

Classifiers for biosignal interpretation?

-Not beyond toy examples...

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Biosignal interpretation: The problem

For decades, a main objective of biosignal processing research has been to provide **classification algorithms** for identifying the underlying physiological phenomena from signal samples by using **pattern recognition**.



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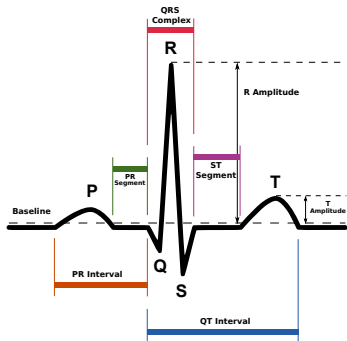
For decades, a main objective of biosignal processing research has been to provide **classification algorithms** for identifying the underlying physiological phenomena from signal samples by using **pattern recognition**.



But these signals usually show the **concurrence and interaction between complex processes**, having an extreme intrinsic variability.

Biosignal interpretation: Classical approaches

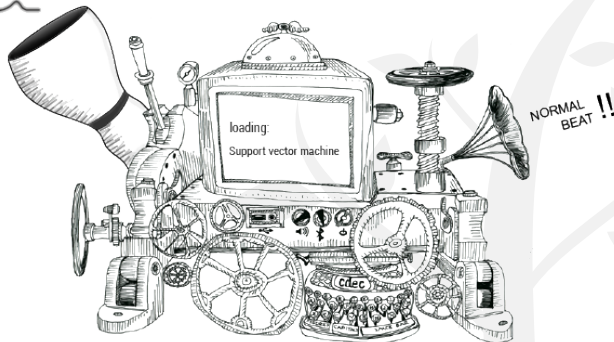
- **Knowledge Based Approaches:** Aim to model the domain knowledge or to simulate an expert reasoning process.



- **IF** {st_segment > 0.1s AND pq_interv < 0.8s} **THEN...**
- **IF** {t_amp / r_amp > 0.5 OR r_amp < 0.4mV} **THEN...**
- **IF** {qt ∈ [150, 420] AND # P AND QRS < 0.075s} **THEN...**
- ...

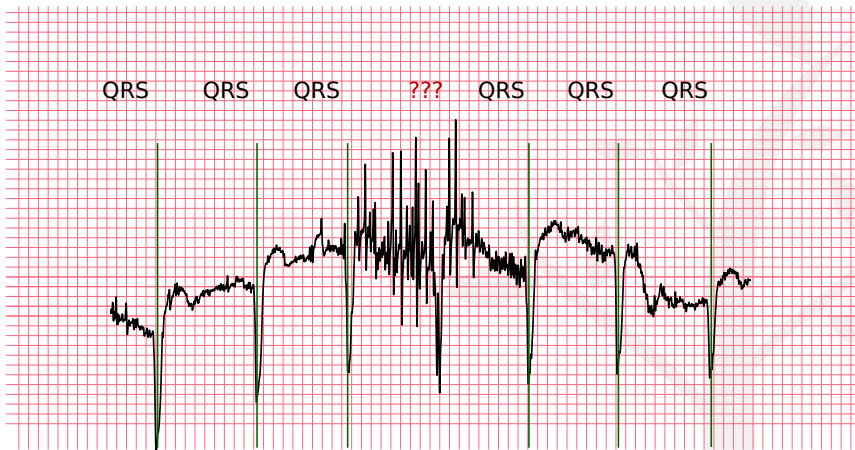
Biosignal interpretation: Classical approaches

- **Learning Based Approaches:** Build a model by estimating the underlying mechanisms that produce the data of a training set.



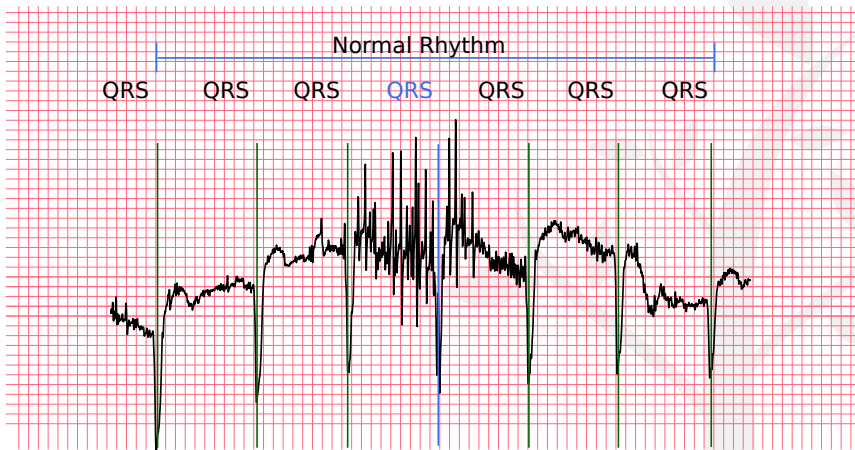
Biosignal interpretation: Classical approaches

Monotonic deductive reasoning cannot fix classification errors with posterior information.



Biosignal interpretation: Classical approaches

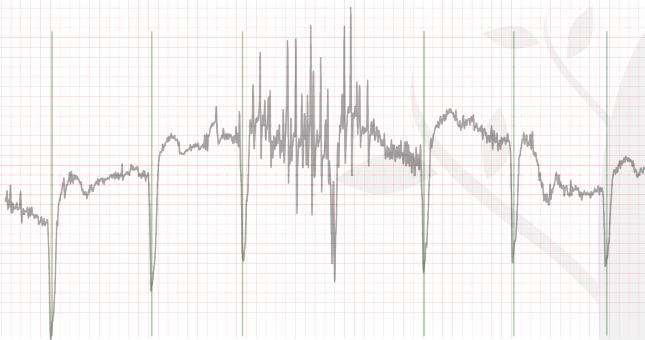
Monotonic deductive reasoning cannot fix classification errors with posterior information.



Biosignal interpretation: Classical approaches

Monotonic deductive reasoning cannot fix classification errors with posterior information.

You can ~~understand~~ understand this



Abductive Reasoning

- Abduction was defined by the philosopher C.S. Peirce as the **process of forming explanatory hypotheses**, illustrated by the following reasoning:

The surprising fact, C, is observed;

But if A were true, C would be a matter of course,

Hence, there is reason to suspect that A is true.

- Which is formalized in the logical formula:

$$\frac{C, A \rightarrow C}{A} \Rightarrow C \mid\!\!\!< A$$

- But A is not necessarily true. Abduction is **ampliative**, but **fallible**.

