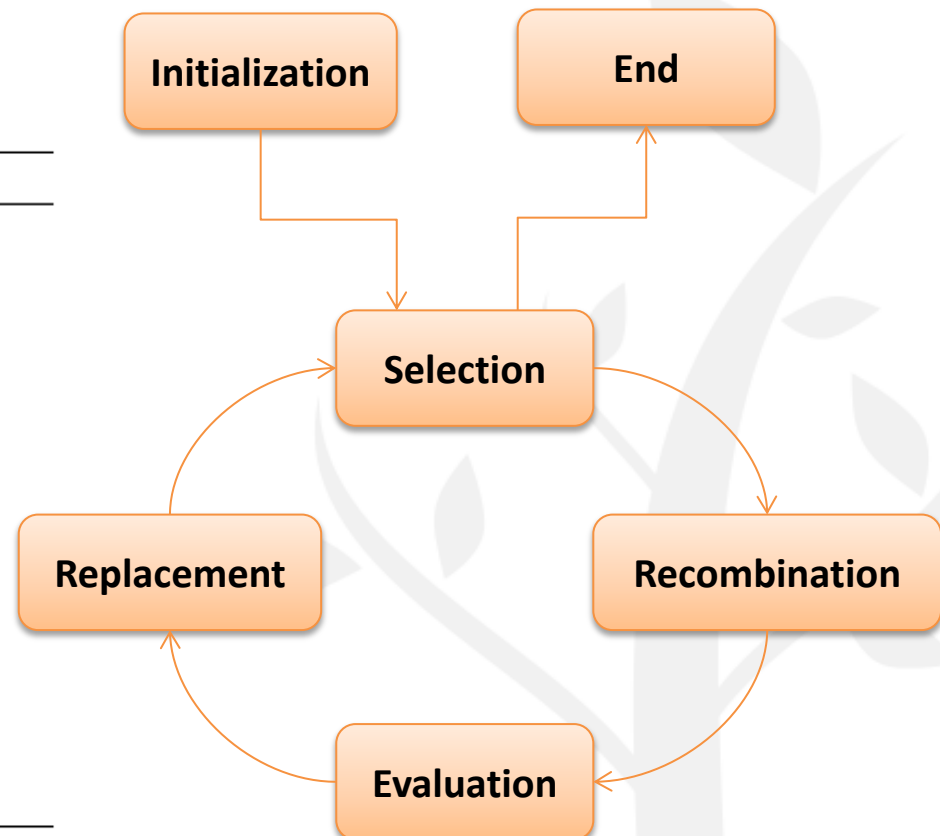
■ Components:

- ▷ **Individuals:** solutions.
- ▷ **Population:** set of individuals.

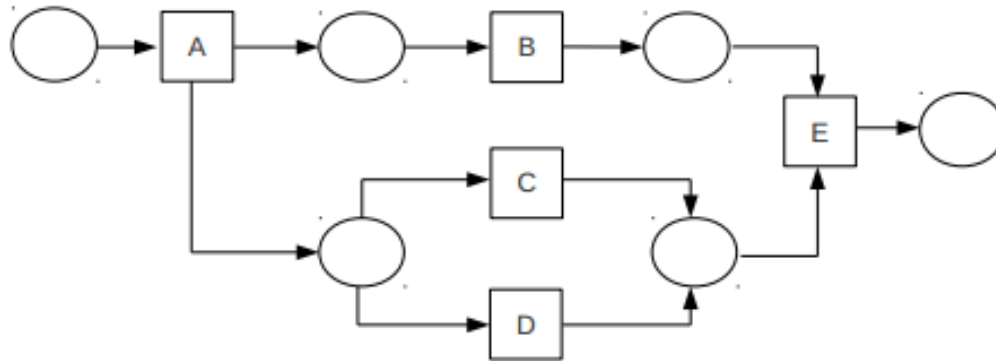
Algorithm 1: Genetic algorithm for process discovery.

```
1 Initialize population;  
2 Evaluate population;  
3  $t = 1, timesRun = initialTimesRun, restarts = 0;$   
4 while  $t \leq maxGenerations$  &&  $restarts < maxRestarts$  do  
5     Selection;  
6     Crossover;  
7     Mutation;  
8     Evaluate new individuals;  
9     Replace population;  
10     $t = t + 1;$   
11    if  $bestInd(t) == bestInd(t - 1)$  then  
12         $timesRun = timesRun - 1;$   
13    if none of the individuals of the population have been replaced then  
14         $timesRun = timesRun - 1;$   
15    if  $timesRun < 0$  then  
16        Reinitialize population;  
17        Evaluate population;  
18         $timesRun = initialTimesRun, restarts = restarts + 1;$ 
```

Evolutionary cycle



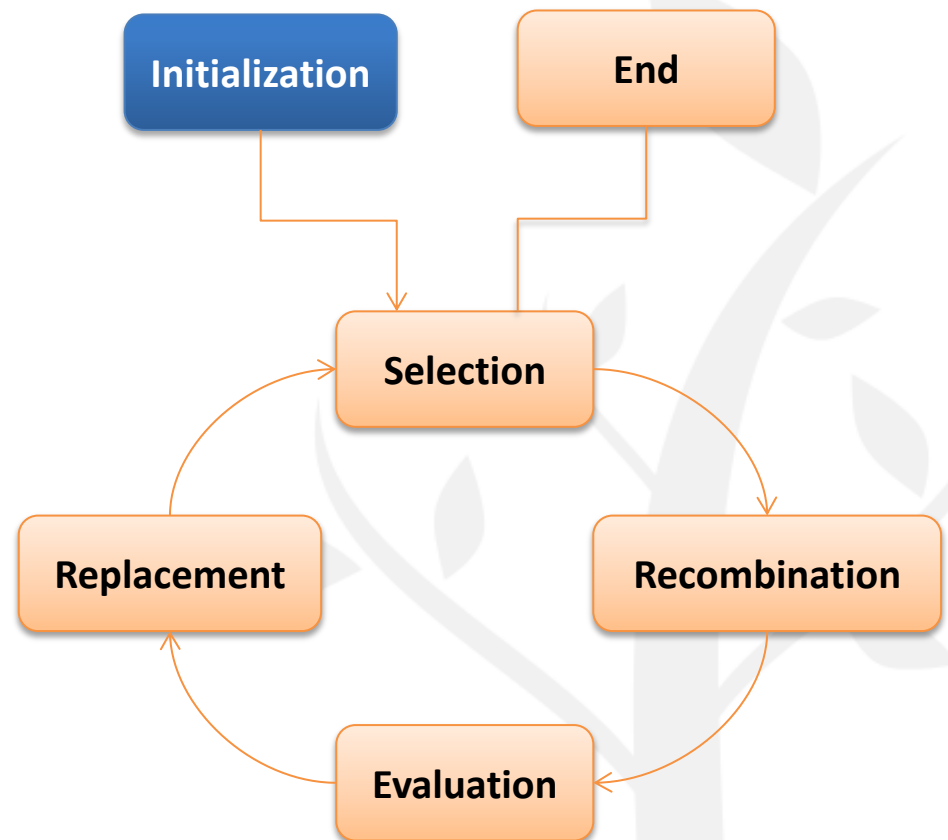
- **Causal matrix:** maps the input and output dependencies of each task.



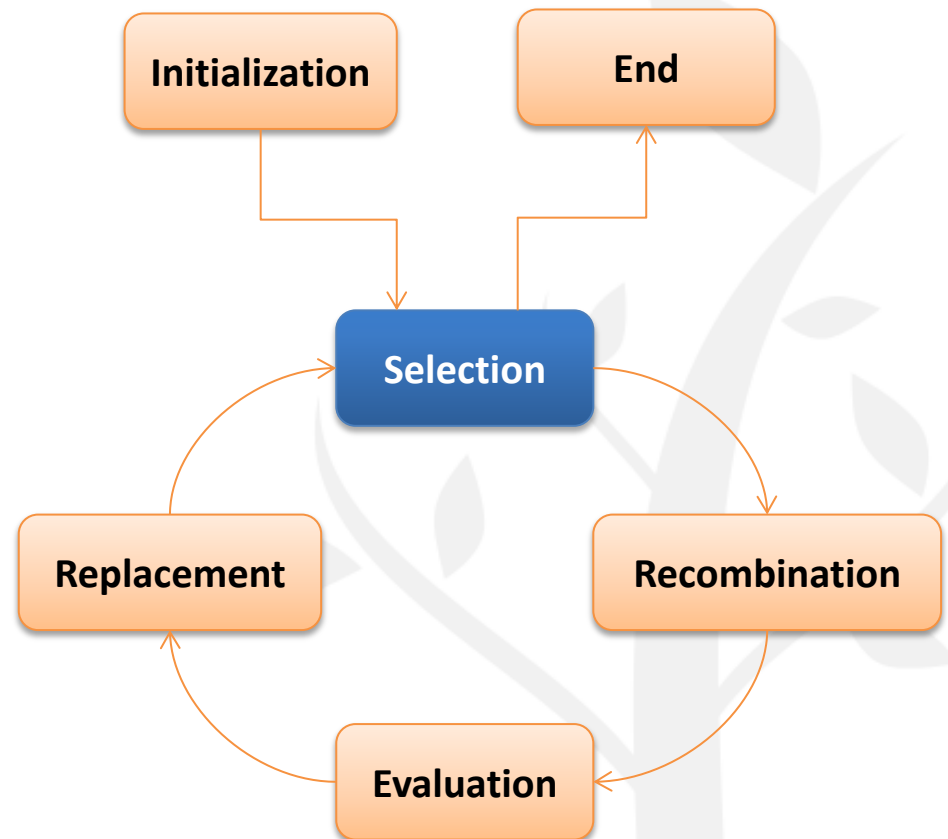
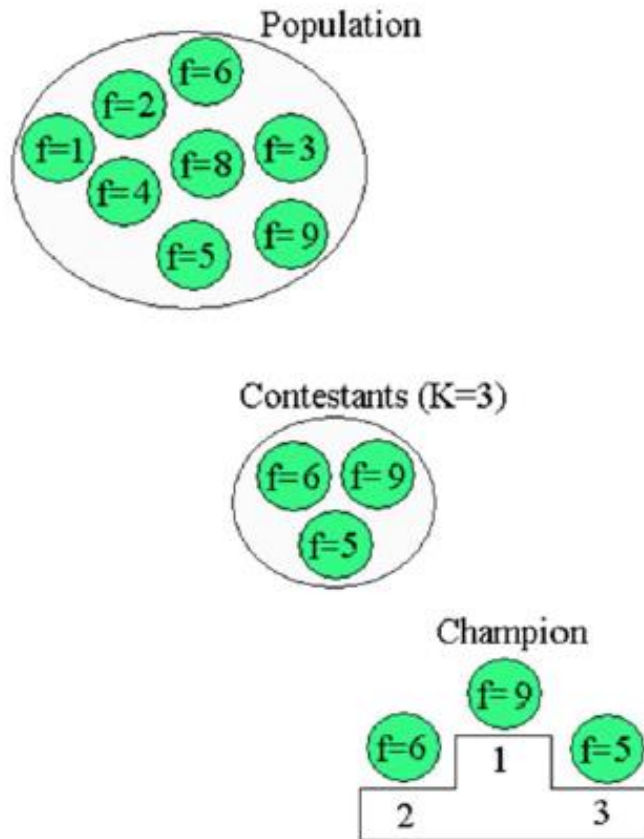
Tarea	I(Tarea)	O(Tarea)
A	{}	{{B},{C,D}}
B	{A}	{E}
C	{A}	{E}
D	{A}	{E}
E	{{B},{C,D}}	{}

