

Feeling *Lucky*? Multi-armed bandits for Ordering Judgements in Pooling-based Evaluation

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Lab



ACM SAC, 2016

A scientist in a white lab coat is working in a laboratory. They are using a multi-channel pipette to transfer liquid into several white microcentrifuge tubes. The tubes are arranged in a rack and have blue caps and yellow labels. The background is slightly blurred, showing laboratory equipment and a window.

**Evaluation
is crucial**

**compare retrieval algorithms, design
new search solutions, ...**



information retrieval evaluation: 3 main ingredients

docs





information retrieval evaluation: 3 main ingredients

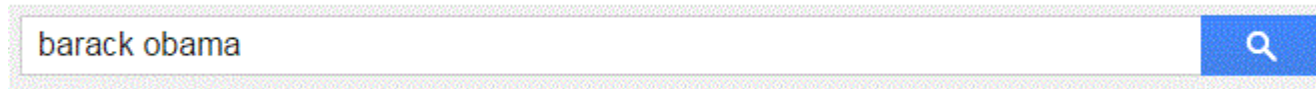
**relevance
judgements**



relevance assessments are incomplete



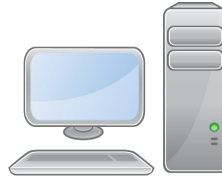
relevance assessments are incomplete



search system 1



search system 2

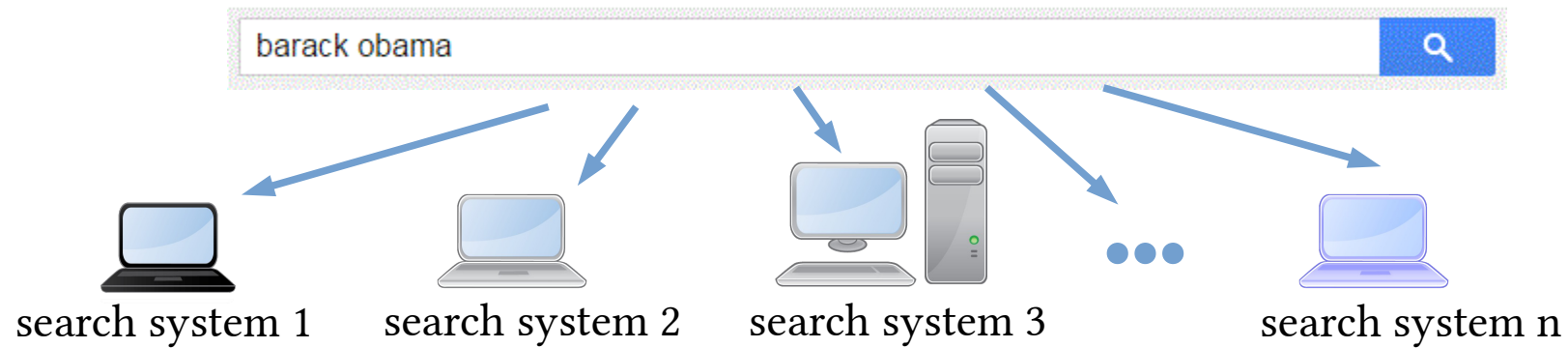


search system 3

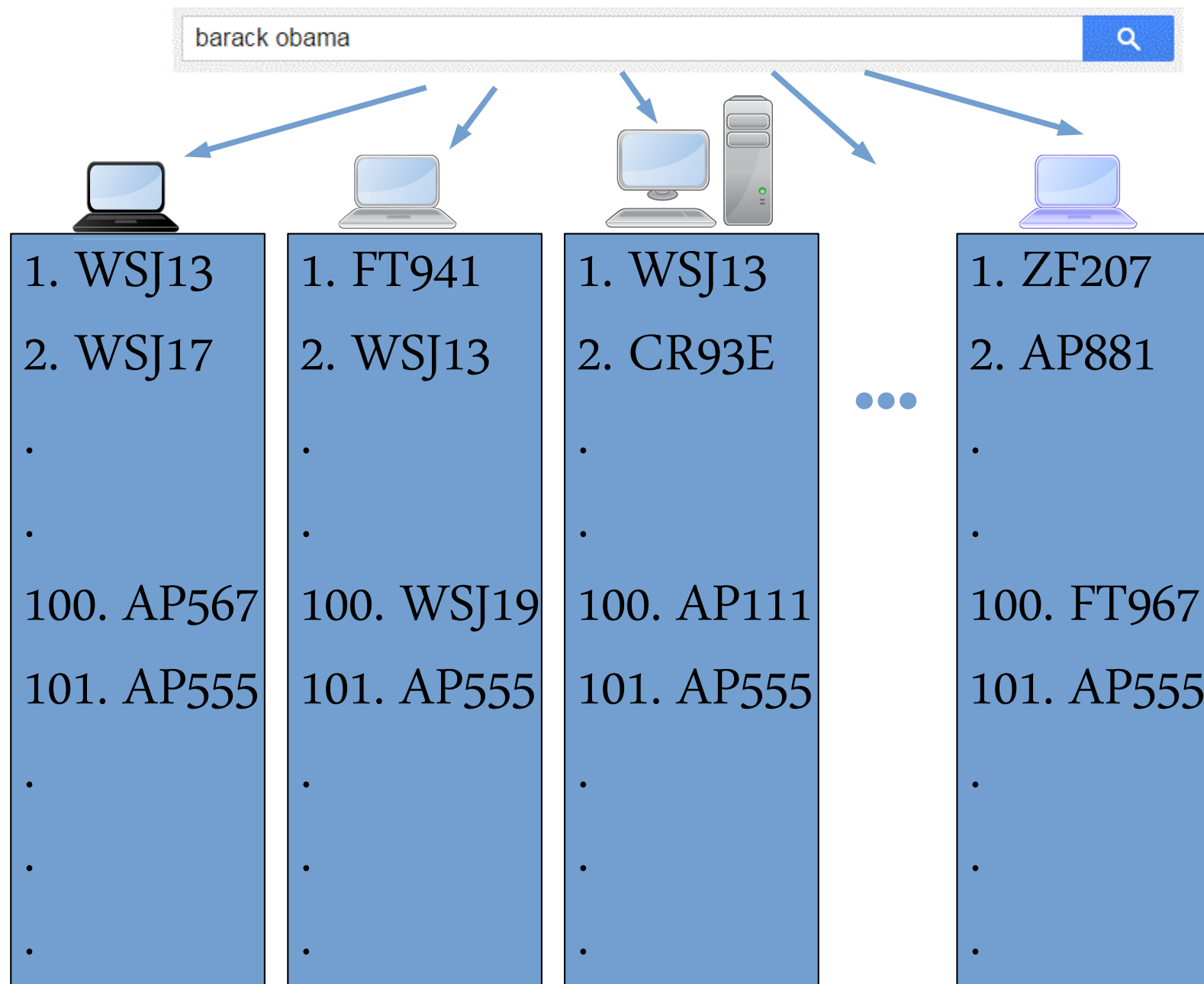


search system n

relevance assessments are incomplete