Observables

The **observable** $q = \langle \eta, \vec{A}, T_b, T_e \rangle$ is the basic representation entity of our framework, and has the following properties:

- η : Name of the observable.
- $\vec{A} = (A_1, \dots, A_{n_q})$: Set of attributes to be valued.
- T_b and T_e : Temporal variables representing the beginning and the end of the observable.

Example: QRS observable

$$q_{QRS} = \langle \text{QRS}, (\text{shape}, \text{amplitude}), T_b, T_e \rangle$$

An observable can be observed in multiple instances called **observations**, defined as $o = \langle \eta, \vec{v}, t_b, t_e \rangle$.

- $o_1 = \langle \text{QRS}, (\text{QS}, 0.94\text{mV}), 00:32.123, 00:32.201 \rangle$
- $o_2 = \langle \text{QRS}, (\text{rsR}', 1.92\text{mV}), 00:33.054, 00:33.139 \rangle$.

Interpretation Problem

Abstraction patterns define an abstraction relation between the observables of a domain, and are generated by the G^{ap} grammars, whose rules are of the following type:

$$H = q_H \rightarrow q[L]C$$

$$C \rightarrow q[L]D \mid q[L] \mid \lambda$$

- H is the hypothesis conjectured by the pattern.
- q is the observable predicted by the rule.
- $[L]$ is a set of temporal constraints between the observable generated by the rule and all the observables previously generated

Given $G \in G^{ap}$, an **abstraction pattern** $P = \langle q_H, M_P, N_P, \Pi_P \rangle$ is a tuple where:

- q_H is the hypothesized observable.
- $M_P = \{q_1, \dots, q_n\}$ is a set of findings that form the evidence supporting q_H .
- N_P is a temporal network between all the temporal variables of q_H and M_P .
- Π_P is an observation procedure to compute the attribute values of q_H .

$$\forall q_i \in M_P : q_i \prec q_H$$

The knowledge base of a particular domain is represented in a **domain model** $\mathcal{M} = \langle \mathcal{Q}, \mathcal{P} \rangle$ where:

- \mathcal{Q} is a set of domain observables.
- \mathcal{P} is a set of abstraction patterns involving those observables.

An interpretation problem

$IP = \langle \mathcal{O}, \mathcal{M} \rangle$ is defined by a set of initial observations \mathcal{O} and a domain model \mathcal{M} .

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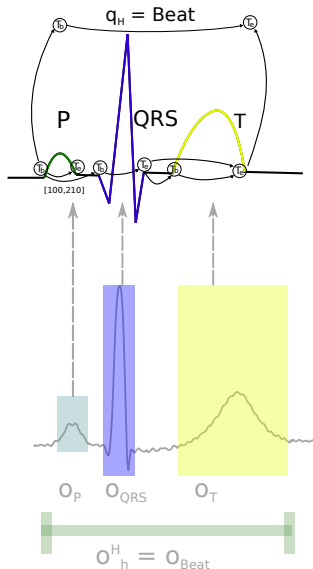
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Hypotheses and Interpretations



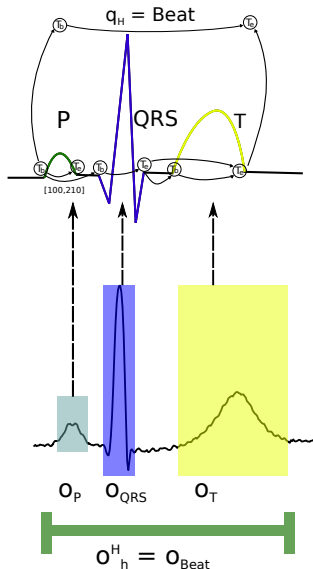
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An **interpretation** $I = \{h_1, \dots, h_m\}$ is a set of consistent abstraction hypotheses.

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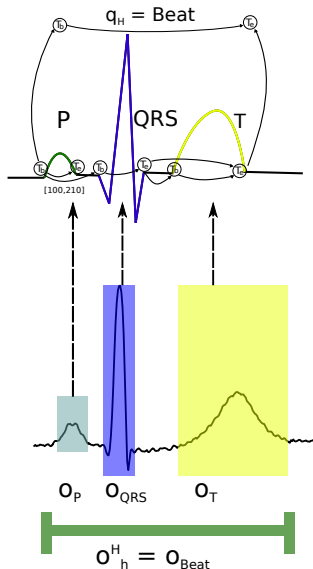
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Interpretation algorithm

Theorem:

Finding the solution of an interpretation problem is NP-Hard.

In order to reduce the complexity of the problem, we pose the interpretation algorithm as an *heuristic search process*, guided by the following general principles:

1. **Coverage principle:** An interpretation explaining more initial observations is better.
2. **Simplicity principle:** An interpretation with fewer hypotheses is better (Occam's razor).
3. **Abstraction principle:** An interpretation that uses terms of higher abstraction levels is better.
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Building an interpretation

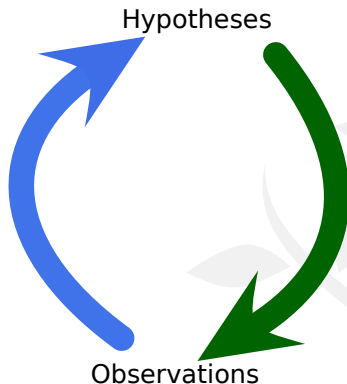
The interpretation is posed as a hypothesis-and-test cycle, in which a **focus of attention** determines what is the next reasoning step:

- **Abduction:**

Conjectures an hypothesis explaining the observation that is in the focus of attention.

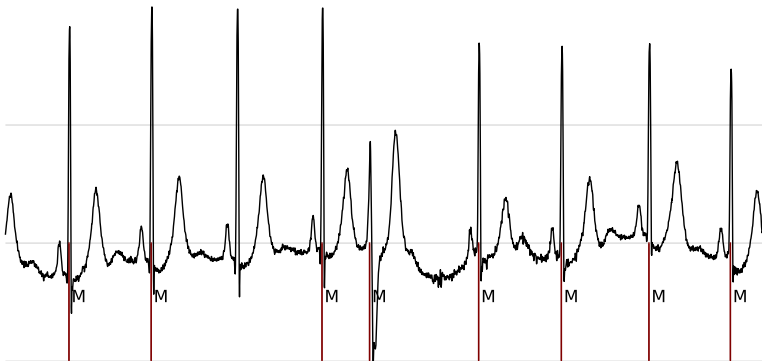
- **Subsumption:**

Matches an existing observation with a finding of an existing hypothesis.