- Initialization of each individual of the population
- Based on a heuristics approach
 - ▷ Using the local information of the log.
 - ▷ Dependencies between tasks.

$$\left\{ \begin{array}{ll} \frac{\#aba + \#bab}{\#aba + \#bab + 1} & \text{if } a \neq b \text{ and } \#aba > 0; \\ \frac{\#ab - \#ba}{\#ab + \#ba + 1} & \text{if } a \neq b \text{ and } \#aba = 0; \\ \frac{\#ab}{\#ab + 1} & \text{if } a = b. \end{array} \right.$$



■ Binary tournament



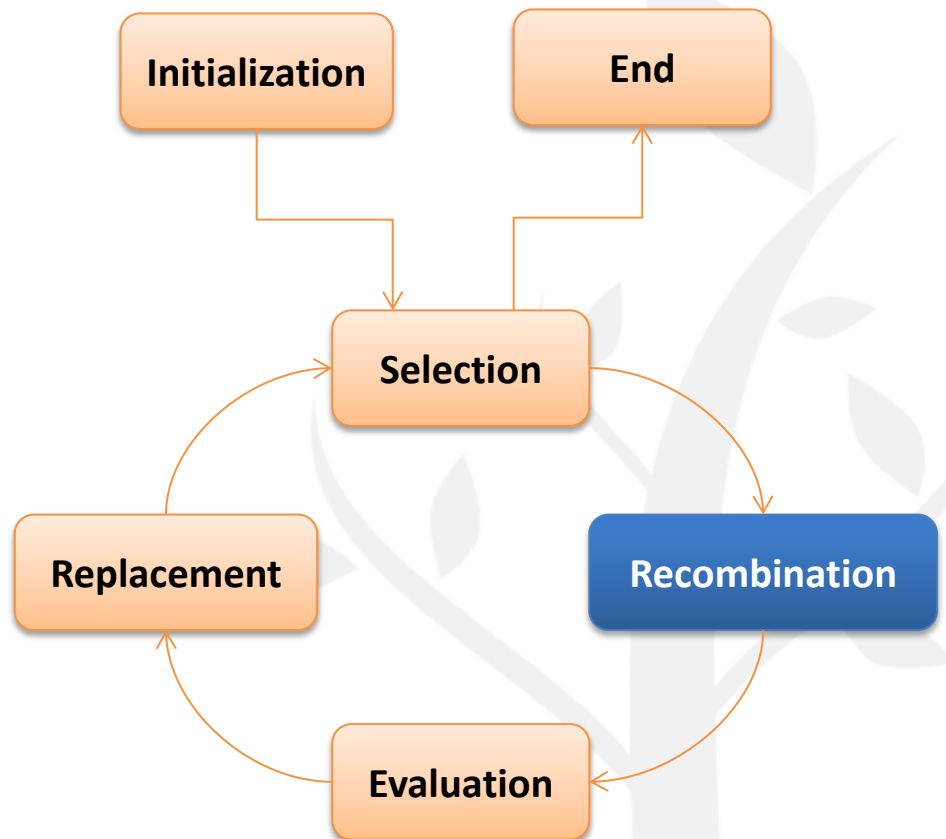
Generate new individuals.

- **Crossover:**

- ▶ Combine the characteristics of two parents into two offspring

- **Mutation:**

- ▶ Add or remove material form an individual.



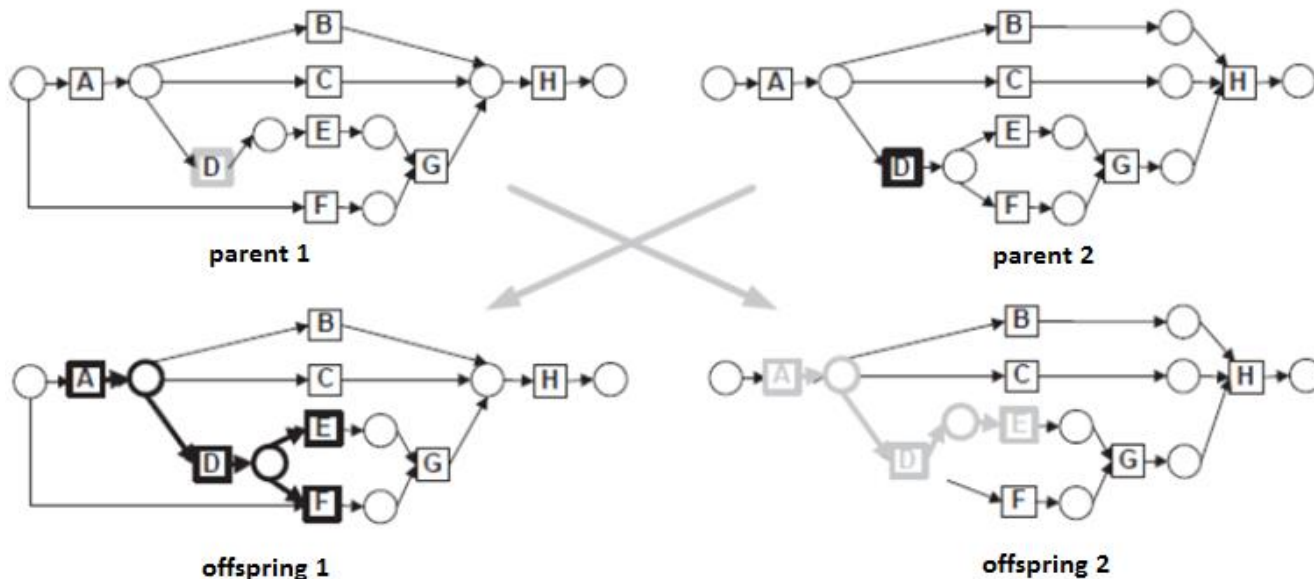
- Guided by a *Probability Density Function* generated from the errors.

Algorithm 2: Pseudo-code for the crossover operator.

```

1  $r \leftarrow \text{getRandomNumber}()$  // returns a random number between  $[0,1)$ ;
2 if  $r < \text{crossoverRate}$  then
3    $\text{incorrectlyFiredActivities} \leftarrow \emptyset$ ;
4   if  $\text{fitness}(\text{parent}_1) \geq \text{fitness}(\text{parent}_2)$  then
5      $\text{incorrectlyFiredActivities} \leftarrow \text{set of incorrectly fired activities of parent}_1$ ;
6   else
7      $\text{incorrectlyFiredActivities} \leftarrow \text{set of incorrectly fired activities of parent}_2$ ;
8   if  $\text{incorrectlyFiredActivities} \neq \emptyset$  then
9      $\text{crossoverPoint} \leftarrow \text{randomly select an activity } i \text{ from } \text{incorrectlyFiredActivities}$ ;
10  else
11     $\text{crossoverPoint} \leftarrow \text{randomly select an activity } i \text{ from the bag of all possible tasks in the log}$ ;
12   $\text{offspring}_1, \text{offspring}_2 \leftarrow \text{doCrossover}(\text{parent}_1, \text{parent}_2, \text{crossoverPoint})$ ;
13  Repair  $\text{offspring}_1$  and  $\text{offspring}_2$ ;

```

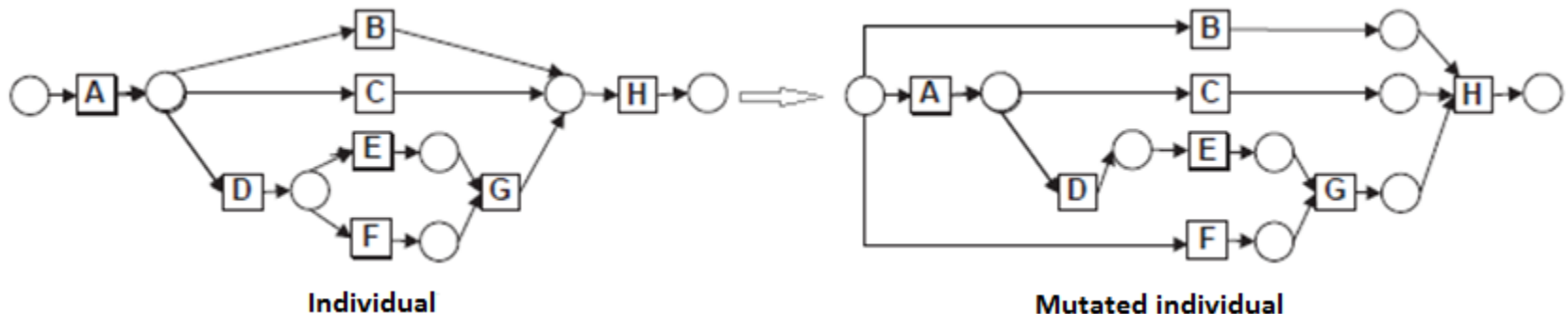


- Guided by the causal dependencies of the log.