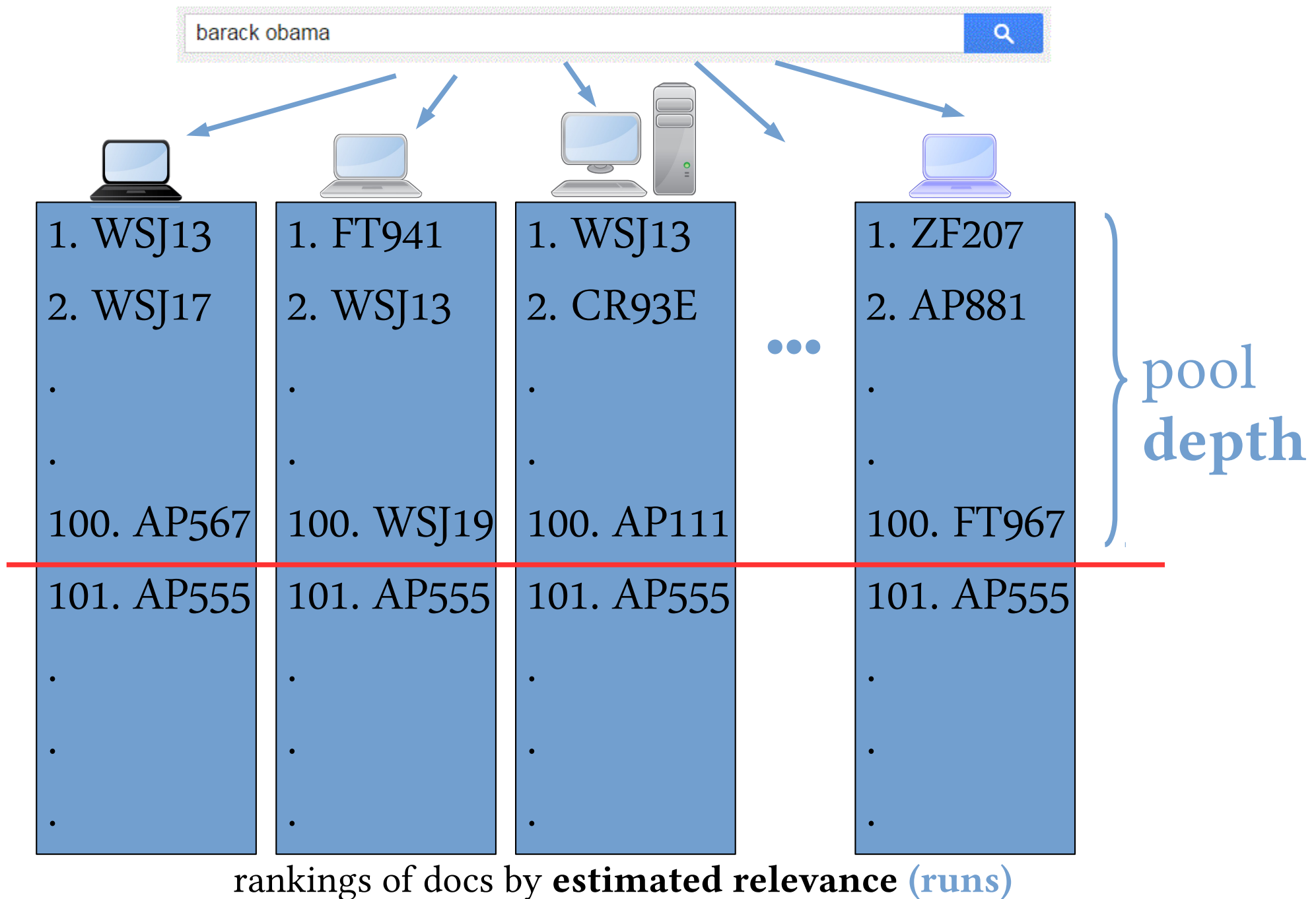


relevance assessments are incomplete

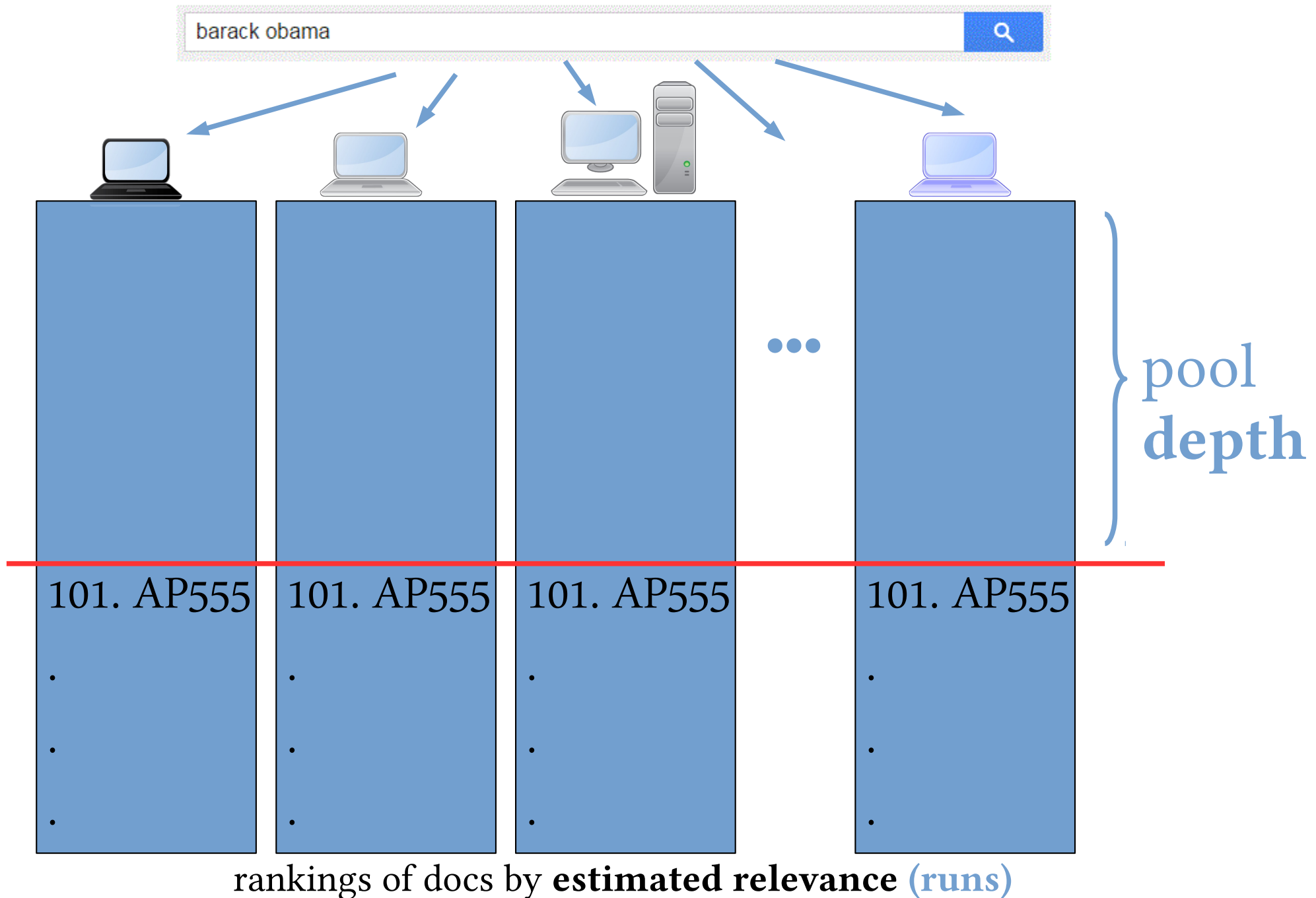


rankings of docs by **estimated relevance** (runs)

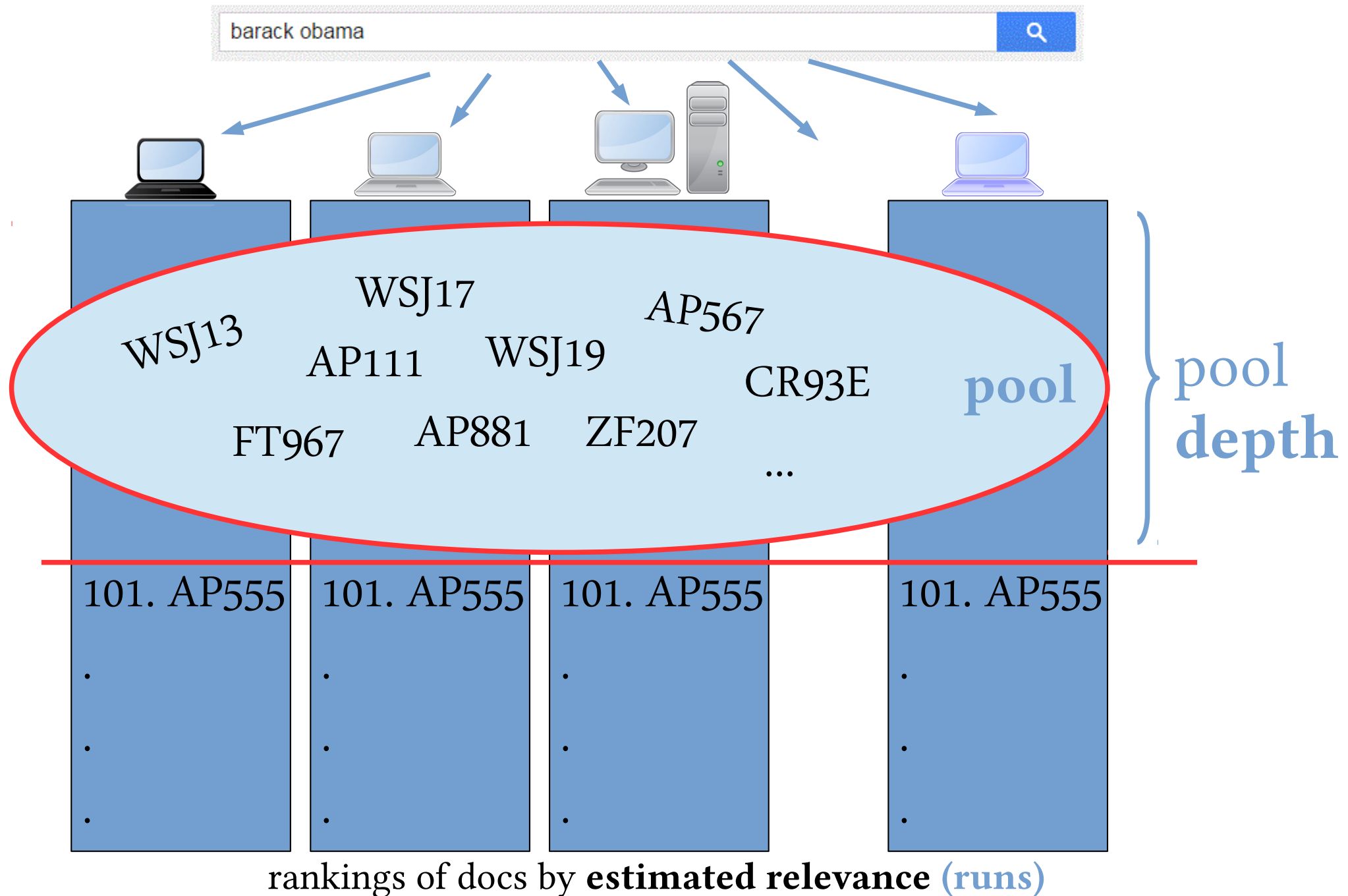
relevance assessments are incomplete



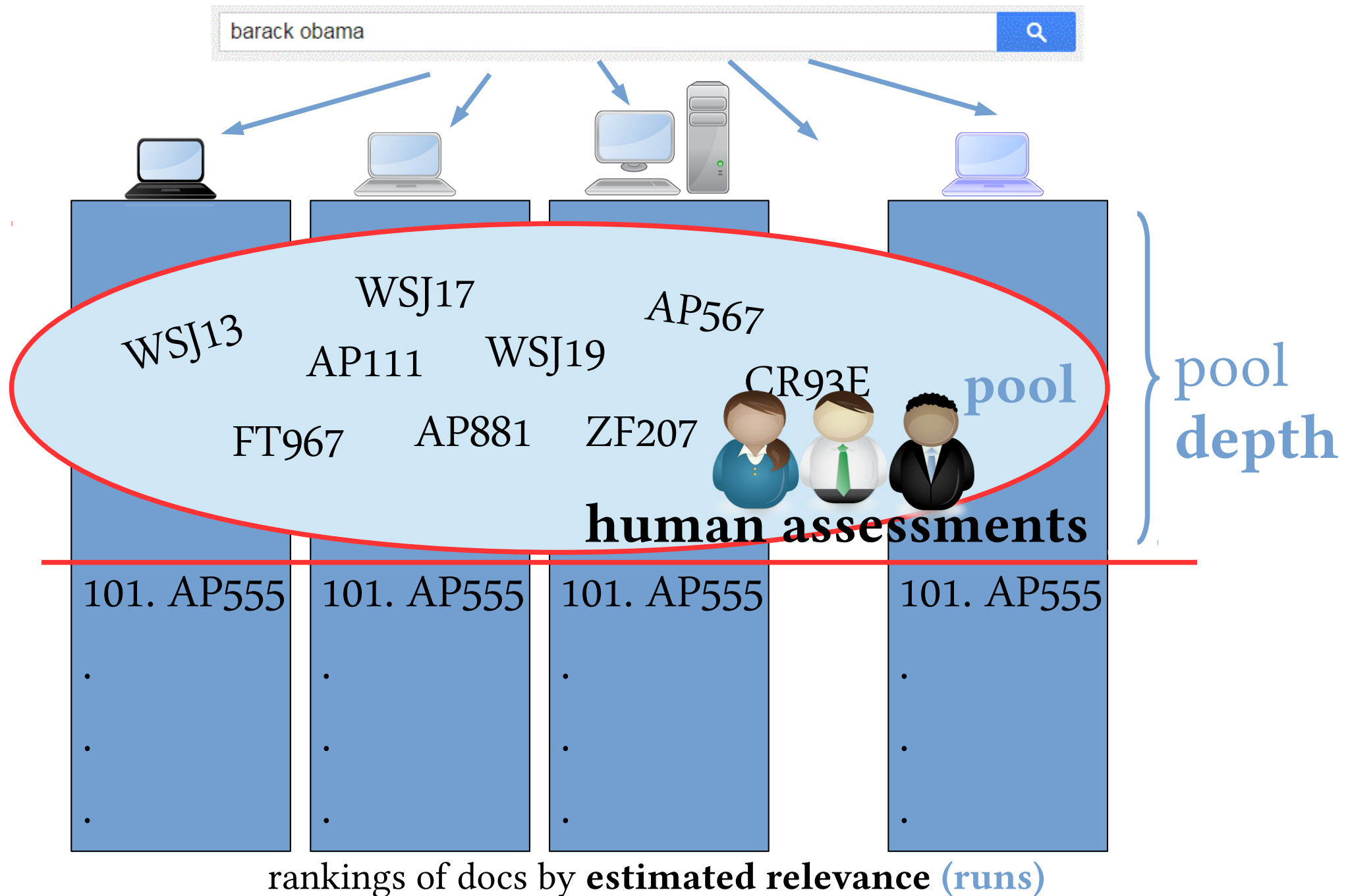
relevance assessments are incomplete



relevance assessments are incomplete



relevance assessments are incomplete





finding relevant docs is the key

Most productive use of assessors' time
is spent on judging relevant docs
(Sanderson & Zobel, 2005)

Effective adjudication methods

Give priority to **pooled docs** that are **potentially relevant**

Can **significantly reduce** the num. of **judgements** required to identify a given num. of relevant docs

But most existing methods are **adhoc...**

A photograph of a gorilla sitting on a wooden structure, possibly a platform or a piece of furniture, in front of a large window. The gorilla is looking out the window, which shows some greenery outside. The text is overlaid on the image.