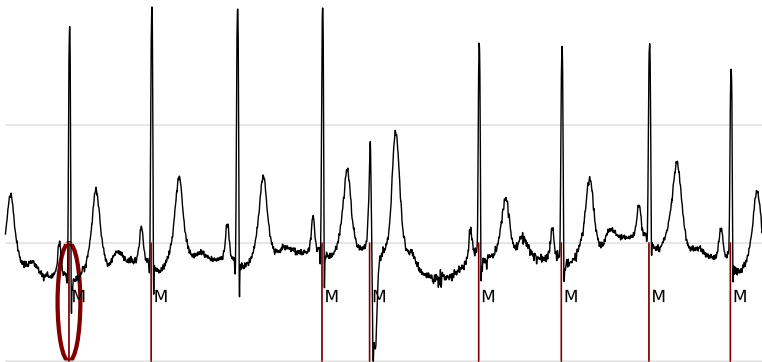


- **Deduction:** Looks for an observation predicted by the abstraction pattern that conjectured a hypothesis.

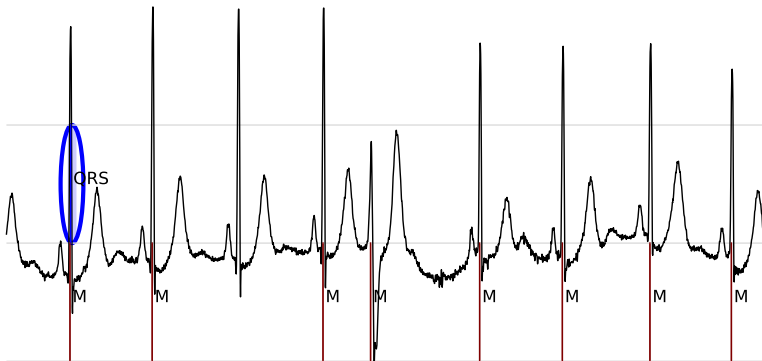
Interpretation example



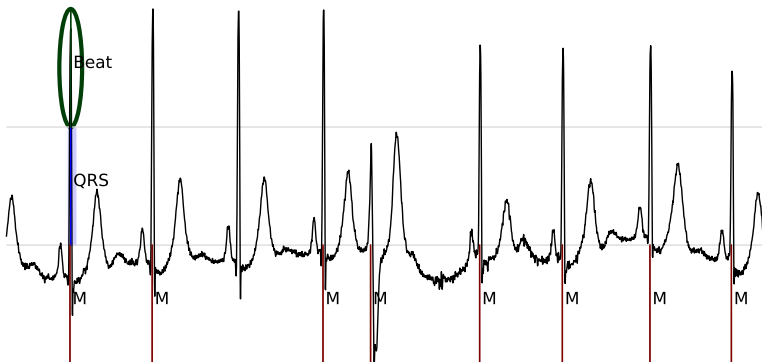
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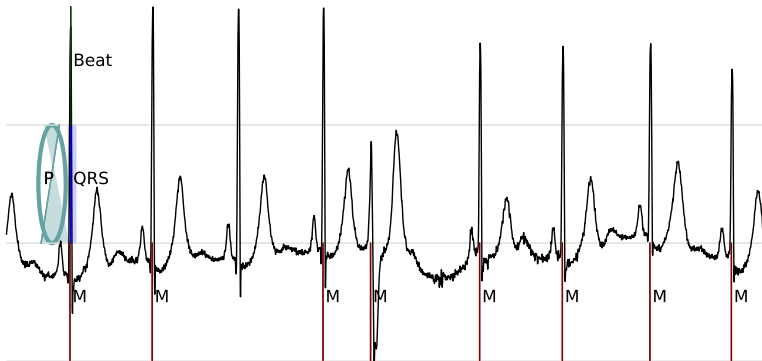
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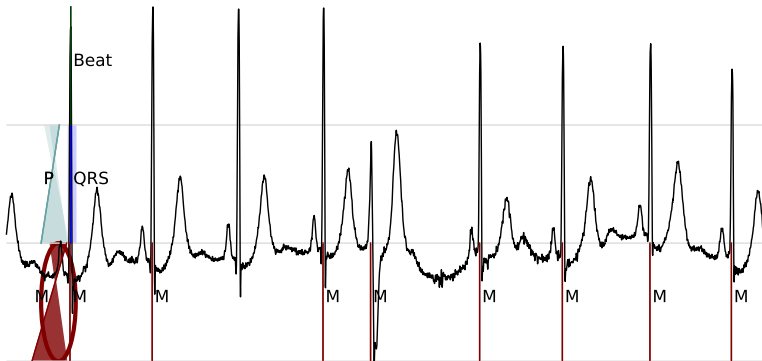
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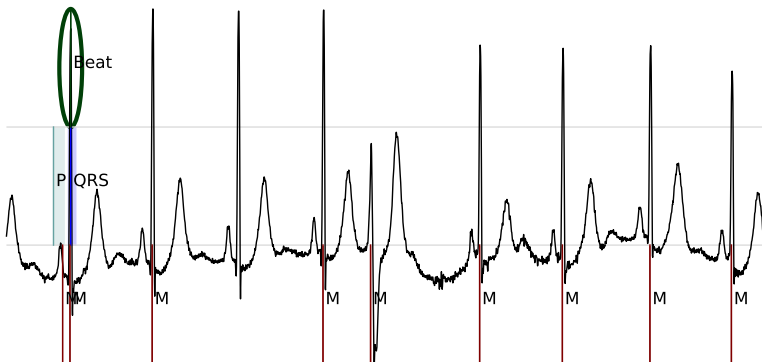
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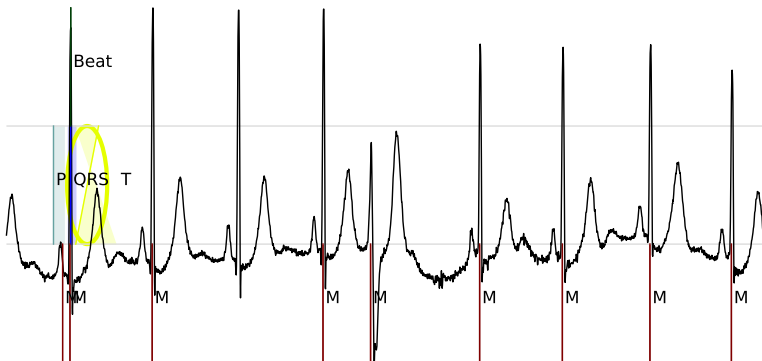
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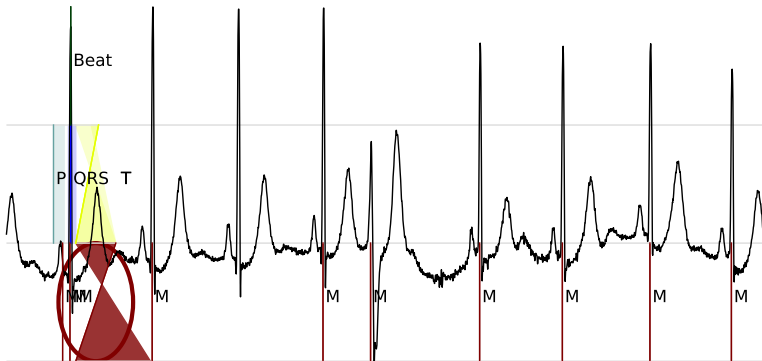
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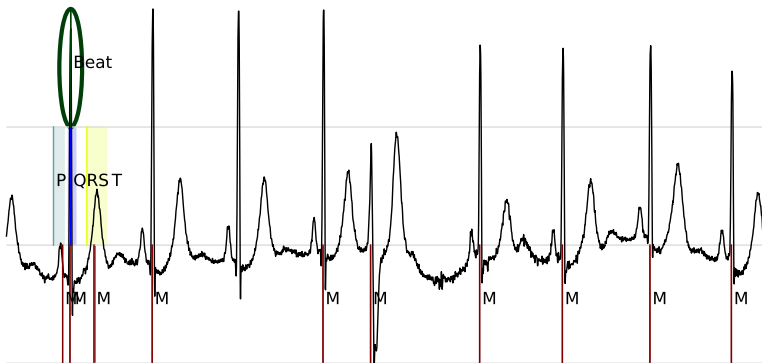
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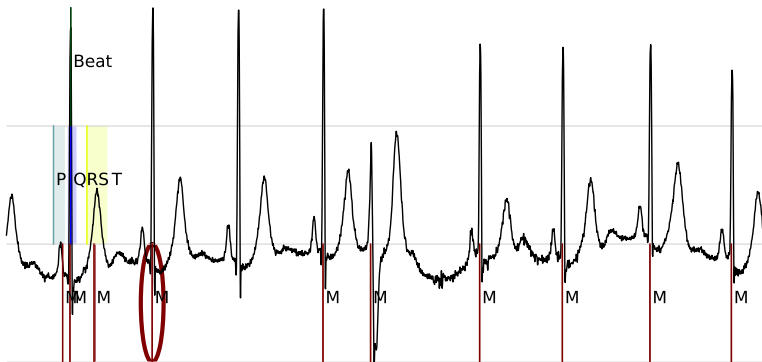