Algorithm 3: Pseudo-code for the mutation operator.

```

1 while the individual does not change do
2   Randomly choose one task  $t$  in the individual;
3    $mutationType \leftarrow getRandomNumber()$  // returns a random number
    between  $[0,1)$ ;
4   if  $mutationType < 1/3$  then
5     Randomly add a new task  $t'$  to  $I(t)$ , being  $t'$  a task from
       $inputDependencies(t)$ ;
6     if  $getRandomNumber() < 1/2$  then
7       Randomly choose one subset  $X \in I(t)$  and add the task  $t'$  to  $X$ ;
8     else
9       Create a new subset  $X$ , add the task  $t'$  to  $X$ , and add  $X$  to  $I(t)$ ;
10  else if  $mutationType < 2/3$  then
11    Randomly choose one subset  $X \in I(t)$  and remove a task  $t'$  from  $X$ ,
      where  $t' \in X$ . If  $X$  is empty after this operation, exclude  $X$  from  $I(t)$ ;
12  else
13    Randomly redistribute the elements from  $I(t)$ ;
14  Repeat from line 3, but using  $O(t)$  instead of  $I(t)$  and  $outputDependencies(t)$ 
    instead of  $inputDependencies(t)$ ;
15  Repair the individual;
  
```

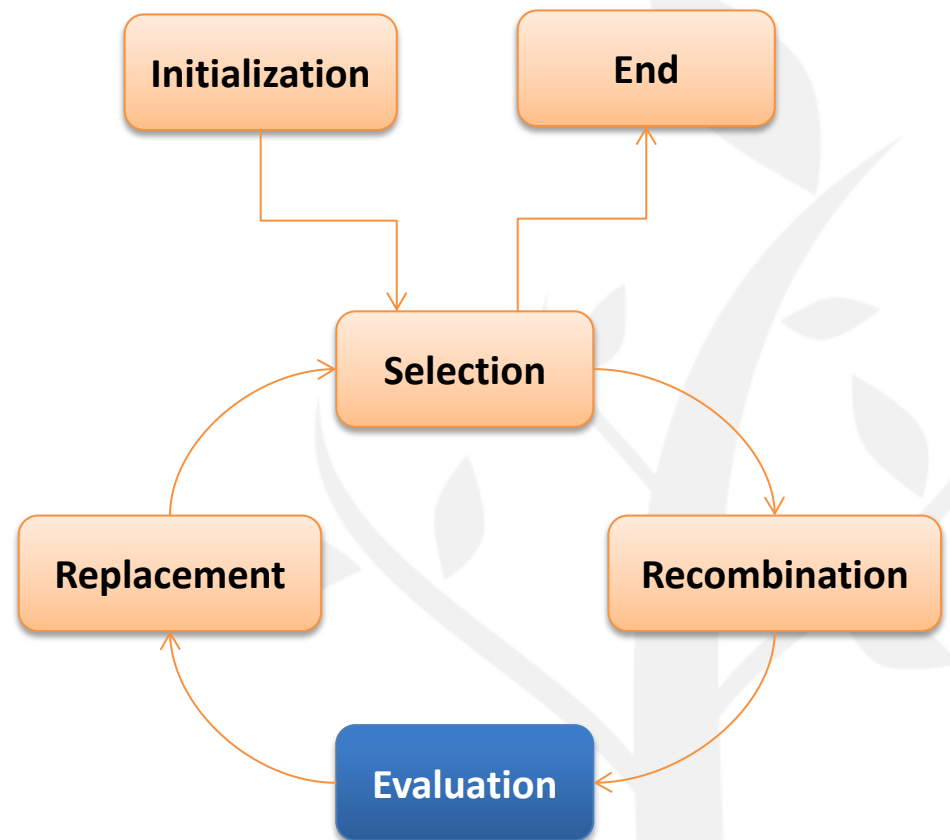


- Each individual is evaluated with **three** objectives:

Completeness

Precision

Simplicity



■ Completeness

$$C_f(L, CM) = \frac{\text{allParsedActivities}(L, CM) - \text{punishment}}{\text{numActivitiesLog}(L)}$$

where

$$\begin{aligned} \text{punishment} = & \frac{\text{allMissingTokens}(L, CM)}{\text{numTracesLog}(L) - \text{numTracesMissingTokens}(L, CM) + 1} \\ & + \frac{\text{allExtraTokensLeftBehind}(L, CM)}{\text{numTracesLog}(L) - \text{numTracesExtraTokensLeftBehind}(L, CM) + 1} \end{aligned}$$

■ Precision:

$$P_f(L, CM) = \frac{1}{allEnabledActivities(L, CM)}$$

■ Simplicity:

$$S_f(CM) = \frac{1}{\sum_{t \in CM} \left(\sum_{\Phi \in I(t)} |\Phi| + \sum_{\Psi \in O(t)} |\Psi| \right)}$$

Hierarchical fitness function

$$F(a) > F(b) \iff \{C_f(a) > C_f(b)\} \vee \{C_f(a) = C_f(b) \wedge P_f(a) > P_f(b)\} \\ \vee \{C_f(a) = C_f(b) \wedge P_f(a) = P_f(b) \wedge S_f(a) > S_f(b)\}$$

Completeness



Precision



Simplicity

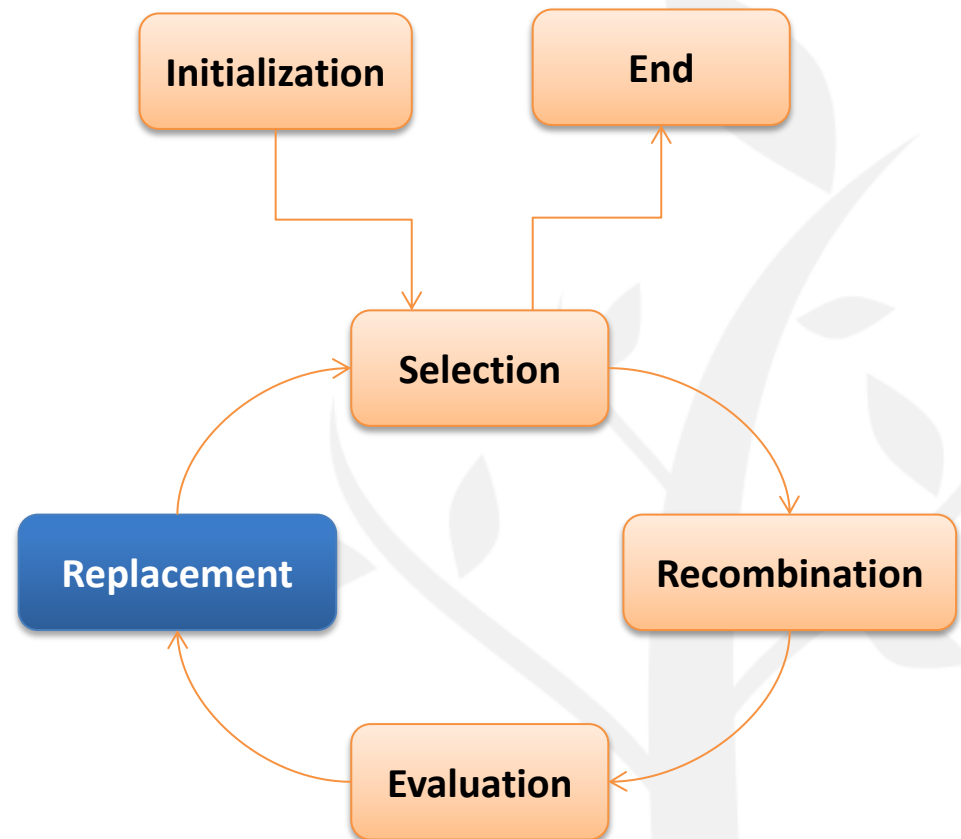
Update of the population

■ **Steady-state** process...

- ▷ Combine and sort parents and offspring ($2N$)
- ▷ The N best survive to the next cycle.

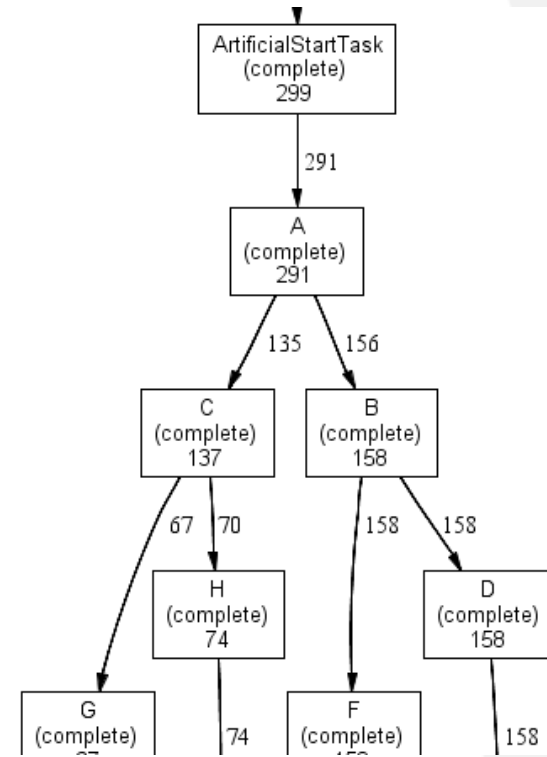
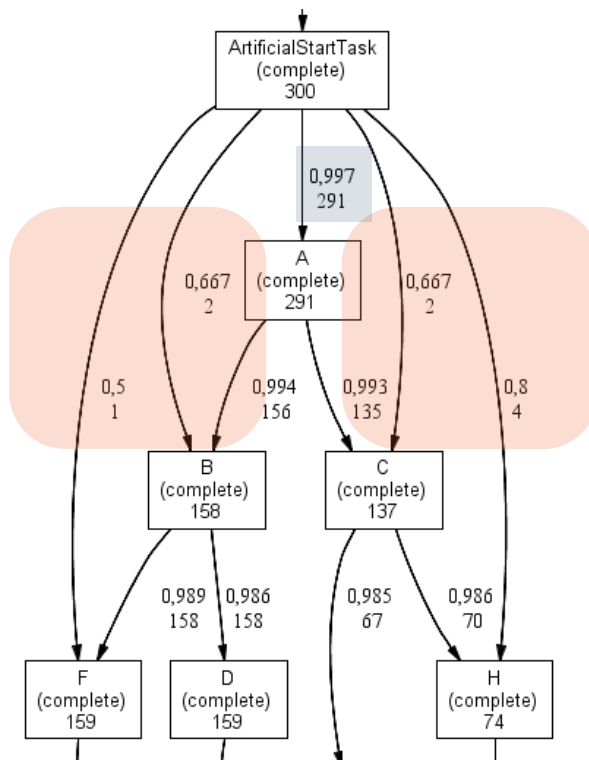
■ ...with **reinitialization**:

- ▷ If the best solution does not change
- ▷ If there are not new individuals in the population



WAIT..., AND WHAT ABOUT NOISE?