Our main idea...

Cast **doc adjudication** as a **reinforcement learning** problem

Doc judging is an **iterative** process where we learn as judgements come in

Doc adjudication as a reinforcement learning problem

Initially we **know nothing** about the quality of the runs

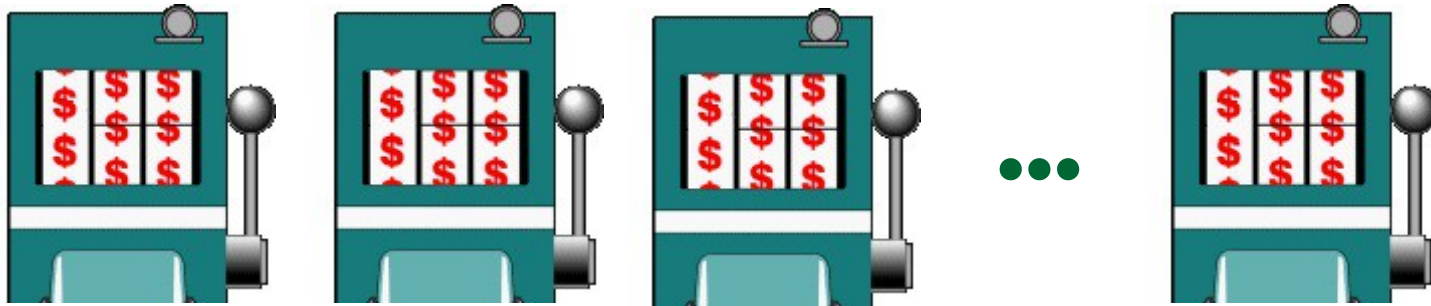


As judgements
come in...



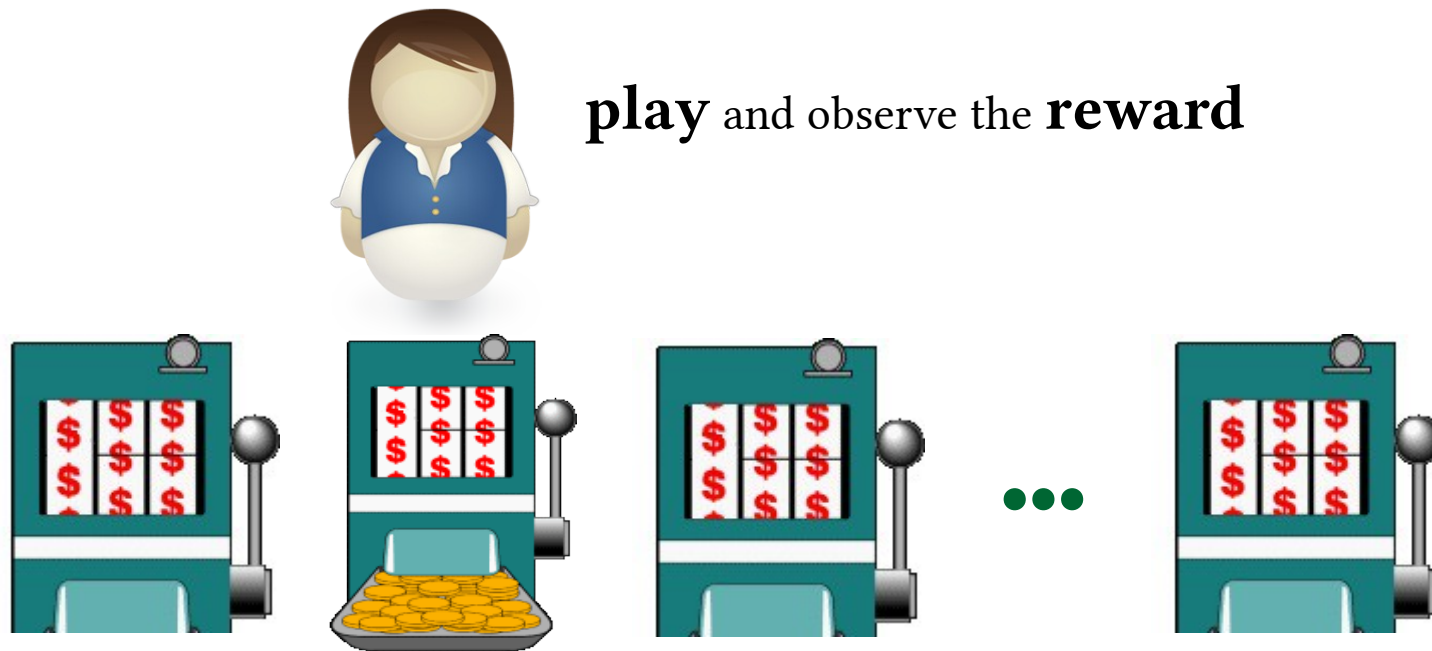
And we can **adapt** and allocate more docs for judgement from the most promising runs

Multi-armed bandits



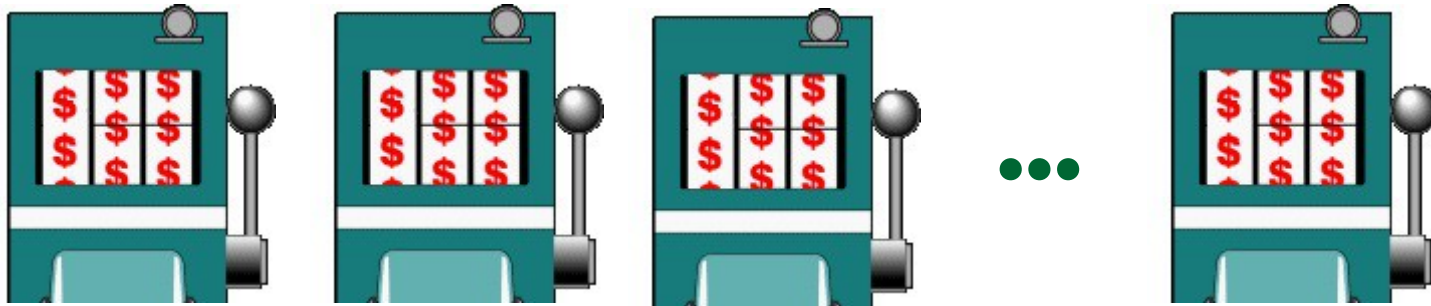
unknown probabilities of giving a prize

Multi-armed bandits



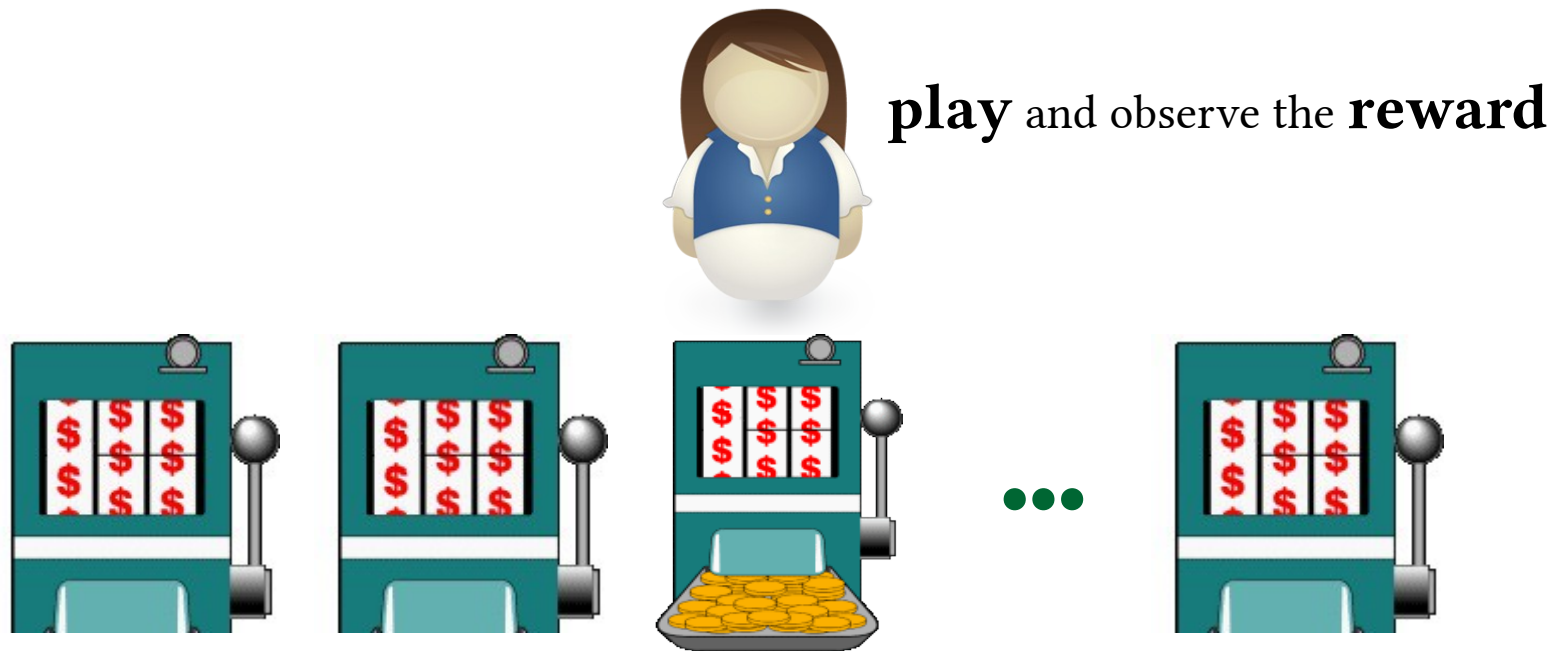
unknown probabilities of giving a prize

Multi-armed bandits



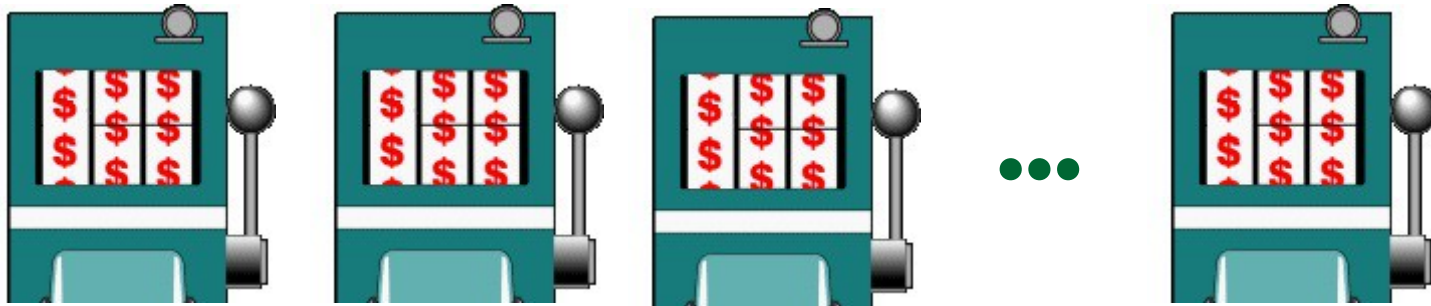
unknown probabilities of giving a prize

Multi-armed bandits



unknown probabilities of giving a prize

Multi-armed bandits

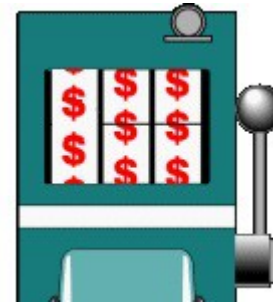
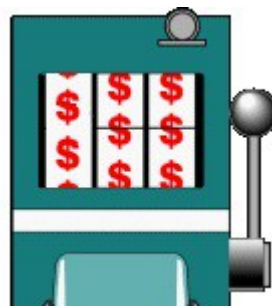
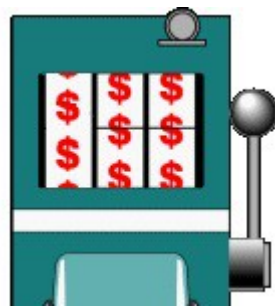