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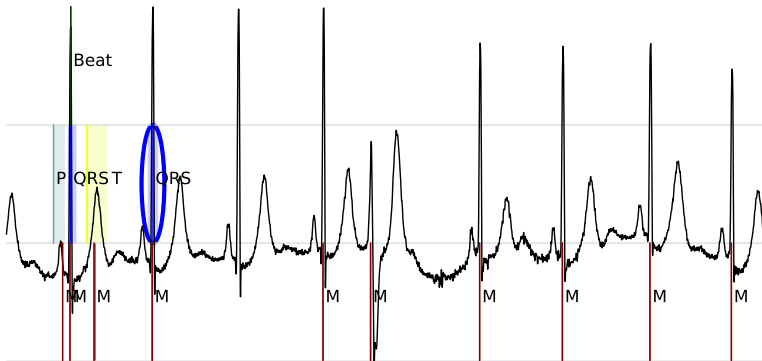
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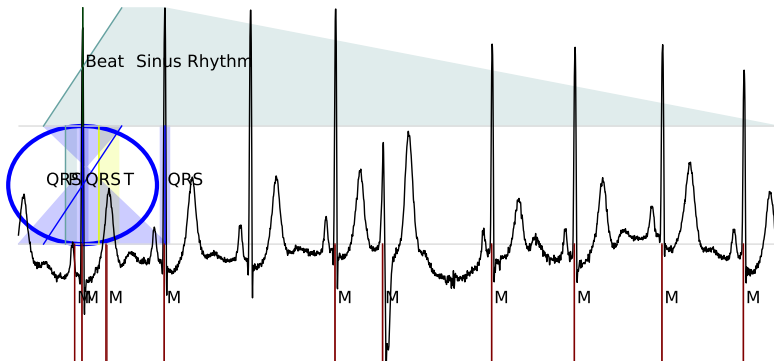
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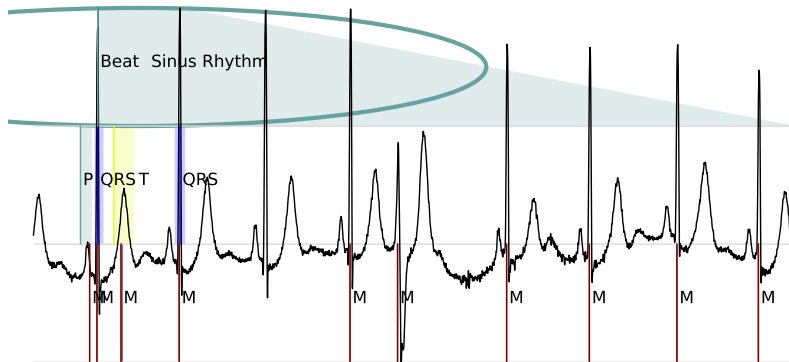
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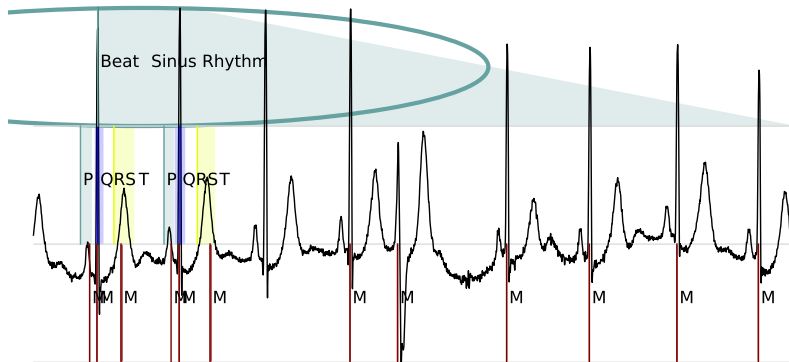
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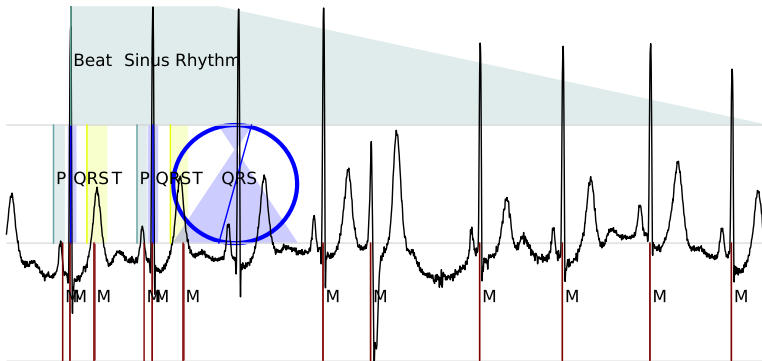
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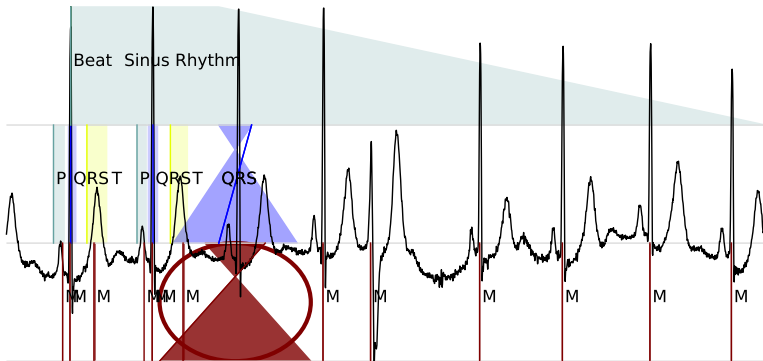
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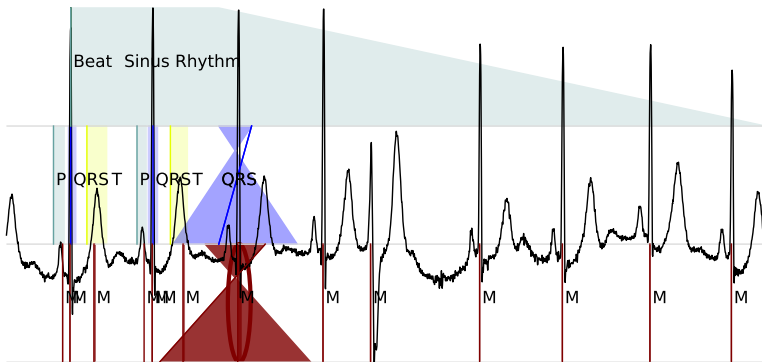
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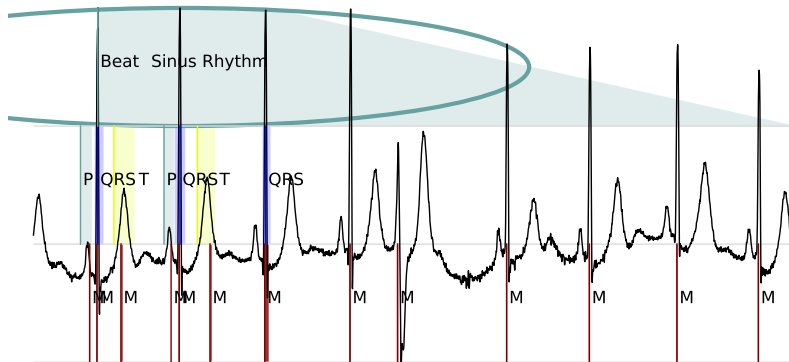
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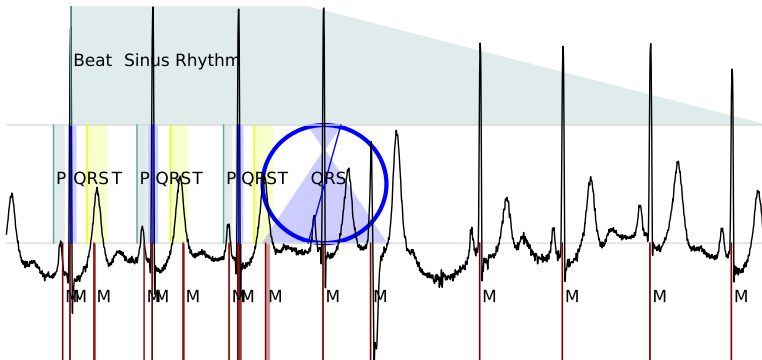