- Post-processing of the best individual: **arc-pruning**
 - ▷ Remove those arcs used fewer than a certain threshold



■ 18 different models

- ▷ Different degrees of complexity
- ▷ Logs with several levels of noise:
 - 0% of noise
 - 1% of noise
 - 5% of noise
 - 10% of noise.
 - 20% of noise.

▷ In total: 90 different logs

Model	Activity structures										Log content		
	#Tasks	Sequence	Choice	Parallelism	Length-One Loop	Length-Two Loop	Arbitrary Loop	Structured Loop	Non-local NFC	Local NFC	Invisible tasks	#traces	#events
<i>Caminatas</i>	12	✓	✓	✓								700	4,200
<i>A8</i>	7	✓	✓	✓								300	1,200
<i>D2</i>	6	✓		✓								300	1,200
<i>MI11Skip</i> [11]	6	✓	✓	✓	✓							500	4,757
<i>Ma5</i> [11]	7	✓	✓	✓	✓							300	2,178
<i>MI2l</i> [11]	6	✓	✓			✓						300	4,668
<i>MDriverLL</i> [11]	11	✓	✓	✓			✓	✓		✓		700	13,303
<i>allLoops</i>	5	✓	✓		✓	✓		✓		✓		300	1,035
<i>l2la</i>	6	✓	✓	✓			✓					300	2,264
<i>Ma7</i> [11]	9	✓	✓	✓								500	2,427
<i>Herbst6p37</i> [11]	16	✓		✓								700	12,600
<i>MexampleL</i> [11]	8	✓	✓	✓								300	1,645
<i>Ma6nfc</i> [11]	8	✓	✓							✓		300	2,006
<i>MParallel5</i> [11]	10	✓		✓								700	12,600
<i>NC</i>	7	✓	✓	✓						✓		300	1,704
<i>L2LP</i>	7	✓	✓	✓	✓	✓		✓		✓		300	5,476
<i>NCB</i>	7	✓	✓	✓			✓			✓		300	2,950
<i>DWS</i> [23]	12	✓	✓	✓						✓		500	4,033

(a) *Balanced logs.*

- 21 different models
 - ▷ Models with many interleaving situations.
 - ▷ Models with many different traces and frequencies
 - ▷ In total: 21 different logs

Model	#Tasks	Activity structures							Log content			
		Sequence	Choice	Parallelism	Length-One Loop	Length-Two Loop	Arbitrary Loop	Structured Loop	Invisible tasks	Unbalance	#traces	#events
<i>g2</i> [11]	22	✓	✓	✓	✓	✓		✓			300	4,501
<i>g3</i> [11]	29	✓	✓	✓		✓	✓	✓			300	14,599
<i>g4</i> [11]	29	✓	✓	✓	✓					✓	300	5,975
<i>g5</i> [11]	20	✓	✓	✓			✓	✓			300	6,172
<i>g6</i> [11]	23	✓	✓	✓	✓			✓			300	5,419
<i>g7</i> [11]	29	✓	✓	✓		✓		✓			300	14,451
<i>g8</i> [11]	30	✓	✓	✓	✓	✓		✓	✓		300	5,133
<i>g9</i> [11]	26	✓	✓	✓	✓	✓		✓			300	5,679
<i>g10</i> [11]	23	✓	✓	✓			✓	✓			300	4,117
<i>g12</i> [11]	26	✓	✓	✓	✓		✓	✓			300	4,841
<i>g13</i> [11]	22	✓	✓	✓	✓	✓		✓	✓		300	5,007
<i>g14</i> [11]	24	✓	✓	✓		✓		✓	✓		300	11,340
<i>g15</i> [11]	25	✓	✓	✓	✓	✓		✓			300	3,978
<i>g19</i> [11]	23	✓	✓	✓	✓			✓	✓		300	4,107
<i>g20</i> [11]	21	✓	✓		✓	✓		✓	✓		300	6,193
<i>g21</i> [11]	22	✓	✓				✓	✓	✓		300	3,882
<i>g22</i> [11]	24	✓	✓	✓		✓		✓	✓		300	3,095
<i>g23</i> [11]	25	✓	✓	✓	✓				✓	✓	300	9,654
<i>g24</i> [11]	21	✓	✓	✓			✓	✓	✓		300	4,130
<i>g25</i> [11]	20	✓	✓	✓	✓			✓			300	6,312
<i>EMT</i> [9]	7	✓	✓	✓				✓	✓		100	790

- 21 different models
 - ▷ Models with many interleaving situations.
 - ▷ Models with many different traces and frequencies
 - ▷ In total: 21 different logs

Model	#Tasks	Activity structures							Log content			
		Sequence	Choice	Parallelism	Length-One Loop	Length-Two Loop	Arbitrary Loop	Structured Loop	Imvisible tasks	Unbalance	#traces	#events
<i>g2</i> [11]	22	✓	✓	✓	✓	✓		✓			300	4,501
<i>g3</i> [11]	29	✓	✓	✓		✓	✓	✓			300	14,599
<i>g4</i> [11]	29	✓	✓	✓	✓					✓	300	5,975
<i>g5</i> [11]	20	✓	✓	✓			✓	✓			300	6,172
<i>g6</i> [11]	23	✓	✓	✓	✓			✓			300	5,419
<i>g7</i> [11]	29	✓	✓	✓		✓		✓			300	14,451
<i>g8</i> [11]	30	✓	✓	✓	✓	✓		✓	✓		300	5,133
<i>g9</i> [11]	26	✓	✓	✓	✓	✓		✓			300	5,679
<i>g10</i> [11]	23	✓	✓	✓			✓	✓			300	4,117
<i>g12</i> [11]	26	✓	✓	✓	✓		✓	✓			300	4,841
<i>g13</i> [11]	22	✓	✓	✓	✓	✓		✓	✓		300	5,007
<i>g14</i> [11]	24	✓	✓	✓		✓		✓	✓		300	11,340
<i>g15</i> [11]	25	✓	✓	✓	✓	✓		✓			300	3,978
<i>g19</i> [11]	23	✓	✓	✓	✓			✓	✓		300	4,107
<i>g20</i> [11]	21	✓	✓		✓	✓		✓	✓		300	6,193
<i>g21</i> [11]	22	✓	✓				✓	✓	✓		300	3,882
<i>g22</i> [11]	24	✓	✓	✓		✓		✓	✓		300	3,095
<i>g23</i> [11]	25	✓	✓	✓	✓				✓	✓	300	9,654
<i>g24</i> [11]	21	✓	✓	✓			✓	✓	✓		300	4,130
<i>g25</i> [11]	20	✓	✓	✓	✓			✓			300	6,312
<i>EMT</i> [9]	7	✓	✓	✓				✓	✓		100	790

PRODIGEN HAS BEEN TESTED WITH 111 DIFFERENT LOGS

- Based on the original model:

- ▷ Behavior similarity:

$$B_p(L, CM_o, CM_m) = \frac{\sum_{\sigma \in L} \left(\frac{L(\sigma)}{|\sigma|} \times \sum_{i=1}^{|\sigma|} \frac{|Enabled(CM_o, \sigma, i) \cap Enabled(CM_m, \sigma, i)|}{|Enabled(CM_m, \sigma, i)|} \right)}{\sum_{\sigma \in L} L(\sigma)}$$
$$B_r(L, CM_o, CM_m) = \frac{\sum_{\sigma \in L} \left(\frac{L(\sigma)}{|\sigma|} \times \sum_{i=1}^{|\sigma|} \frac{|Enabled(CM_o, \sigma, i) \cap Enabled(CM_m, \sigma, i)|}{|Enabled(CM_o, \sigma, i)|} \right)}{\sum_{\sigma \in L} L(\sigma)}$$

- ▷ Similarity from the structural point of view:

$$S_p(CM_o, CM_m) = \frac{|C_o \cap C_m|}{|C_m|}$$

$$S_r(CM_o, CM_m) = \frac{|C_o \cap C_m|}{|C_o|}$$

- Based on the log:

- ▷ **Proper completion:** percentage of correctly parsed traces.

- ▷ **Precision:** how much behavior of the log is allowed by the model

$$precision(L, M) = \frac{1}{|\mathcal{E}|} \sum_{e \in \mathcal{E}} \frac{|en_L(e)|}{|en_M(e)|}$$

- ▷ **Simplicity:** Weighted place/transition node arc degree

ProDiGen

Results on balanced logs (i)