unknown probabilities of giving a prize

Multi-armed bandits

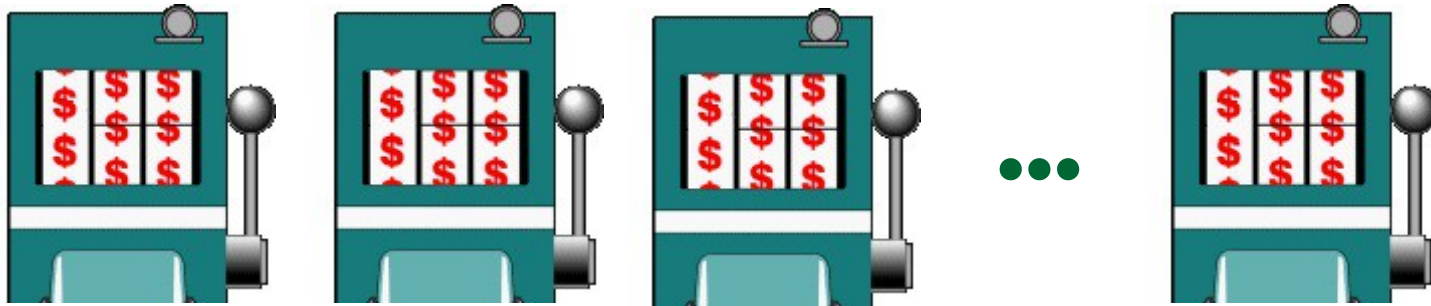


play and observe the **reward**



unknown probabilities of giving a prize

Multi-armed bandits



unknown probabilities of giving a prize

exploration

vs

exploitation



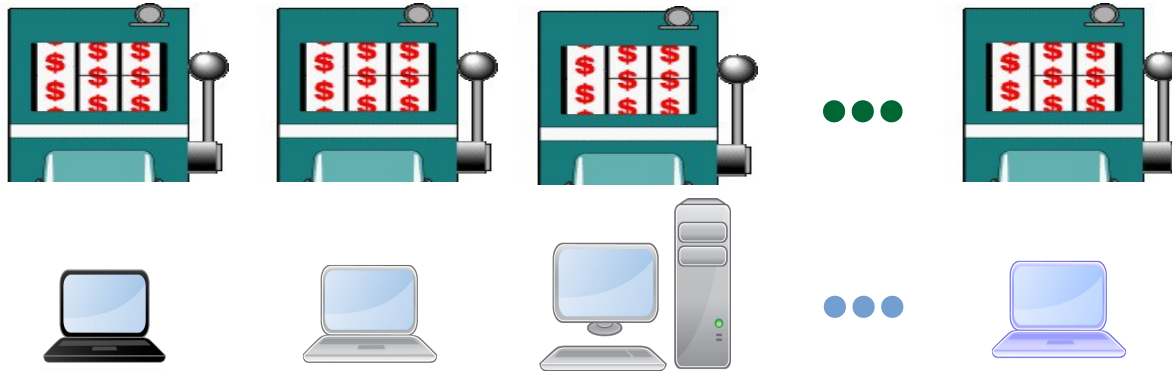
explores **uncertain** actions
gets **more info** about expected payoffs
may produce greater total reward
in the long run

exploits **current knowledge**
spends no time sampling inferior actions
maximizes expected reward
on the **next** action

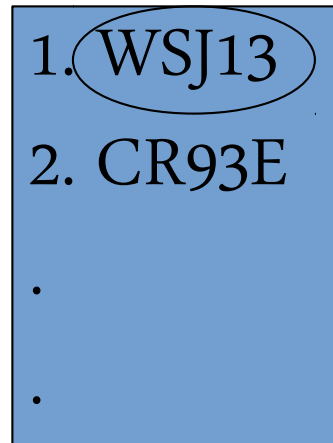
allocation methods: choose next action (play) based on past plays and obtained rewards
implement different ways to **trade** between exploration and exploitation

Multi-armed bandits for ordering judgements

machines = runs



play a machine = select a run and get the next (unjudged) doc



(binary) reward = relevance/non-relevance of the selected doc

Allocation methods tested

random

Upper Confidence Bound (UCB)

computes upper confidence bounds for avg rewards

conf. intervals get **narrower** with the number of plays

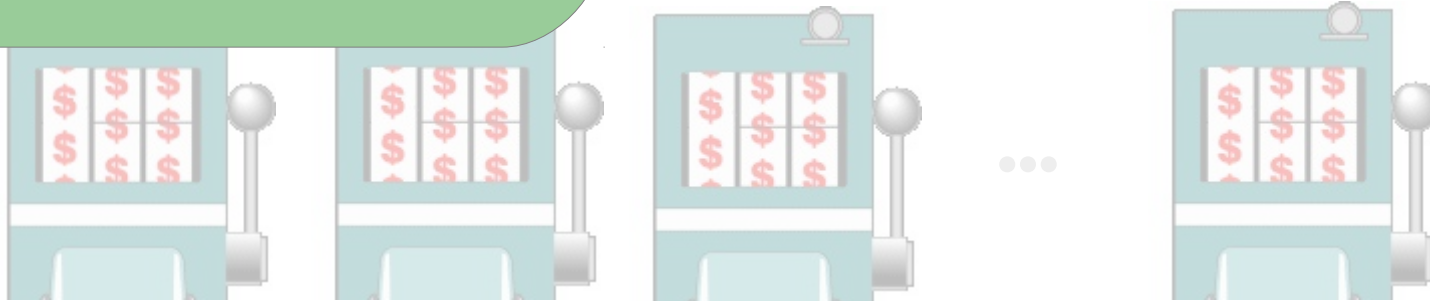
selects the machine with the **highest optimistic estimate**

ϵ_n -greedy

with **prob** $1-\epsilon$ plays the machine with the highest avg reward

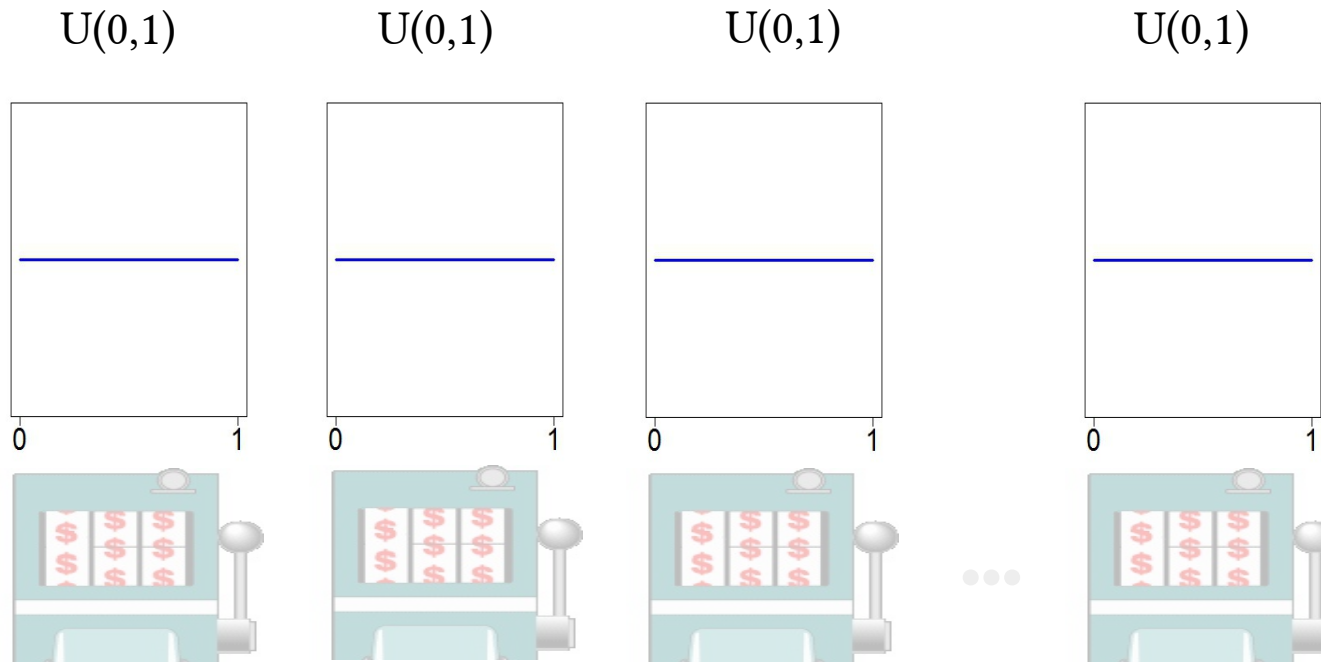
with **prob** ϵ plays a random machine

prob of exploration (ϵ) decreases with the num. of plays



Allocation methods tested: **Bayesian** bandits

prior probabilities of giving a relevant doc: **Uniform(0,1)** (or, equivalently, $\text{Beta}(\alpha, \beta)$, $\alpha, \beta=1$)