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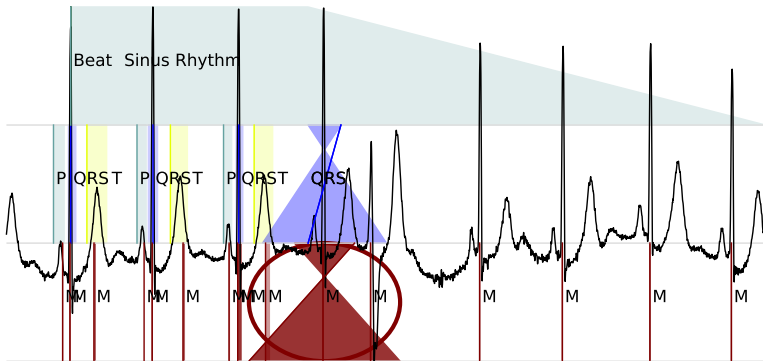


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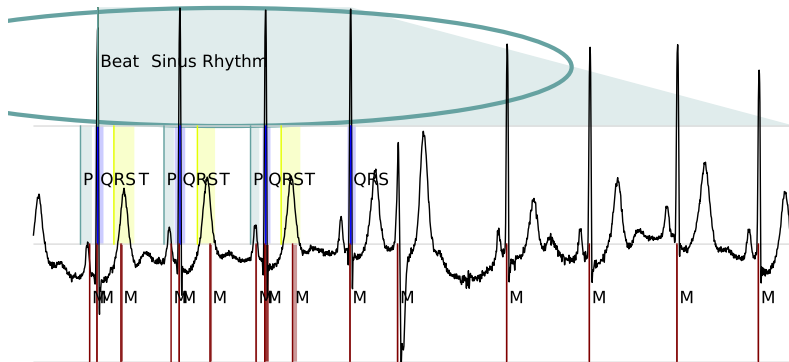