		Logs with 0% of noise																			Logs with 1% of noise																		
		Caminatas	A8	D2	M1USkip	Ma5	M2I	MDriverLL	allLoops	Ma7	I2la	MeXsampleL	Herbato6p37	Ma6nc	MParallel85	NC	L2LP	NCB	DWS	Caminatas	A8	D2	M1USkip	Ma5	M2I	MDriverLL	allLoops	Ma7	I2la	MeXsampleL	Herbato6p37	Ma6nc	MParallel85	NC	L2LP	NCB	DWS		
ProDiGen	Model metrics	Bp	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
		Br	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
		Sp	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
		Sr	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0
	Log metrics	P	1.0	1.0	1.0	0.78	0.89	0.84	0.89	0.77	1.0	0.94	0.94	0.95	1.0	1.0	1.0	0.56	0.87	0.78	1.0	1.0	1.0	0.82	0.91	0.85	0.9	0.86	1.0	0.96	0.96	0.96	1.0	1.0	1.0	0.56	0.87	0.78	
		C	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	
		S	0.25	0.32	0.3	0.31	0.3	0.34	0.28	0.29	0.28	0.29	0.29	0.34	0.31	0.31	0.29	0.31	0.31	0.3	0.25	0.32	0.3	0.32	0.31	0.34	0.29	0.3	0.29	0.3	0.3	0.34	0.32	0.31	0.3	0.31	0.31	0.3	
GM	Model metrics	Bp	0.84	1.0	1.0	1.0	0.96	1.0	0.9	0.99	0.95	1.0	0.94	1.0	0.98	0.74	1.0	1.0	1.0	1.0	0.68	1.0	0.95	0.99	0.97	1.0	0.92	0.99	0.82	1.0	1.0	1.0	0.98	0.8	1.0	1.0	1.0	0.86	
		Br	0.98	1.0	1.0	1.0	1.0	1.0	0.99	0.99	1.0	0.97	1.0	1.0	0.97	1.0	1.0	1.0	1.0	1.0	0.99	0.99	1.0	0.96	0.99	0.99	1.0	1.0	0.99	1.0	0.99	1.0	0.98	1.0	1.0	1.0	0.81		
		Sp	0.85	1.0	1.0	1.0	1.0	1.0	0.93	0.98	0.94	1.0	0.86	1.0	0.96	0.08	1.0	1.0	1.0	1.0	0.79	0.8	1.0	1.0	0.91	0.88	0.94	1.0	0.75	1.0	1.0	0.95	0.96	0.85	1.0	1.0	1.0	0.83	
		Sr	0.73	1.0	1.0	1.0	0.91	1.0	0.84	0.96	0.97	1.0	0.88	1.0	0.99	0.98	1.0	1.0	1.0	1.0	0.67	1.0	0.87	0.92	0.91	1.0	0.85	0.96	1.0	1.0	1.0	1.0	0.99	0.93	1.0	1.0	0.95		
	Log metrics	P	0.81	1.0	1.0	0.78	0.86	0.84	0.81	0.68	0.68	0.94	0.91	0.95	0.81	0.89	1.0	0.56	0.87	0.78	0.0	1.0	0.64	0.78	0.89	0.73	0.78	0.68	0.77	0.96	0.96	0.9	0.93	0.75	1.0	0.56	0.87	0.71	
		C	0.36	1.0	1.0	1.0	1.0	1.0	0.48	0.15	1.0	0.52	1.0	1.0	0.81	1.0	1.0	1.0	1.0	1.0	0.23	1.0	1.0	1.0	1.0	1.0	1.0	0.49	1.0	1.0	1.0	1.0	0.14	1.0	1.0	1.0	0.82		
		S	0.29	0.32	0.3	0.31	0.32	0.34	0.3	0.28	0.28	0.29	0.31	0.34	0.31	0.29	0.29	0.31	0.31	0.3	0.29	0.29	0.29	0.29	0.32	0.32	0.3	0.29	0.29	0.3	0.3	0.33	0.31	0.27	0.3	0.31	0.31	0.29	
HM	Model metrics	Bp	1.0	1.0	1.0	0.97	1.0	1.0	1.0	0.96	1.0	1.0	1.0	1.0	0.91	1.0	0.44	0.82	0.88	0.89	1.0	1.0	1.0	0.97	1.0	1.0	0.93	0.96	1.0	1.0	1.0	1.0	0.9	1.0	0.87	0.82	0.88	0.89	
		Br	1.0	1.0	1.0	0.95	1.0	1.0	1.0	0.92	1.0	1.0	1.0	1.0	1.0	1.0	0.82	0.93	1.0	0.94	1.0	1.0	1.0	0.92	1.0	1.0	1.0	0.92	1.0	1.0	1.0	1.0	1.0	1.0	0.93	1.0	0.94		
		Sp	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.9	1.0	0.83	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.9	1.0	0.81		
		Sr	1.0	1.0	1.0	0.82	1.0	1.0	1.0	0.83	1.0	1.0	1.0	1.0	0.9	1.0	0.91	0.9	0.88	1.0	1.0	1.0	1.0	0.76	1.0	1.0	0.9	0.83	1.0	1.0	1.0	1.0	0.91	1.0	0.91	0.9	0.88	1.0	
	Log metrics	P	1.0	1.0	1.0	0.71	0.89	0.84	0.89	0.8	1.0	0.94	0.94	0.95	0.89	1.0	0.84	0.65	0.0	0.82	1.0	1.0	1.0	0.71	0.91	0.85	0.81	0.87	1.0	0.96	0.96	0.96	0.91	1.0	0.88	0.65	0.0	0.82	
		C	1.0	1.0	1.0	0.84	1.0	1.0	1.0	0.73	1.0	1.0	1.0	1.0	0.69	1.0	0.84	0.24	0.0	0.51	1.0	1.0	1.0	0.84	1.0	1.0	1.0	0.73	1.0	1.0	1.0	1.0	0.69	1.0	0.84	0.24	0.0	0.51	
		S	0.25	0.32	0.3	0.32	0.3	0.34	0.28	0.27	0.28	0.29	0.29	0.34	0.33	0.31	0.31	0.3	0.32	0.3	0.25	0.32	0.3	0.32	0.31	0.34	0.3	0.28	0.29	0.3	0.3	0.34	0.33	0.31	0.32	0.3	0.32	0.3	
α^{++}	Model metrics	Bp	1.0	1.0	1.0	1.0	1.0	1.0	0.87	0.77	1.0	1.0	1.0	1.0	1.0	1.0	0.59	0.88	0.75	0.76	0.82	1.0	0.73	0.84	0.76	0.77	0.94	0.83	0.73	0.4	0.41	0.6	0.87	0.76	0.77	0.88	0.46		
		Br	1.0	1.0	1.0	1.0	1.0	1.0	0.89	0.83	1.0	1.0	1.0	1.0	1.0	1.0	0.72	1.0	0.63	0.87	0.87	1.0	0.63	0.82	0.69	0.75	0.83	0.85	0.6	0.7	0.52	0.78	0.99	0.86	0.56	1.0	0.45		
		Sp	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.72	1.0	0.81	0.93	0.77	1.0	0.81	0.83	1.0	0.79	0.81	0.83	0.69	0.69	0.46	0.68	0.68	0.84	1.0	1.0	0.74		
		Sr	1.0	1.0	1.0	1.0	1.0	1.0	0.9	0.83	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.88	1.0	1.0	1.0	1.0	0.69	0.83	0.75	0.9	0.75	0.83	0.81	0.75	0.61	0.91	0.86	0.91	0.6	0.88	0.9		
	Log metrics	P	1.0	1.0	1.0	0.78	0.89	0.84	0.95	0.74	1.0	0.94	0.94	0.95	1.0	1.0	1.0	0.0	0.0	0.0	0.0	1.0	1.0	0.0	0.87	0.68	0.0	0.82	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
		C	1.0	1.0	1.0	1.0	1.0	1.0	0.63	0.25	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.5	1.0	1.0	1.0	1.0	0.0	0.25	1.0	0.0	0.0	0.0	0.0	0.0	1.0	0.0	0.0	0.0	
		S	0.25	0.32	0.3	0.31	0.3	0.34	0.26	0.3	0.28	0.29	0.29	0.34	0.31	0.31	0.29	0.24	0.32	0.27	0.24	0.31	0.3	0.29	0.26	0.35	0.13	0.27	0.3	0.28	0.28	0.3	0.24	0.28	0.28	0.24	0.29	0.19	
ILP	Model metrics	Bp	1.0	1.0	1.0	1.0	1.0	1.0	0.86	0.81	1.0	1.0	1.0	1.0	1.0	1.0	0.63	1.0	0.82	0.3	0.39	0.64	0.58	0.84	0.63	0.32	0.31	0.42	0.48	0.47	0.33	0.47	0.3	0.52	0.62	0.63	0.42		
		Br	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.92	1.0	1.0	1.0	1.0	1.0	1.0	0.9	1.0	0.97	0.68	0.56	0.83	0.75	0.89	0.9	0.68	0.53	0.69	0.7	0.75	0.89	0.78	0.74	0.84	0.9	0.99	0.56		
		Sp	1.0	1.0	1.0	1.0	1.0	1.0	0.86	0.54	1.0	1.0	1.0	1.0	1.0	1.0	0.66	1.0	0.66	0.28	0.53	0.63	0.69	0.75	0.76	0.32	0.53	0.43	0.34	0.41	0.87	0.49	0.45	0.45	0.66	0.66	0.29		
		Sr	1.0	1.0	1.0	1.0	1.0	1.0	0.93	0.71	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	
	Log metrics	P	1.0	1.0	1.0	0.78	0.89	0.84	0.81	0.77	1.0	0.94	0.94	0.95	1.0	1.0	1.0	0.48	0.87	0.72	0.48	0.51	0.73	0.64	0.87	0.55	0.54	0.65	0.58	0.0	0.75	0.56	0.63	0.74	0.64	0.48	0.54	0.52	
		C	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.5	1.0	1.0	1.0	1.0	1.0	1.0	0.0	0.0	0.49	1.0	1.0	1.0	1.0	1.0	0.82		
		S	0.25	0.32	0.3	0.31	0.3	0.34	0.28	0.25	0.28	0.29	0.29	0.34	0.31	0.31	0.29	0.3	0.31	0.25	0.16	0.27	0.25	0.26	0.26	0.32	0.15	0.19	0.21	0.19	0.24	0.27	0.24	0.21	0.2	0.3	0.3	0.14	

ProDiGen

Experimentation - Results on balanced logs (i)