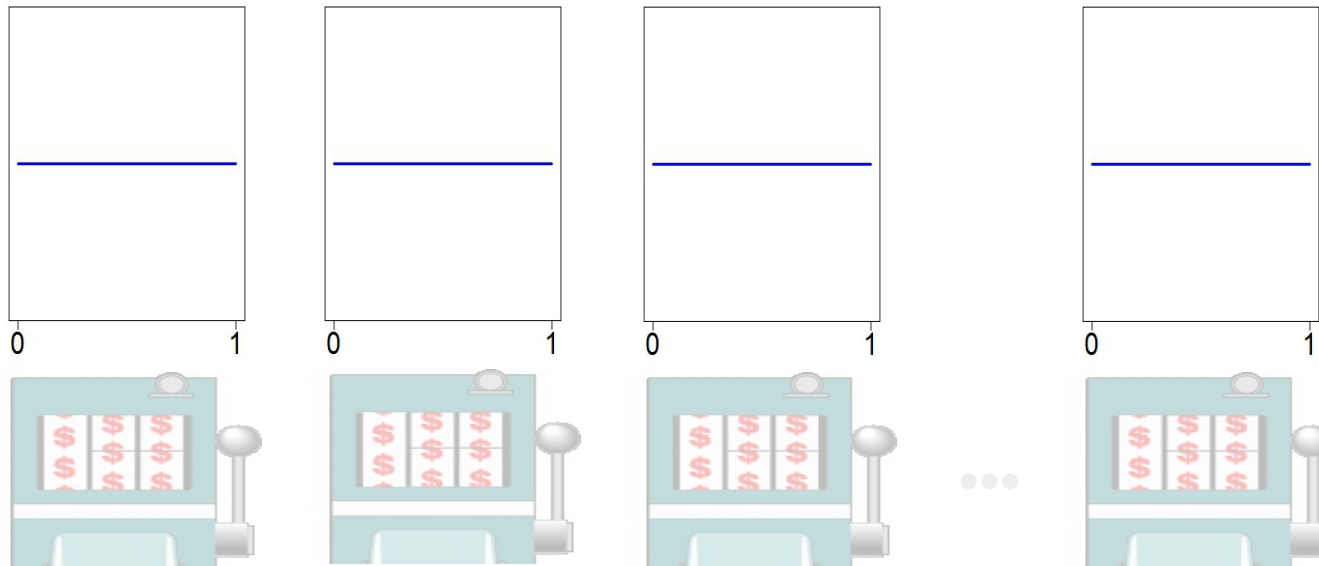


evidence ($O \in \{0,1\}$) is Bernoulli (or, equivalently, $\text{Binomial}(1,p)$)

posterior probabilities of giving a relevant doc: $\text{Beta}(\alpha+O, \beta+1-O)$ (Beta: conjugate prior for Binomial)

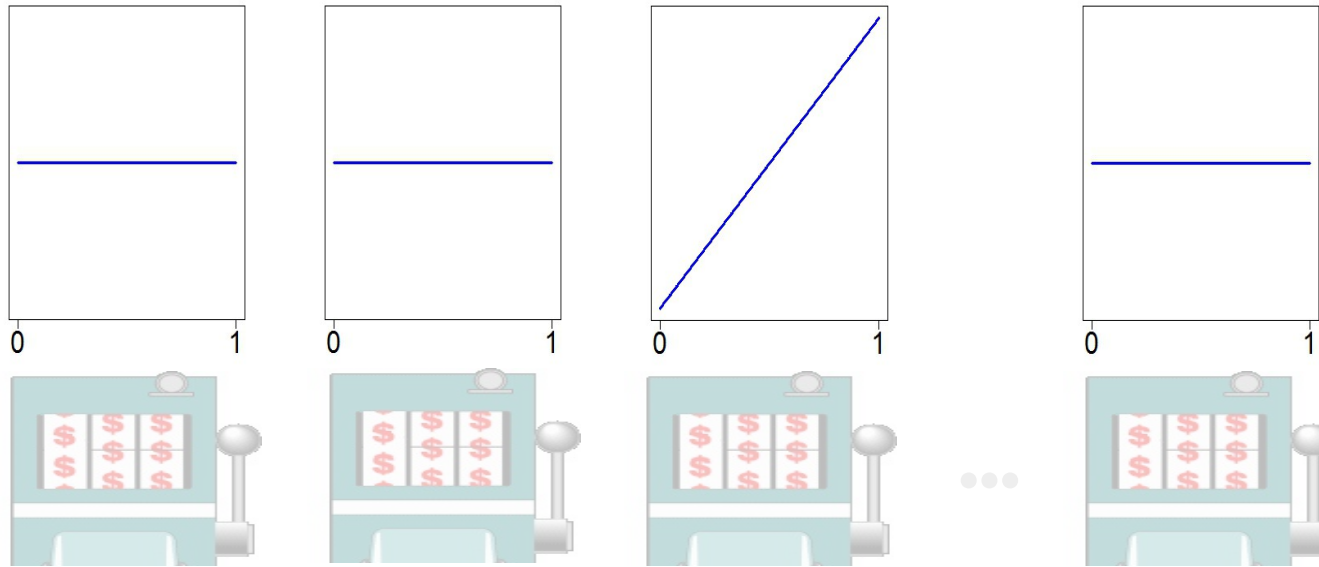
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



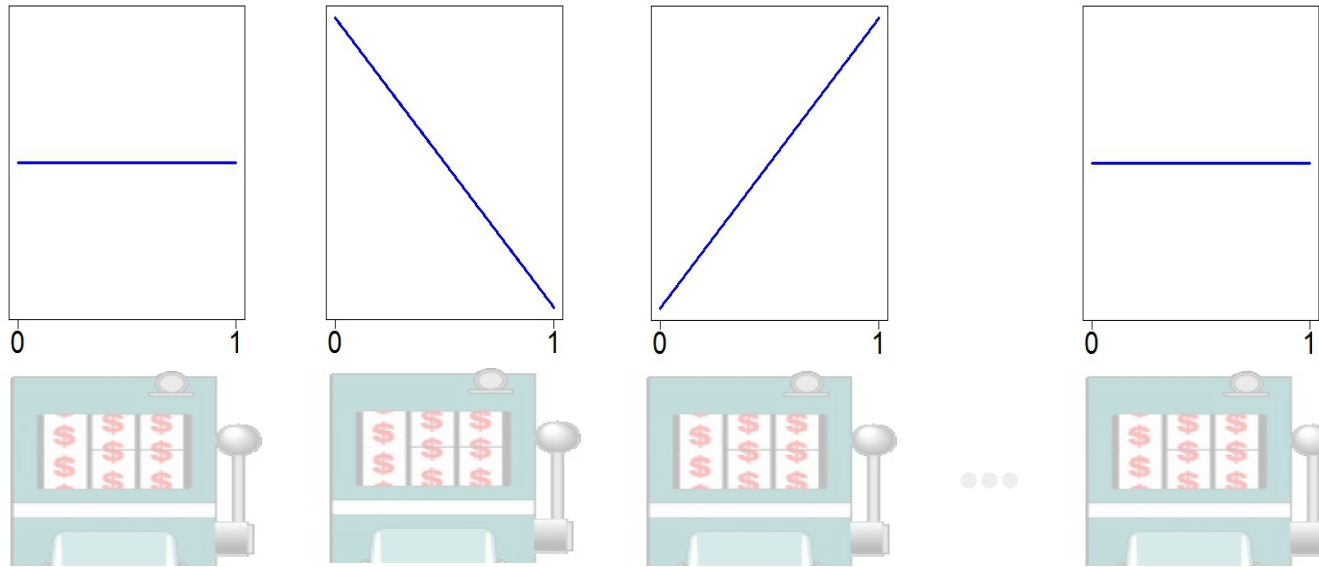
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



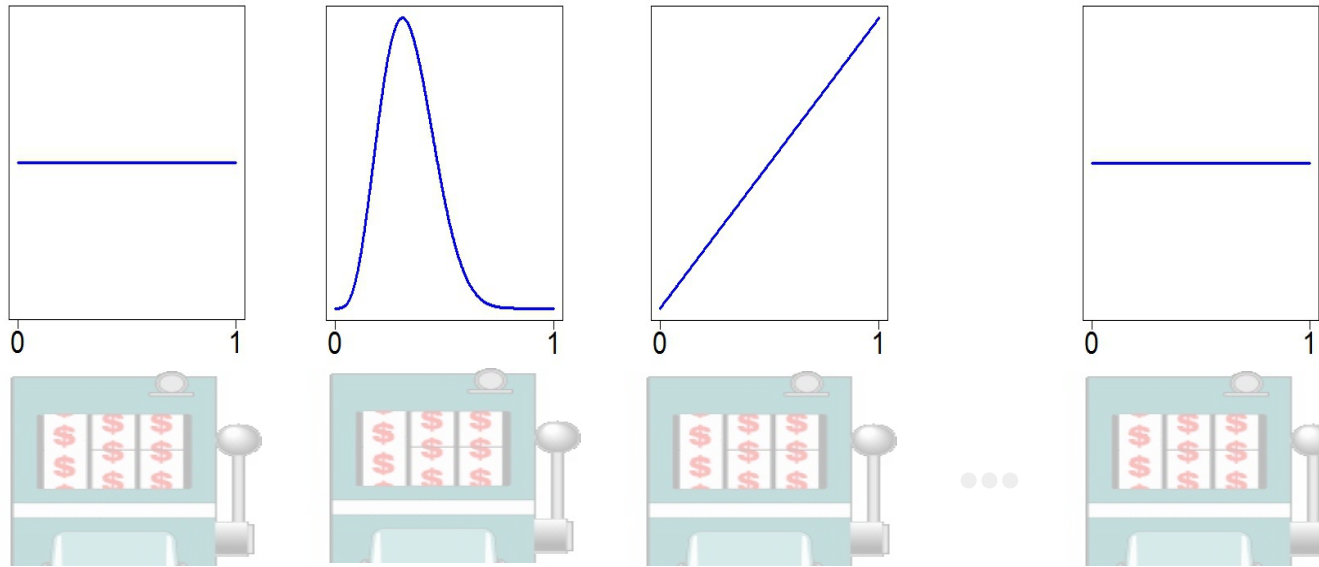
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



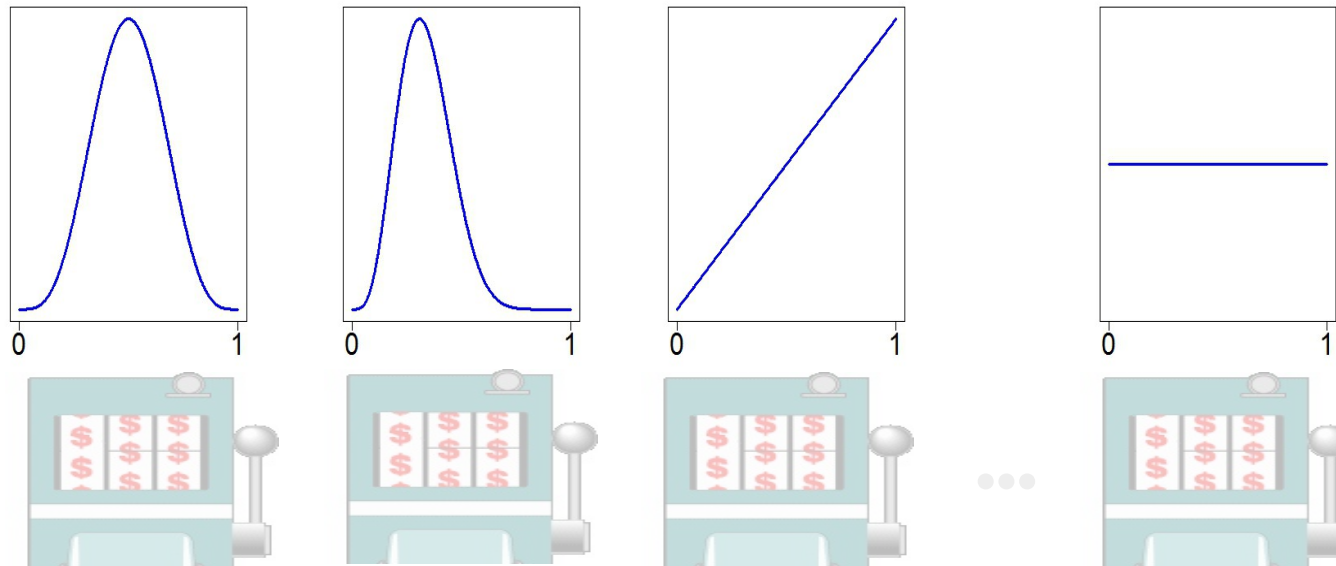
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