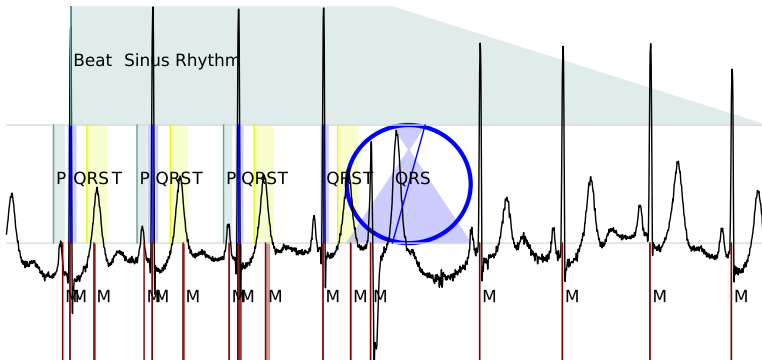
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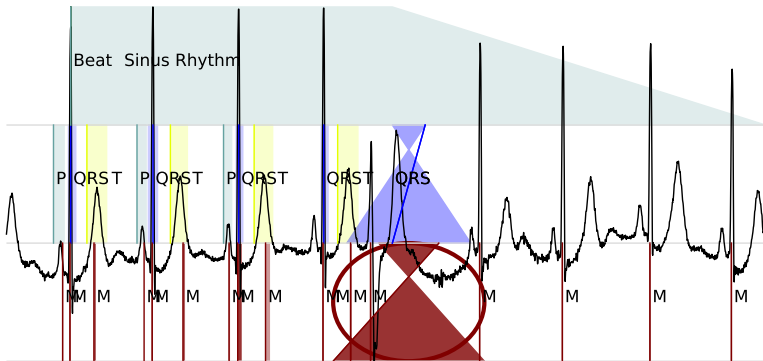
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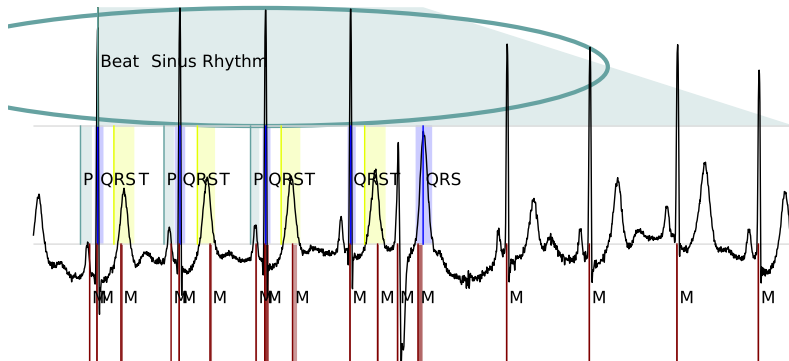
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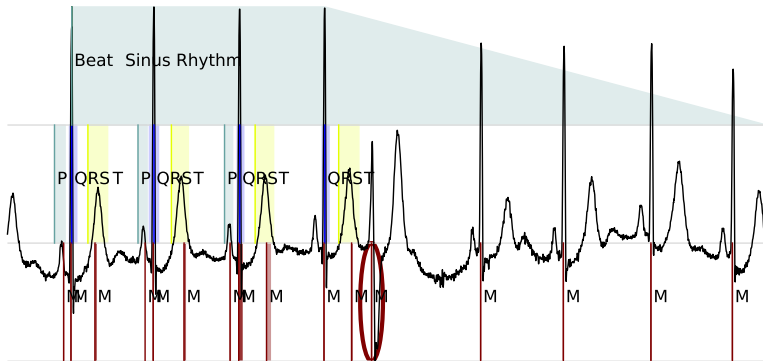
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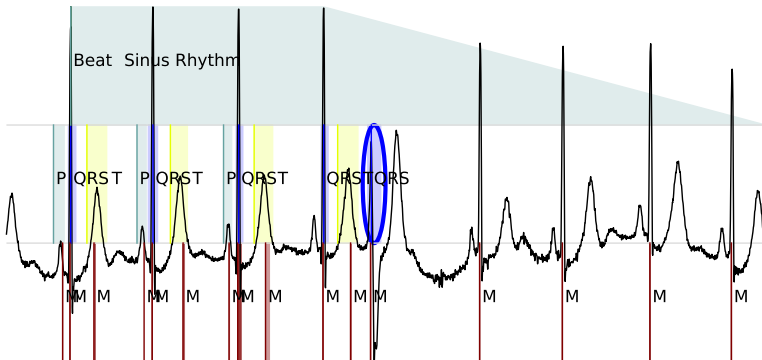
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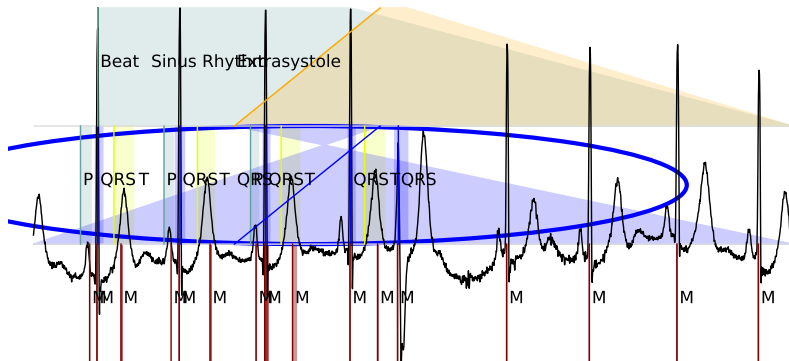
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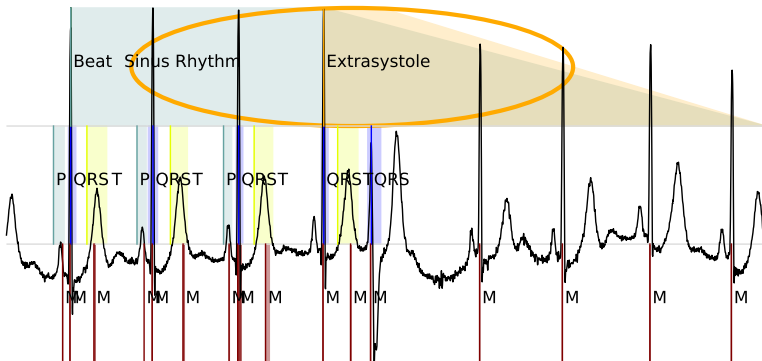
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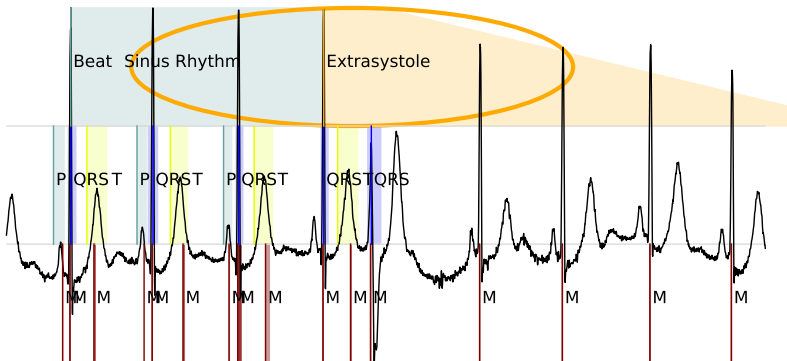
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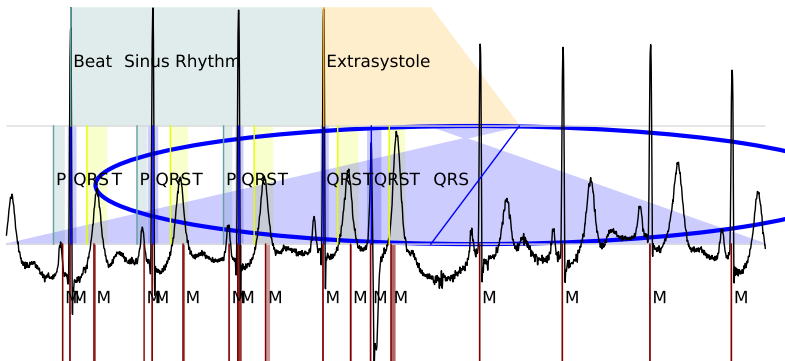
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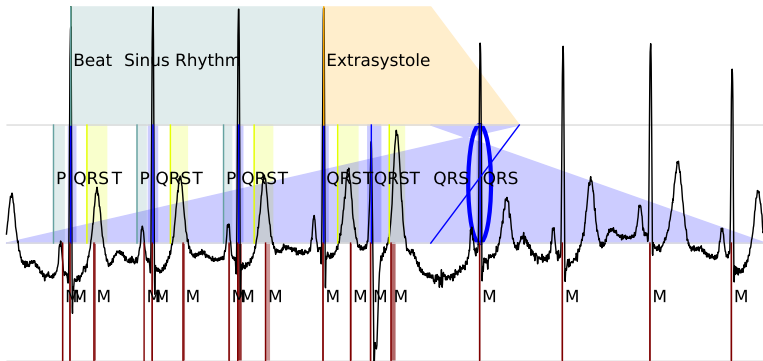
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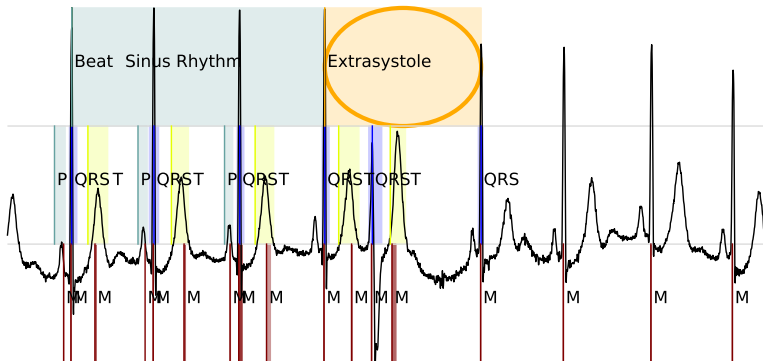
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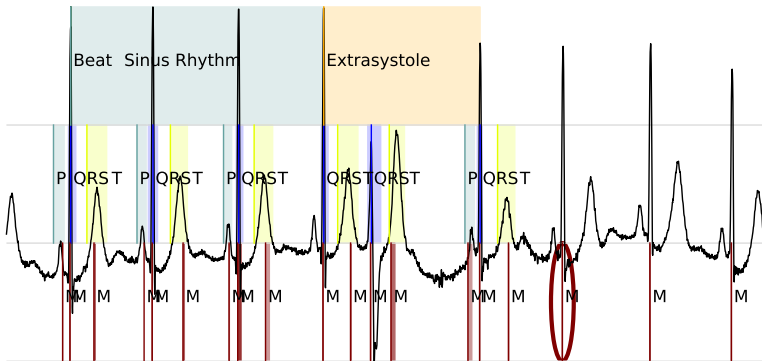