		Logs with 5% of noise																	Logs with 10% of noise																			
		CaminateA8-	D2	M11Skip	Ma5	M21	MDrivenLensed	allLoops	Ma7	I21a	MetamorphicLog	MherbstFig6p37	Ma6ofc	MParallel5	NC	L2LP	NCB	DWS	CaminateA8-	D2	M11Skip	Ma5	M21	MDrivenLensed	allLoops	Ma7	I21a	MetamorphicLog	MherbstFig6p37	Ma6ofc	MParallel5	NC	L2LP	NCB	DWS			
ProDiGen	Model metrics	B _p	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.57	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0			
		B _r	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.99	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0			
		S _p	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.73	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0		
		S _r	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.78	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0		
	Log metrics	P	1.0	1.0	1.0	0.82	0.91	0.85	0.9	0.85	1.0	0.96	0.96	0.96	1.0	1.0	1.0	0.56	0.87	0.78	0.86	1.0	1.0	0.82	0.91	0.86	0.9	0.86	1.0	0.96	0.96	1.0	1.0	1.0	0.56	0.87	0.78	
C	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0			
S	0.25	0.32	0.3	0.32	0.31	0.34	0.29	0.3	0.29	0.3	0.3	0.34	0.32	0.31	0.3	0.31	0.31	0.3	0.25	0.32	0.3	0.32	0.31	0.34	0.29	0.3	0.29	0.3	0.3	0.34	0.32	0.31	0.3	0.31	0.31	0.3		
GM	Model metrics	B _p	0.8	0.91	0.94	0.99	0.84	1.0	0.88	0.99	0.94	0.94	0.87	0.79	1.0	0.86	0.85	0.95	1.0	0.86	0.92	0.83	0.8	1.0	0.87	1.0	0.92	0.99	0.77	0.87	0.99	0.92	0.88	0.86	0.89	1.0	0.82	0.84
		B _r	0.99	0.99	0.99	0.96	0.99	0.99	0.99	0.99	0.99	0.99	0.98	0.99	0.99	0.99	1.0	1.0	0.81	0.99	0.99	0.99	0.99	0.99	1.0	0.99	0.99	0.99	0.99	1.0	0.99	0.99	0.99	0.99	0.99	0.83		
		S _p	0.66	0.77	0.77	0.92	0.66	0.88	0.8	1.0	0.8	0.9	0.68	0.76	0.92	0.66	0.69	0.9	1.0	0.83	0.84	0.6	0.75	0.92	0.9	0.88	0.9	0.98	0.57	0.75	0.92	0.95	0.83	0.66	0.91	0.9	0.72	0.79
		S _r	0.5	0.87	0.87	0.92	0.66	1.0	0.76	0.96	1.0	0.9	0.91	0.95	1.0	0.66	0.75	0.9	1.0	0.95	0.78	0.75	0.75	1.0	0.83	1.0	0.85	0.96	0.66	0.81	1.0	0.95	0.83	0.66	0.91	1.0	0.88	0.95
	Log metrics	P	0.68	0.64	0.87	0.68	0.66	0.66	0.54	0.6	0.78	0.86	0.54	0.61	0.92	0.47	0.63	0.55	0.87	0.6	0.79	0.56	0.46	0.68	0.51	0.44	0.63	0.51	0.52	0.44	0.67	0.75	0.43	0.58	0.76	0.58	0.57	0.54
C	0.22	1.0	1.0	1.0	0.69	1.0	0.38	1.0	0.86	1.0	1.0	0.76	1.0	1.0	0.55	0.77	1.0	0.27	0.23	0.5	1.0	1.0	1.0	1.0	0.61	0.59	1.0	0.53	1.0	1.0	1.0	0.17	1.0	1.0	0.57			
S	0.29	0.28	0.29	0.27	0.3	0.32	0.28	0.28	0.26	0.3	0.28	0.31	0.29	0.29	0.28	0.31	0.31	0.29	0.28	0.28	0.29	0.29	0.29	0.3	0.28	0.28	0.27	0.29	0.28	0.32	0.29	0.28	0.28	0.29	0.3	0.28		
HM	Model metrics	B _p	0.96	1.0	1.0	0.97	0.92	0.91	0.92	0.93	1.0	1.0	1.0	1.0	0.9	1.0	0.87	0.77	0.88	0.77	0.96	1.0	0.91	1.0	0.92	0.86	0.92	0.93	1.0	0.94	1.0	1.0	0.9	1.0	0.87	0.96	0.88	0.86
		B _r	1.0	1.0	1.0	0.92	0.79	0.99	0.95	0.83	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.95	1.0	0.94	1.0	1.0	1.0	0.89	0.79	0.99	0.95	0.91	1.0	1.0	1.0	1.0	1.0	1.0	0.9	1.0	0.81	
		S _p	1.0	1.0	1.0	1.0	1.0	0.88	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.8	1.0	0.83	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.9	1.0	0.83		
		S _r	0.92	1.0	1.0	0.76	0.91	1.0	0.9	0.83	1.0	1.0	1.0	1.0	1.0	0.91	1.0	0.91	0.8	0.88	1.0	0.93	1.0	0.75	0.84	1.0	1.0	0.9	0.83	1.0	0.9	1.0	1.0	0.91	1.0	0.91	0.9	0.88
	Log metrics	P	0.92	1.0	1.0	0.0	0.0	0.57	0.88	0.89	1.0	0.96	0.96	0.96	0.91	1.0	0.88	0.55	0.0	0.0	1.0	1.0	0.92	0.0	0.0	0.57	0.89	0.82	1.0	0.89	0.96	0.96	0.91	1.0	0.88	0.0	0.0	0.0
C	0.66	1.0	1.0	0.0	0.0	1.0	0.63	0.26	1.0	1.0	1.0	1.0	0.69	1.0	0.85	0.77	0.0	0.0	1.0	1.0	1.0	0.9	0.0	1.0	0.62	0.34	1.0	0.3	1.0	1.0	0.69	1.0	0.84	0.0	0.0	0.0		
S	0.29	0.32	0.3	0.31	0.32	0.33	0.3	0.28	0.29	0.3	0.3	0.34	0.33	0.31	0.32	0.31	0.32	0.29	0.25	0.32	0.33	0.31	0.31	0.32	0.3	0.3	0.29	0.32	0.3	0.34	0.33	0.31	0.32	0.3	0.32	0.29		
α ⁺⁺	Model metrics	B _p	0.73	0.81	0.69	0.34	0.75	0.63	0.38	0.68	0.83	0.72	0.55	0.38	0.8	0.45	0.75	0.76	0.23	0.57	0.85	0.84	0.84	0.86	0.64	0.61	0.35	0.74	0.84	0.65	0.63	0.33	0.54	0.63	0.62	0.68	0.32	0.43
		B _r	0.69	0.99	0.83	0.32	0.88	0.68	0.49	0.67	0.97	0.65	0.6	0.47	0.88	0.54	0.99	0.56	0.24	0.66	0.95	0.99	0.99	0.66	0.64	0.65	0.45	0.77	0.99	0.68	0.69	0.41	0.6	0.75	0.97	0.52	0.36	0.56
		S _p	0.62	0.41	0.57	0.31	0.46	0.3	0.41	0.5	0.47	0.43	0.36	0.4	0.55	0.37	0.5	0.6	0.5	0.48	0.61	0.46	0.71	0.46	0.3	0.35	0.35	0.41	0.44	0.58	0.37	0.36	0.31	0.29	0.25	0.45	0.66	0.31
		S _r	0.82	0.62	0.5	0.38	0.5	0.37	0.57	0.58	0.66	0.63	0.66	0.56	0.91	0.6	0.83	0.6	0.66	0.72	0.75	0.75	0.62	0.53	0.5	0.62	0.61	0.41	0.66	0.63	0.75	0.45	0.58	0.66	0.33	0.5	0.44	0.42
	Log metrics	P	0.0	0.69	0.95	0.0	0.75	0.0	0.0	0.0	0.85	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.85	0.85	0.0	0.0	0.0	0.0	0.0	0.77	0.71	0.0	0.0	0.0	0.0	0.76	0.7	0.0	0.0
C	0.0	0.49	1.0	0.0	1.0	0.0	0.0	0.0	0.86	0.0	0.0	0.0	0.69	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1.0	1.0	0.0	0.0	1.0	0.0	0.0	0.57	0.82	0.0	0.0	0.0	0.0	0.84	1.0	0.0	0.0	
S	0.18	0.27	0.32	0.18	0.29	0.21	0.11	0.16	0.25	0.17	0.2	0.34	0.25	0.25	0.21	0.21	0.18	0.16	0.21	0.27	0.32	0.19	0.19	0.22	0.13	0.19	0.25	0.21	0.2	0.34	0.21	0.21	0.25	0.29	0.31	0.15		
ILP	Model metrics	B _p	0.13	0.15	0.24	0.48	0.31	0.14	0.07	0.27	0.05	0.14	0.18	0.1	0.24	0.34	0.28	0.36	0.26	0.25	0.16	0.25	0.2	0.33	0.32	0.2	0.12	0.28	0.21	0.12	0.15	0.05	0.13	0.17	0.1	0.41	0.24	0.15
		B _r	0.3	0.48	0.83	0.33	0.62	0.42	0.21	0.81	0.17	0.44	0.36	0.45	0.59	0.64	0.4	0.69	0.75	0.49	0.25	0.72	0.58	0.47	0.64	0.5	0.19	0.64	0.38	0.42	0.29	0.15	0.43	0.29	0.32	0.72	0.47	0.24
		S _p	0.23	0.23	0.32	0.26	0.26	0.17	0.16	0.33	0.23	0.21	0.13	0.09	0.16	0.16	0.23	0.3	0.27	0.13	0.24	0.19	0.34	0.27	0.18	0.18	0.15	0.36	0.19	0.25	0.16	0.06	0.16	0.13	0.18	0.28	0.28	0.12
		S _r	1.0	1.0	1.0	0.8	0.95	0.93	1.0	1.0	1.0	1.0	0.92	0.92	0.94	1.0	0.78	1.0	0.91	0.96	1.0	0.83	0.8	1.0	0.87	1.0	1.0	0.95	1.0	1.0	1.0	1.0	1.0	0.93	1.0	1.0	0.92	
	Log metrics	P	0.32	0.41	0.42	0.31	0.0	0.27	0.18	0.45	0.58	0.3	0.39	0.0	0.42	0.42	0.48	0.33	0.31	0.36	0.36	0.41	0.44	0.34	0.0	0.26	0.17	0.45	0.43	0.37	0.37	0.0	0.37	0.3	0.32	0.36	0.28	0.28
C	1.0	1.0	1.0	1.0	0.0	1.0	0.63	1.0	0.57	1.0	0.48	0.0	1.0	0.0	1.0	0.0	1.0	1.0	0.5	0.13	1.0	1.0	1.0	0.0	1.0	0.62	1.0	1.0	1.0	0.5	0.0	0.69	1.0	1.0	1.0	0.26		
S	0.1	0.18																																				