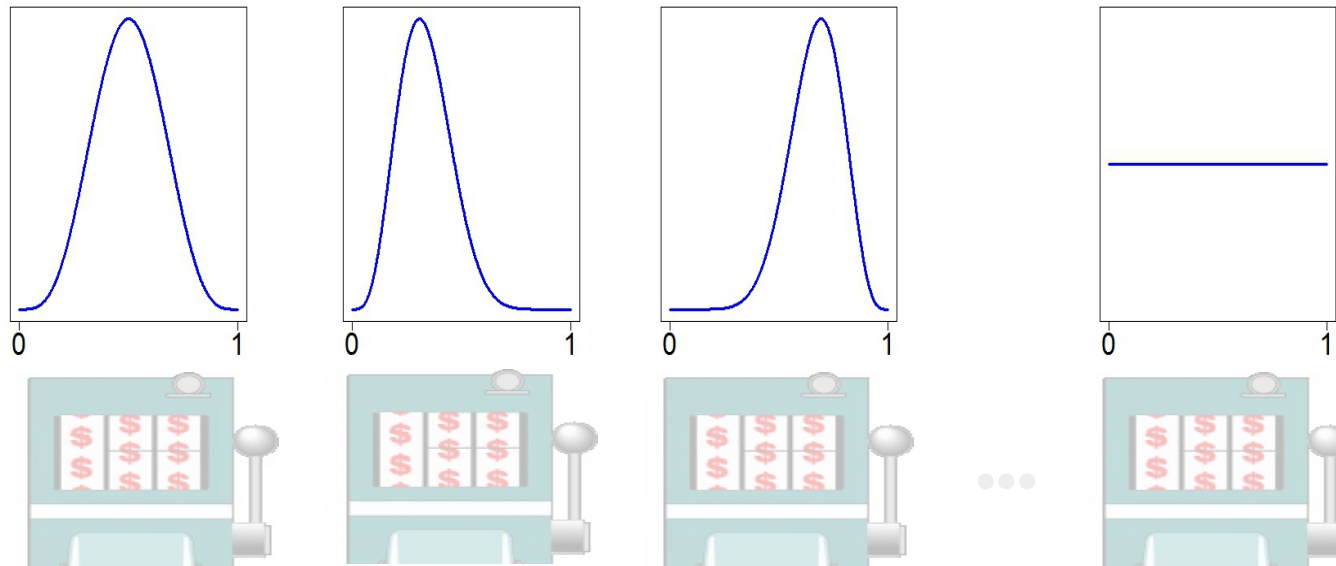
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



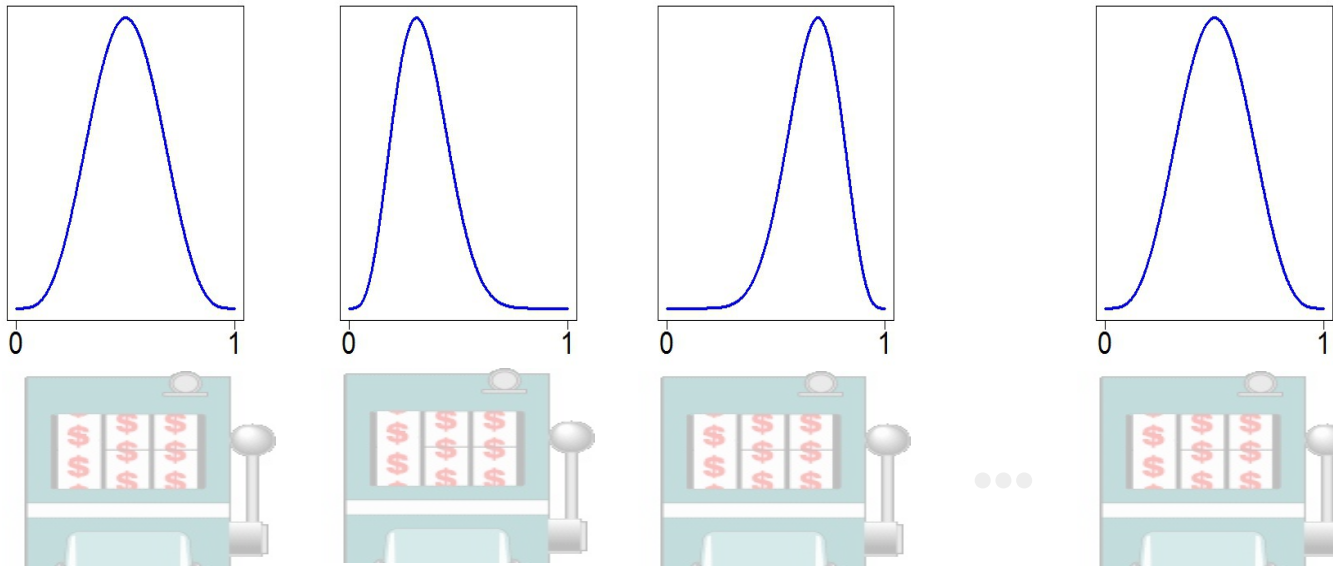
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



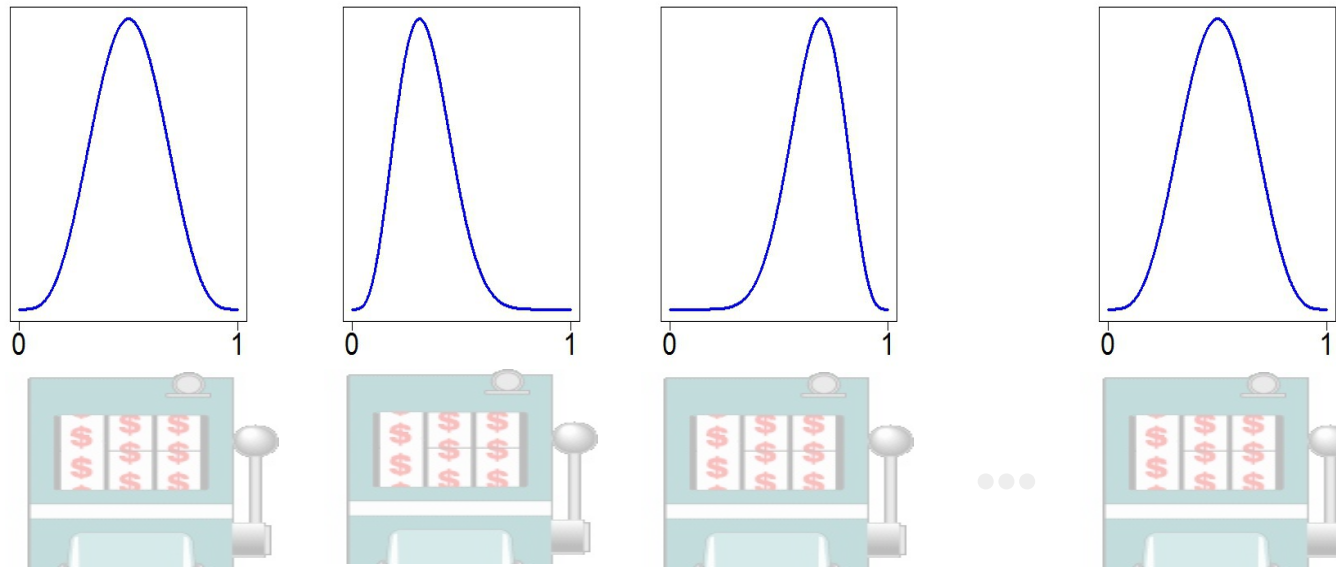
Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



Allocation methods tested: **Bayesian** bandits

we **iteratively update** our estimations using Bayes:



two strategies to select the **next machine**:

Bayesian Learning Automaton (BLA): draws a **sample from each** the posterior distribution and selects the machine yielding the **highest** sample

MaxMean (MM): selects the machine with the **highest** expectation of the posterior distribution

experiments

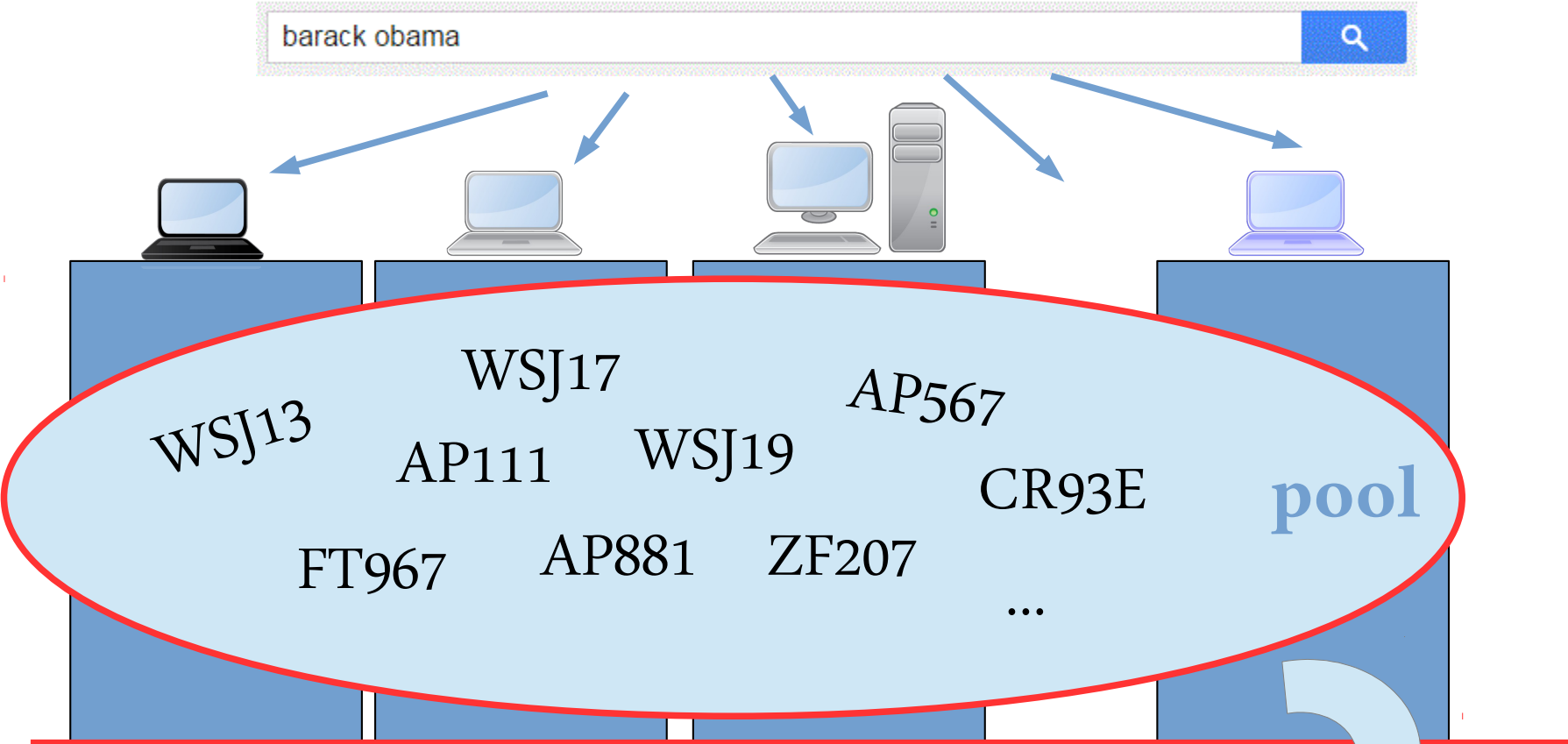
test different document adjudication strategies in terms of **how quickly** they find the **relevant docs** in the pool