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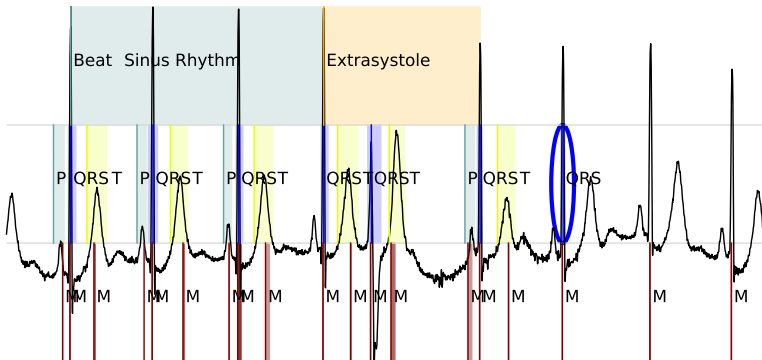


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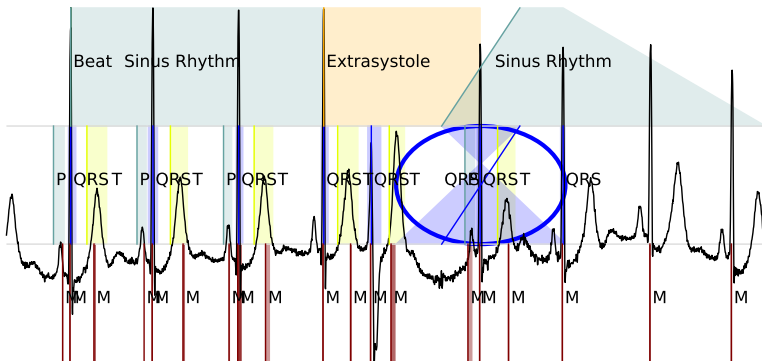