			Logs with 20% of noise																			
			Caminatas	A8	D2	MUSkip	Ma5	M2L	MDriverLL	aILoops	Ma7	I2a	MeXempl.	Herbst6p17	Madafic	MParallel5	NC	L2LP	NCB	DWS-20		
ProDiGen	Model metrics	B_p	0.57	1.0	0.91	1.0	1.0	1.0	0.62	1.0	0.78	0.8	0.75	1.0	0.75	0.92	0.72	1.0	1.0	0.5		
		B_r	0.99	1.0	1.0	1.0	1.0	1.0	0.99	1.0	0.99	0.99	0.99	1.0	0.99	0.99	0.99	1.0	1.0	0.99		
		S_p	0.75	1.0	0.87	1.0	1.0	1.0	0.77	1.0	0.79	0.81	0.76	1.0	0.76	0.78	0.76	1.0	1.0	0.47		
		S_r	0.85	1.0	0.87	1.0	1.0	1.0	0.89	1.0	1.0	1.0	0.83	1.0	0.83	0.84	0.75	1.0	1.0	0.95		
	Log metrics	P	0.62	1.0	0.95	0.81	0.91	0.85	0.89	0.35	1.0	0.95	0.9	0.95	0.68	0.79	0.7	0.55	0.86	0.75		
		C	0.34	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.52	1.0	0.69	0.72	0.62	1.0	1.0	0.37		
		S	0.27	0.31	0.31	0.31	0.3	0.33	0.28	0.29	0.28	0.29	0.3	0.33	0.3	0.29	0.29	0.3	0.3	0.28		
		GM	Model metrics	B_p	0.56	0.67	0.66	0.85	0.82	1.0	0.44	0.9	0.67	0.77	0.73	0.59	0.65	0.83	0.57	0.95	0.88	0.78
B_r	0.99			0.99	0.99	0.99	0.99	0.99	0.98	0.98	0.99	0.99	0.99	0.97	0.99	0.99	0.99	0.99	0.99	0.81		
S_p	0.56			0.46	0.6	0.69	0.72	0.88	0.52	0.88	0.47	0.69	0.64	0.44	0.61	0.52	0.5	0.9	0.8	0.6		
S_r	0.6			0.75	0.75	0.69	0.66	1.0	0.52	0.95	0.66	0.81	0.91	0.65	0.66	0.66	0.66	0.9	0.88	0.95		
Log metrics	P		0.39	0.42	0.45	0.65	0.36	0.65	0.0	0.46	0.42	0.42	0.38	0.0	0.38	0.59	0.37	0.31	0.51	0.53		
	C		0.0	1.0	1.0	1.0	1.0	1.0	0.0	1.0	0.0	1.0	0.0	0.0	0.3	1.0	0.16	1.0	1.0	0.54		
	S		0.26	0.26	0.28	0.29	0.27	0.31	0.28	0.24	0.26	0.27	0.25	0.27	0.27	0.29	0.27	0.26	0.29	0.27		
	HM		Model metrics	B_p	0.97	0.7	0.95	0.9	0.9	0.67	0.9	0.93	1.0	0.94	1.0	1.0	0.89	1.0	0.75	0.77	0.88	0.7
B_r		1.0		0.85	1.0	0.8	0.89	0.91	0.92	0.89	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.95	1.0	0.6		
S_p		1.0		0.77	1.0	1.0	1.0	0.6	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.8	1.0	0.76		
S_r		0.95		0.87	0.87	0.76	0.83	0.75	0.9	0.83	1.0	0.9	1.0	1.0	0.91	1.0	0.83	0.8	0.88	0.95		
Log metrics		P	0.89	0.0	0.95	0.0	0.85	0.0	0.0	0.89	1.0	0.88	0.95	0.95	0.9	0.99	0.0	0.0	0.0	0.0		
		C	0.34	0.0	1.0	0.0	0.65	0.0	0.63	0.58	1.0	0.3	1.0	1.0	0.69	1.0	0.0	0.0	0.0	0.0		
		S	0.28	0.3	0.31	0.28	0.31	0.3	0.3	0.28	0.28	0.31	0.29	0.33	0.32	0.3	0.32	0.3	0.32	0.28		
		α^{++}	Model metrics	B_p	0.83	0.88	0.84	0.39	0.61	0.4	0.29	0.73	0.76	0.42	0.4	0.29	0.44	0.75	0.53	0.62	0.29	0.26
B_r	0.91			0.99	0.99	0.55	0.56	0.49	0.4	0.82	0.87	0.57	0.75	0.42	0.76	0.99	0.89	0.54	0.4	0.24		
S_p	0.59			0.46	0.62	0.23	0.26	0.26	0.18	0.2	0.27	0.25	0.17	0.21	0.23	0.22	0.26	0.15	0.27	0.29		
S_r	0.67			0.75	0.62	0.23	0.5	0.5	0.28	0.16	0.41	0.27	0.33	0.3	0.41	0.46	0.33	0.2	0.33	0.42		
Log metrics	P		0.0	0.72	0.84	0.0	0.0	0.54	0.0	0.6	0.65	0.0	0.59	0.95	0.0	0.75	0.0	0.0	0.0	0.0		
	C		0.0	0.49	1.0	0.0	0.0	1.0	0.0	0.24	1.0	0.0	0.52	1.0	0.0	1.0	0.83	0.0	0.0	0.0		
	S		0.2	0.25	0.29	0.15	0.17	0.31	0.08	0.28	0.24	0.15	0.2	0.33	0.21	0.21	0.24	0.16	0.19	0.14		
	ILP		Model metrics	B_p	0.1	0.09	0.27	0.35	0.31	0.11	0.24	0.29	0.17	0.1	0.2	0.05	0.07	0.2	0.17	0.35	0.41	0.14
B_r		0.19		0.23	0.83	0.46	0.57	0.27	0.19	0.63	0.34	0.33	0.31	0.06	0.31	0.35	0.49	0.75	0.84	0.21		
S_p		0.23		0.23	0.45	0.28	0.21	0.17	0.19	0.26	0.2	0.22	0.14	0.05	0.14	0.1	0.19	0.29	0.25	0.12		
S_r		1.0		0.64	0.8	1.0	1.0	1.0	0.93	0.7	0.97	1.0	1.0	1.0	0.77	0.76	1.0	1.0	1.0	0.96		
Log metrics		P	0.31	0.4	0.0	0.3	0.28	0.2	0.16	0.44	0.38	0.27	0.3	0.13	0.28	0.26	0.31	0.26	0.22	0.22		
		C	0.24	1.0	0.0	1.0	0.0	1.0	1.0	0.39	1.0	1.0	0.52	0.0	0.0	0.0	1.0	1.0	1.0	0.25		
		S	0.08	0.13	0.26	0.14	0.12	0.12	0.08	0.22	0.14	0.12	0.11	0.04	0.12	0.1	0.16	0.18	0.16	0.07		

ProDiGen

Results on unbalanced logs

			Logs																								
			\mathcal{L}_2	\mathcal{L}_3	\mathcal{L}_4	\mathcal{L}_5	\mathcal{L}_6	\mathcal{L}_7	\mathcal{L}_8	\mathcal{L}_9	\mathcal{L}_{10}	\mathcal{L}_{12}	\mathcal{L}_{13}	\mathcal{L}_{14}	\mathcal{L}_{15}	\mathcal{L}_{19}	\mathcal{L}_{20}	\mathcal{L}_{21}	\mathcal{L}_{22}	\mathcal{L}_{23}	\mathcal{L}_{24}	\mathcal{L}_{25}	EMT				
ProDiGen	Model metrics	B_p	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.96	1.0			
		B_r	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.99	1.0			
		S_p	1.0	1.0	0.96	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.91	1.0			
		S_r	1.0	1.0	0.97	1.0	1.0	1.0	0.94	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.98	0.91	1.0			
		P	0.9	0.82	0.98	0.98	0.95	0.88	0.86	0.92	0.89	0.97	0.93	0.93	0.86	0.92	0.78	0.91	0.9	0.58	0.89	0.74	0.87				
	Log metrics	C	1.0	1.0	1.0	1.0	1.0	1.0	0.52	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.98	1.0			
		S	0.3	0.3	0.3	0.31	0.31	0.32	0.28	0.31	0.3	0.31	0.3	0.31	0.3	0.31	0.25	0.3	0.29	0.31	0.3	0.3	0.29	0.31	0.27		
		GM	B_p	1.0	0.61	0.78	1.0	1.0	1.0	0.84	0.96	0.99	1.0	0.98	0.61	0.8	0.98	1.0	1.0	0.97	0.57	0.83	0.81	1.0			
			B_r	1.0	0.97	0.97	1.0	1.0	1.0	1.0	1.0	0.97	1.0	0.99	1.0	0.97	0.9	1.0	1.0	1.0	0.88	0.88	0.96	0.83			
			S_p	1.0	0.81	0.81	1.0	1.0	1.0	1.0	0.97	0.9	1.0	0.95	0.95	0.88	0.95	1.0	1.0	0.85	0.76	0.75	0.76	0.85			
S_r	1.0		0.81	0.81	1.0	1.0	1.0	0.94	0.98	0.92	1.0	0.94	0.94	0.87	0.89	1.0	1.0	0.85	0.74	0.75	0.74	0.85					
P	0.9		0.42	0.98	0.98	0.95	0.88	0.0	0.94	0.91	0.97	0.96	0.74	0.0	0.0	0.78	0.91	0.86	0.0	0.88	0.49	0.81					
Log metrics	C	1.0	0.31	0.59	1.0	1.0	1.0	0.26	0.48	0.48	1.0	0.75	1.0	0.15	0.2	1.0	1.0	0.43	0.2	0.72	0.41	0.3					
	S	0.3	0.31	0.3	0.31	0.31	0.32	0.26	0.3	0.29	0.31	0.3	0.31	0.24	0.29	0.29	0.31	0.3	0.28	0.3	0.28	0.3					
	HM	B_p	1.0	1.0	0.94	1.0	0.9	0.97	0.87	1.0	0.96	1.0	1.0	0.97	0.96	0.97	1.0	1.0	0.99	0.6	0.92	0.76	0.81				
		B_r	1.0	0.98	0.92	1.0	0.98	0.97	0.99	0.98	0.95	1.0	1.0	0.97	0.98	1.0	1.0	1.0	0.99	1.0	0.88	0.94	0.96				
		S_p	1.0	0.97	0.96	1.0	0.93	0.97	0.95	1.0	0.96	1.0	1.0	0.96	1.0	1.0	1.0	1.0	0.97	0.91	0.89	0.85	0.76				
S_r		1.0	0.97	0.86	1.0	0.97	1.0	0.86	1.0	0.96	1.0	1.0	0.92	0.86	0.9	1.0	1.0	0.91	0.94	0.81	0.85	0.74					
P		0.9	0.83	0.0	0.98	0.93	0.9	0.86	0.93	0.9	0.97	0.93	0.92	0.87	0.93	0.78	0.91	0.9	0.0	0.86	0.71	0.85					
Log metrics	C	1.0	1.0	1.0	1.0	0.66	1.0	0.52	0.74	0.78	1.0	1.0	0.91	0.87	0.85	1.0	1.0	0.9	0.0	0.93	0.23	0.37					
	S	0.3	0.3	0.31	0.31	0.31	0.31	0.28	0.31	0.3	0.31	0.3	0.32	0.26	0.3	0.29	0.31	0.3	0.29	0.29	0.3	0.29					
	α^{++}	B_p	0.8	0.81	0.95	1.0	0.88	0.92	0.87	0.96	0.94	0.95	0.93	0.58	0.85	0.9	0.64	0.84	0.93	0.71	0.81	0.94	0.99				
		B_r	0.85	0.91	0.94	1.0	0.99	0.9	0.94	0.94	0.9	1.0	0.94	0.92	0.85	0.94	0.94	0.89	0.85	0.67	0.7	0.92	0.93				
		S_p	0.89	0.94	0.98	1.0	0.79	0.98	0.83	0.98	0.81	0.96	0.88	0.86	0.9	0.9	0.92	0.93	0.82	0.66	0.85	0.91	1.0				
S_r		1.0	0.98	0.97	1.0	1.0	1.0	0.94	1.0	1.0	1.0	0.97	1.0	0.97	1.0	0.87	1.0	0.97	1.0	1.0	0.98	0.91					
P		0.86	0.0	0.95	0.98	0.94	0.0	0.85	0.94	0.91	0.94	0.95	0.75	0.0	0.9	0.64	0.0	1.0	0.0	0.0	0.0	0.99					
Log metrics	C	0.33	0.0	1.0	1.0	0.45	0.0	0.35	0.48	0.563	1.0	0.48	0.0	0.05	0.25	0.46	0.68	0.43	0.0	0.0	0.97	0.89					
	S	0.27	0.28	0.31	0.31	0.28	0.31	0.26	0.28	0.28	0.3	0.28	0.29	0.25	0.27	0.3	0.29	0.18	0.18	0.2	0.29	0.28					
	ILP	B_p	0.9	0.89	1.0	1.0	0.96	0.96	0.9	0.94	0.92	0.95	0.93	0.85	0.87	0.91	0.72	0.87	0.9	0.58	0.78	0.66	0.98				
		B_r	1.0	0.98	0.99	1.0	0.99	0.99	0.99	0.99	0.97	1.0	0.99	0.99	1.0	0.99	0.95	1.0	0.99	0.88	0.94	0.96	1.0				
		S_p	0.83	0.85	0.98	1.0	0.78	0.94	0.76	0.89	0.73	0.96	0.78	0.78	0.67	0.85	0.85	0.92	0.72	0.5	0.77	0.64	0.91				
S_r		1.0	0.98	0.97	1.0	1.0	1.0	0.96	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.97	1.0	1.0	0.98	1.0					
P		0.87	0.79	0.99	0.98	0.93	0.89	0.83	0.9	0.84	0.94	0.9	0.88	0.82	0.9	0.83	0.87	0.88	0.41	0.78	0.54	0.87					
Log metrics	C	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	1.0	0.52	1.0	0.98	1.0	1.0	1.0	1.0					
	S	0.29	0.29	0.29	0.31	0.28	0.31	0.25	0.3	0.26	0.3	0.3	0.27	0.23	0.28	0.27	0.31	0.23	0.17	0.26	0.25	0.27					