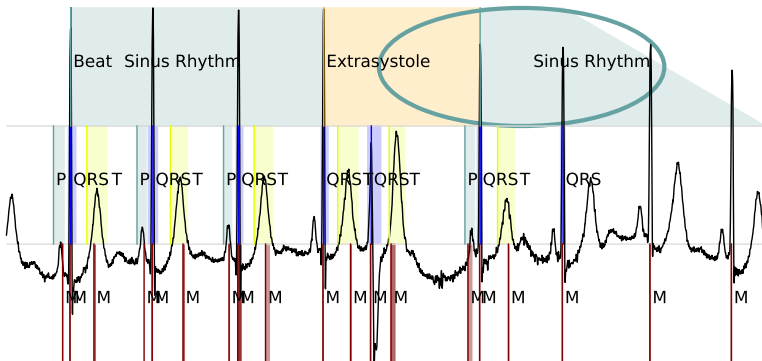


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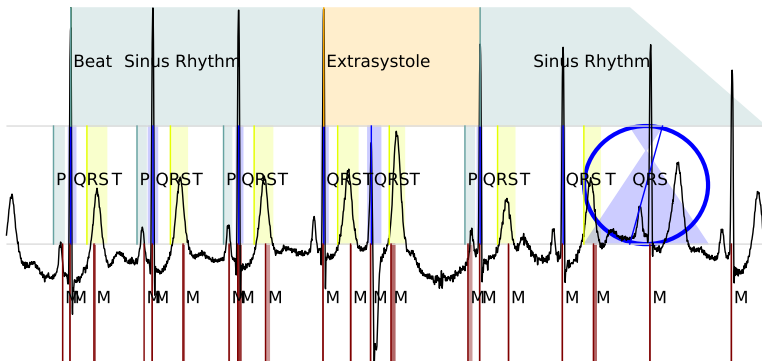


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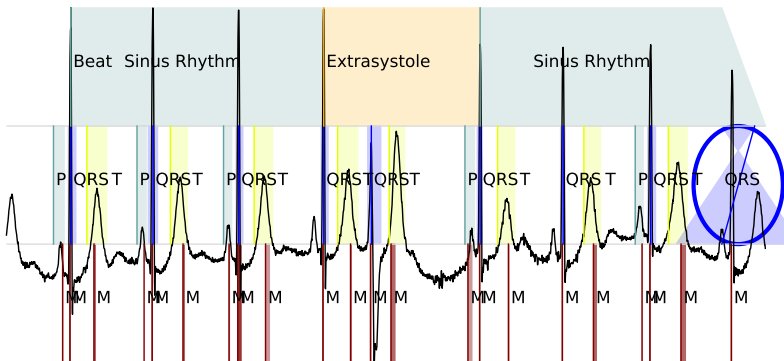




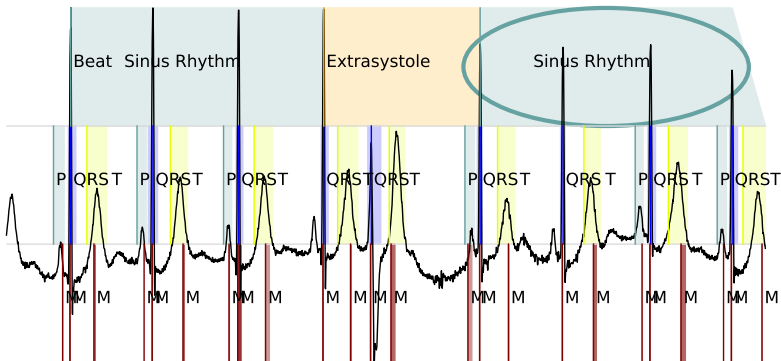
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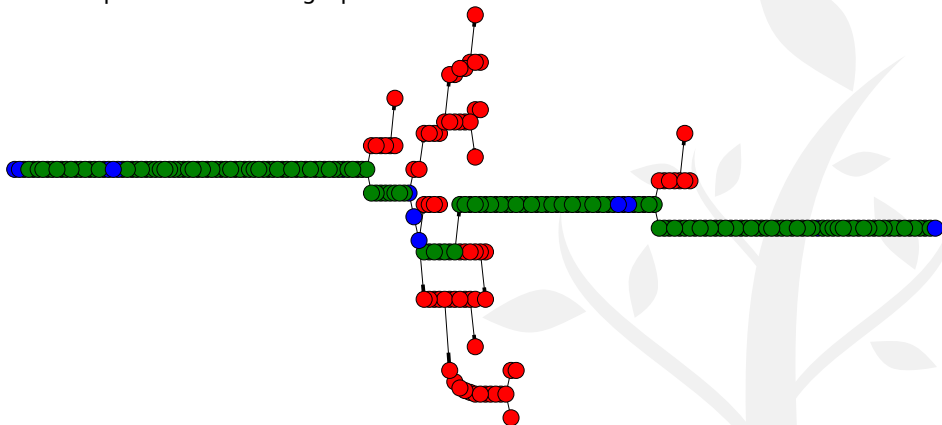


Interpretation example



Interpretation example

Interpretation search graph:



Validation results

Experiment

Improve an state of the art QRS detector by including some basic rhythm abstraction patterns:

- *Normal Rhythm*: Regular heart-rate in 60-100 bpm.
- *Tachycardia*: Regular heart-rate in 100-250 bpm.
- *Bradycardia*: Regular heart-rate in 30-60 bpm.
- *Extrasystole*: Advanced beat with a posterior compensatory pause.

Results with records from two databases, accumulating over 1 700 000 beats:

| Database | WQRS | | | WQRS + Abduction | | | P-value |
|----------------|-------|-------|-------|------------------|-------|--------------|--------------|
| | Se | P+ | F1 | Se | P+ | F1 | |
| NSR | 99.90 | 99.08 | 99.49 | 99.83 | 99.40 | 99.61 | 0.008 |
| MIT-BIH | 99.95 | 98.58 | 99.26 | 99.62 | 99.64 | 99.63 | 0.033 |

Future work

- Define a **comprehensive knowledge base** for interpreting a wider range of phenomena and that can address more complex problems, such as beat classification by origin and arrhythmia classification.
- Evaluate the approach in **multimodal records** (more than one type of signal).
- Include an **hypotheses evaluation scheme** (probability calculus, for example).

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Thank you very much for your attention!

Questions?