■ Friedman test and Holm post hoc test:

— Balanced Logs

Algorithm	Ranking
ProDiGen	1.52
HM	2.74
GM	2.89
ILP	3.74
α^{++}	4.10
Friedman p-value: 5.34E-11	

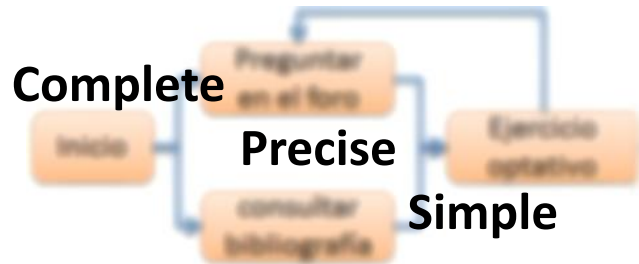
i	Comp.	z	p	α/i	Hypothesis
4	α^{++}	10.9	7.70E-28	0.012	Rejected
3	ILP	9.43	4.17E-21	0.016	Rejected
2	GM	5.80	6.70E-9	0.025	Rejected
1	HM	5.19	2.15E-7	0.05	Rejected

Unbalance Logs

Algorithm	Ranking
ProDiGen	1.55
HM	2.62
ILP	2.95
GM	3.62
α^{++}	4.26
Friedman p-value: 3.58E-7	

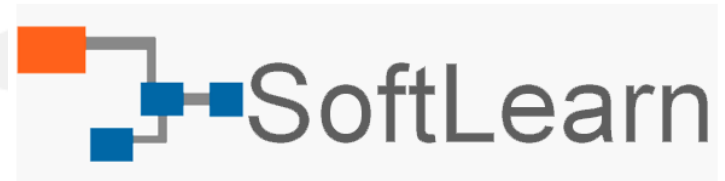
i	Comp.	z	p	α/i	Hypothesis
4	α^{++}	5.56	2.65E-8	0.012	Rejected
3	GM	4.25	2.18E-5	0.016	Rejected
2	ILP	2.88	0.003	0.025	Rejected
1	HM	2.20	0.03	0.05	Rejected

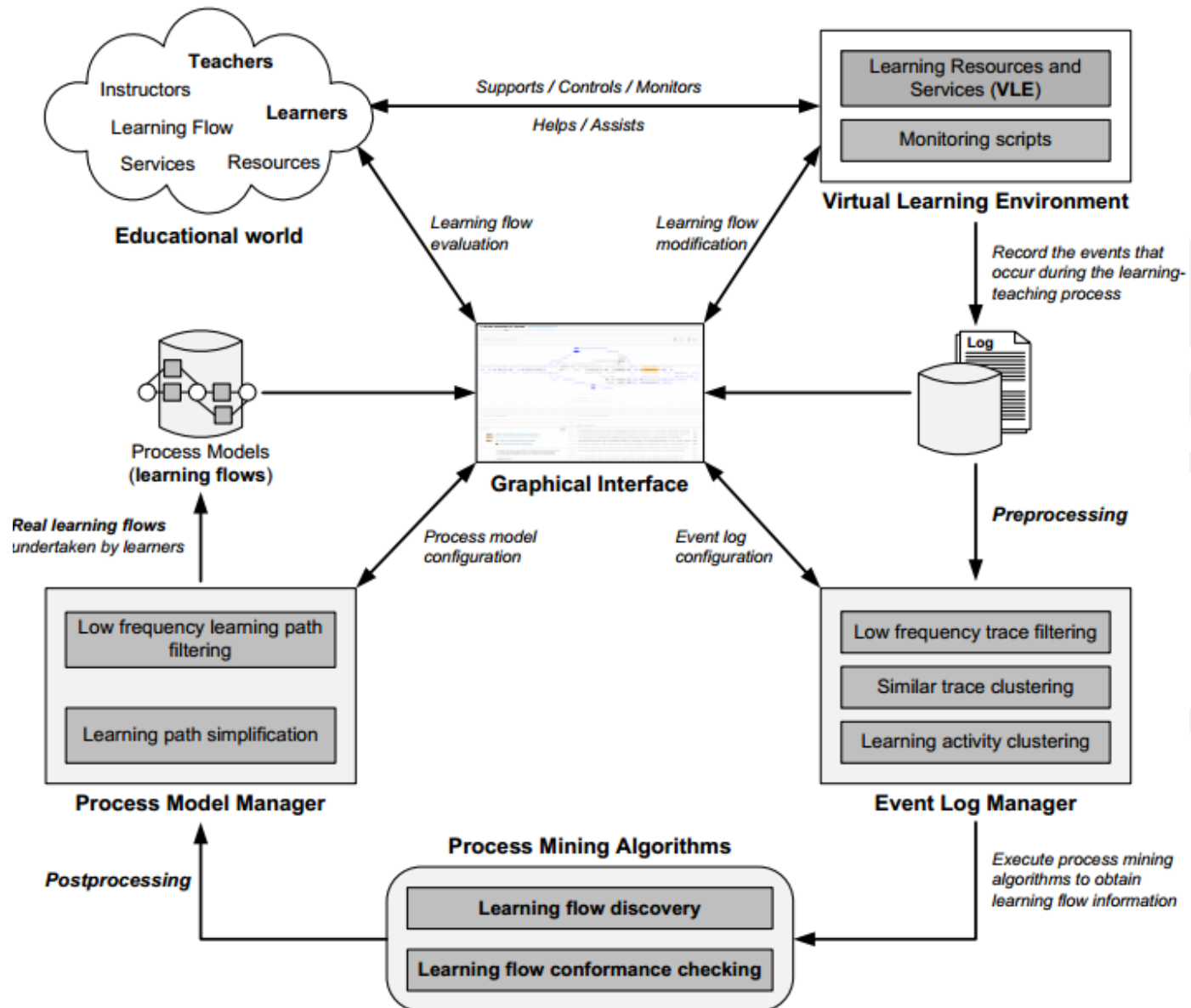
EDUCATION



Grade

- Evaluate learning paths from a virtual learning environment
- Intuitive GUI to visualize:
 - ▷ The real learning path of the course
 - ▷ The learning content generated in the VLE







- Integrated in the virtual learning environment Elgg.
- Used as evaluation software in the present course 13/14.
- **Tecnología Educativa**, *Departamento de Didáctica y Organización Escolar – USC*
 - ▷ **72** enrolled students.

So, WHAT'S NEXT?

1. Multi-objective algorithm.
2. Generalization
3. Conformance
4. Other domains: Medicine (**QUIRAV**)



JOURNALS

1. Borja Vazquez-Barreiros, Manuel Mucientes, Manuel Lama: ***ProDiGen: Mining complete, precise, and minimal structure process models with a genetic algorithm***. Information Sciences. (Under review)
 - JCR 3.64; Ranking 6/131 (Q1) in Computer Science, Information Systems

CONFERENCES

1. Borja Vazquez-Barreiros, Manuel Lama, Manuel Mucientes, Juan C. Vidal: ***SoftLearn, a process mining platform for the discovery of learning paths***. IEEE International Conference on Advanced Learning Technologies (ICALT 2014). (Accepted)
 - Ranking 8/58 in Computer Education
2. A. Rodriguez, A. Gewerc, M. Lama, B. Vazquez-Barreiros, M. Mucientes: ***Using a learning analytics tool for evaluation in self-regulated learning***. Frontiers in Education (FIE 2014) (Abstract accepted)
 - Ranking 7/58 in Computer Education

ProDiGen: a genetic algorithm for process discovery guided by completeness, precision and simplicity

Borja Vázquez Barreiros

Supervisors : Manuel Mucientes, Manuel Lama

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