rel docs found at diff. number of judgements performed

experiments: data

	<i>TREC5</i>	<i>TREC6</i>	<i>TREC7</i>	<i>TREC8</i>
# queries	50	50	50	50
# automatic runs	77	31	77	71
# manual runs	24	15	7	0
# assessed docs	133681	72270	80345	86830
avg. # docs judged per query	2673.6	1445.4	1606.9	1736.6
% of rel docs in the pool	4.1%	6.4%	5.8%	5.4%
avg. # rels per query	110.48	92.22	93.48	94.56

experiments: baselines

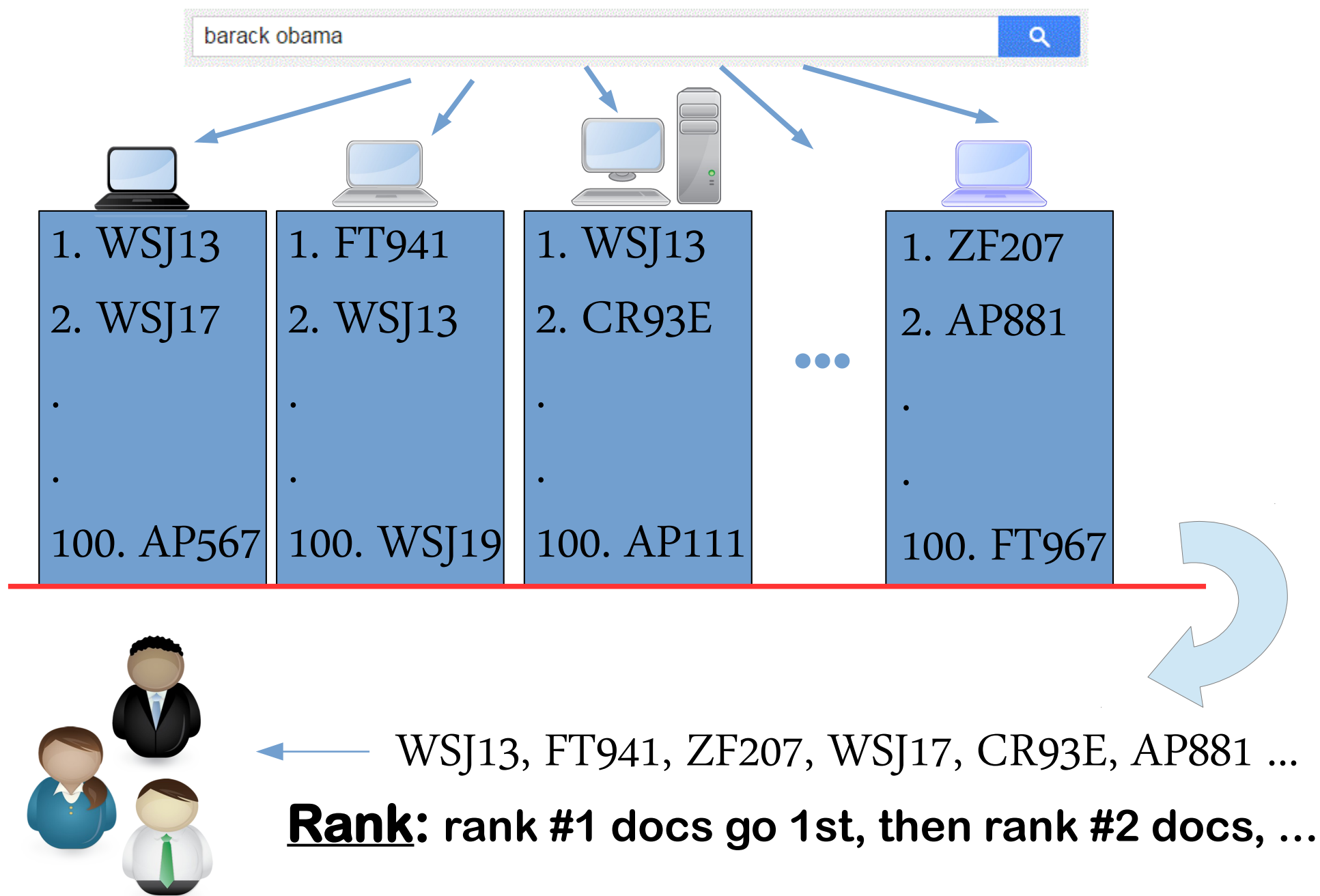


DocId: sorts by Doc Id



← AP111, AP881, AP567, CR93E, FT967, WSJ13, ...

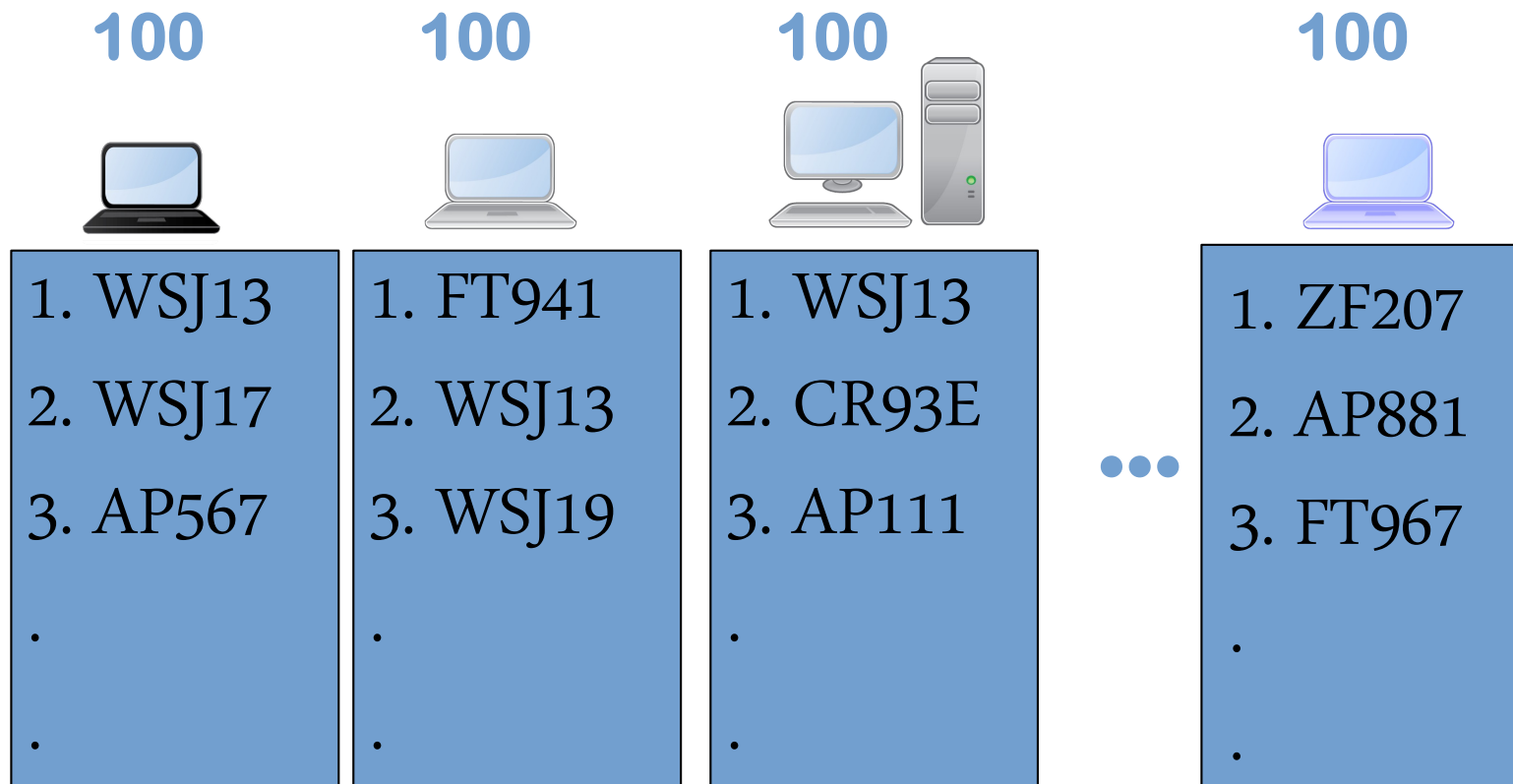
experiments: baselines



experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

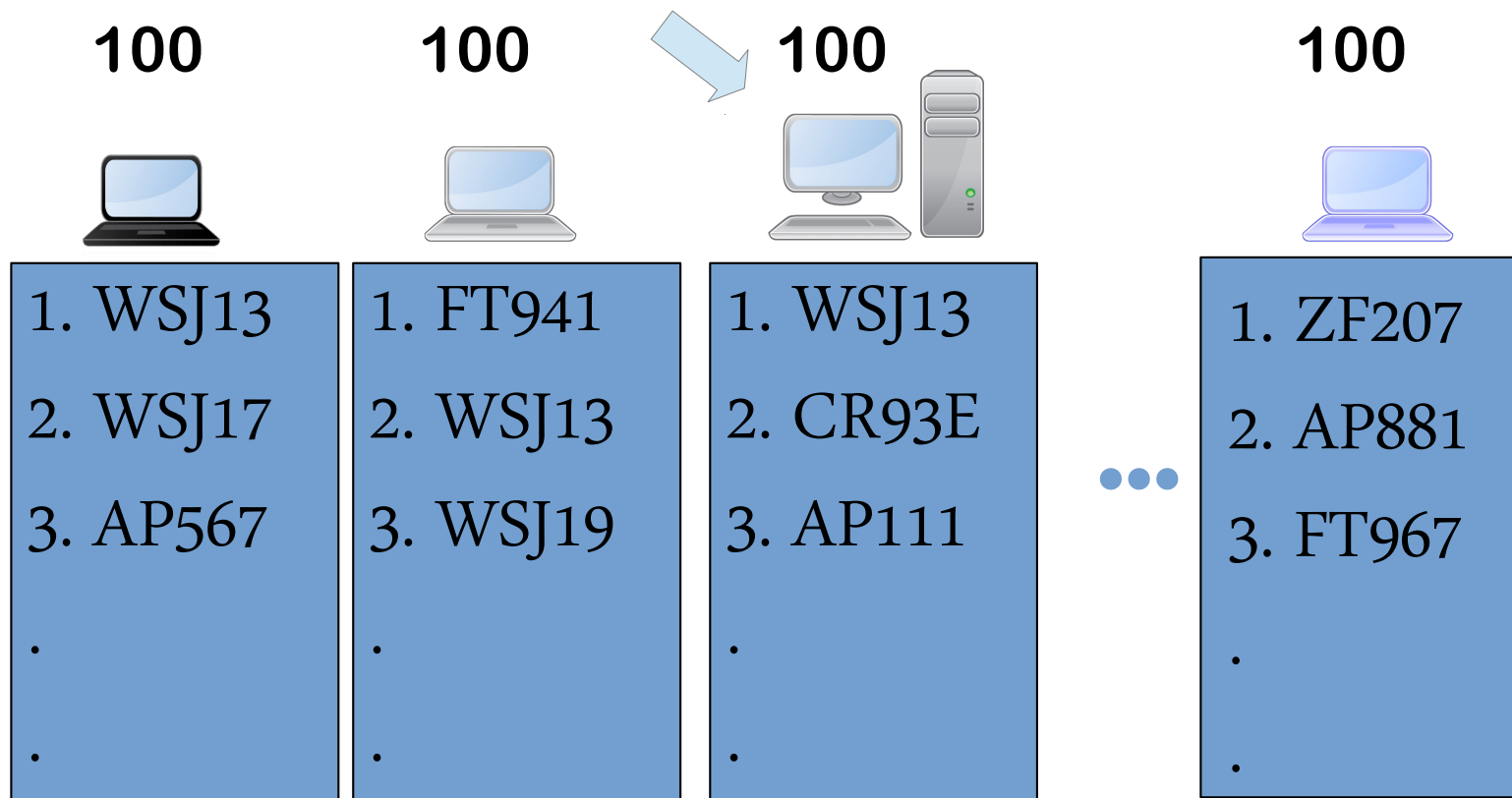
starts with **uniform priorities** for all runs (e.g. max priority=100)
selects a random run (from those with max priority)



experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

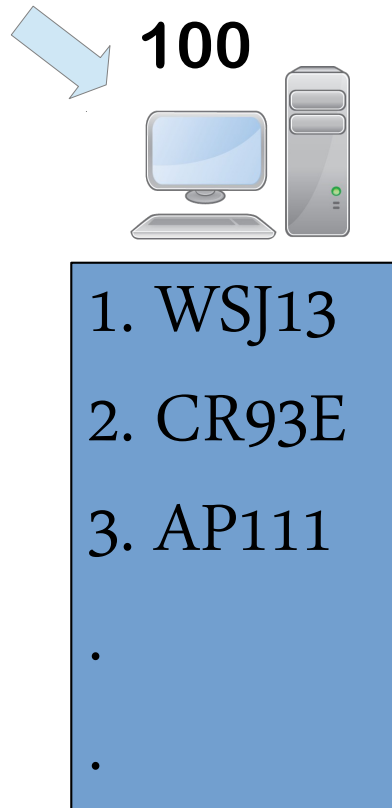
starts with uniform priorities for all runs (e.g. max priority=100)
selects a **random** run (from those with max priority)



experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

extracts & judges docs from the selected run
stays in the run until a non-rel doc is found



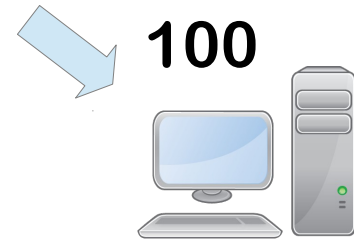
experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

extracts & judges docs from the selected run
stays in the run until a non-rel doc is found



WSJ13



1. ~~WSJ13~~
2. CR93E
3. AP111

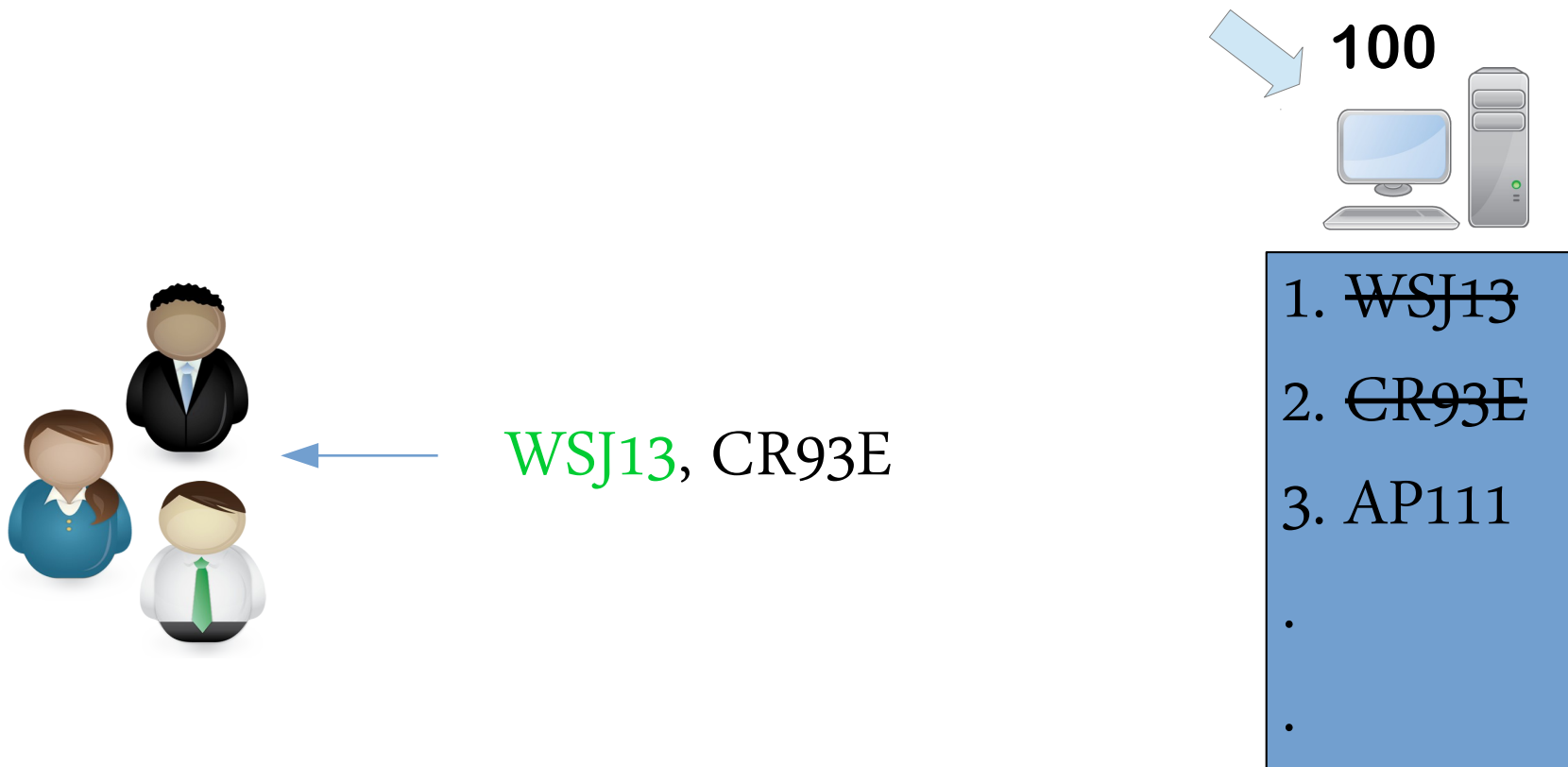
.

.

experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

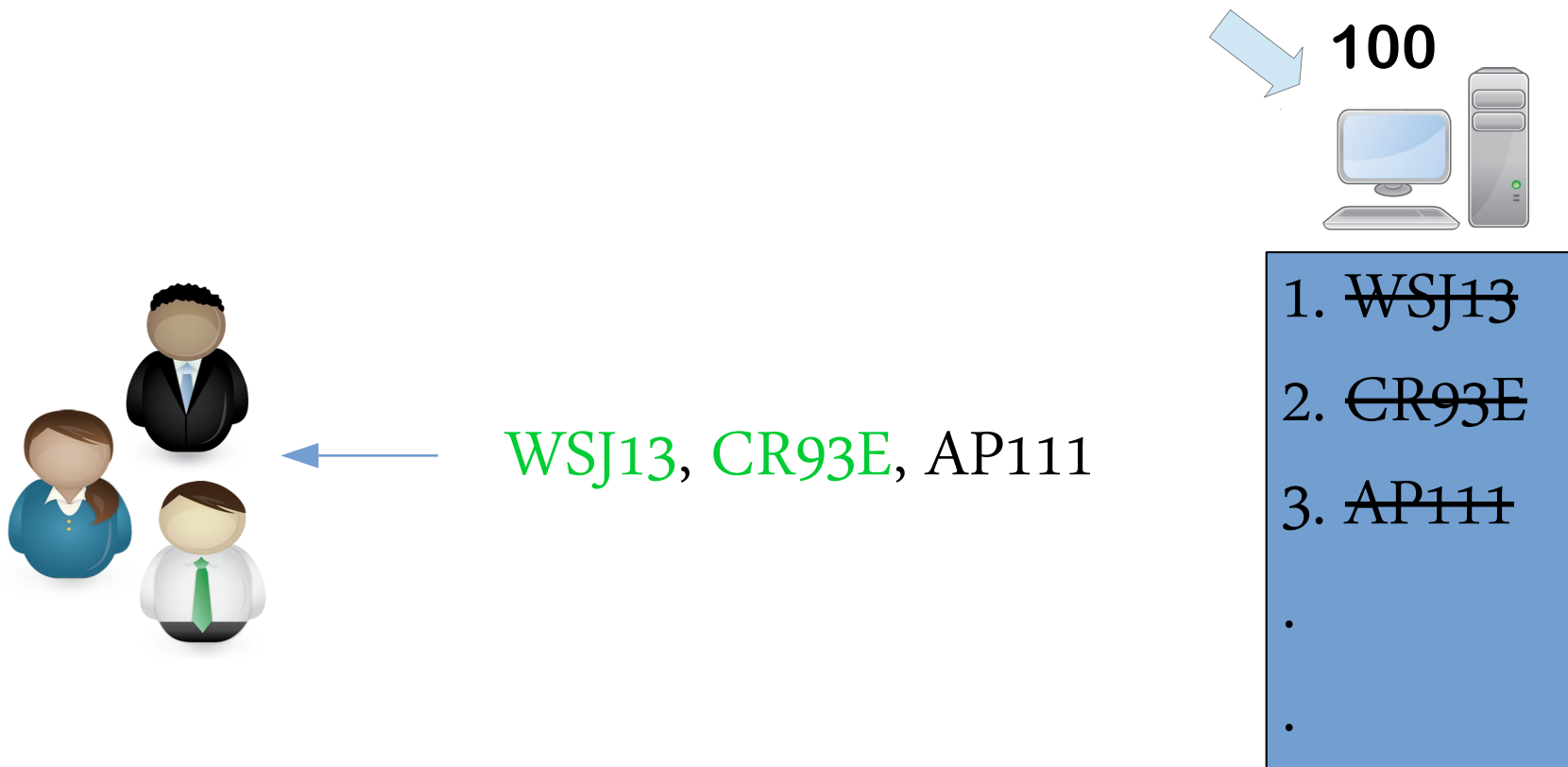
extracts & judges docs from the selected run
stays in the run until a non-rel doc is found



experiments: baselines

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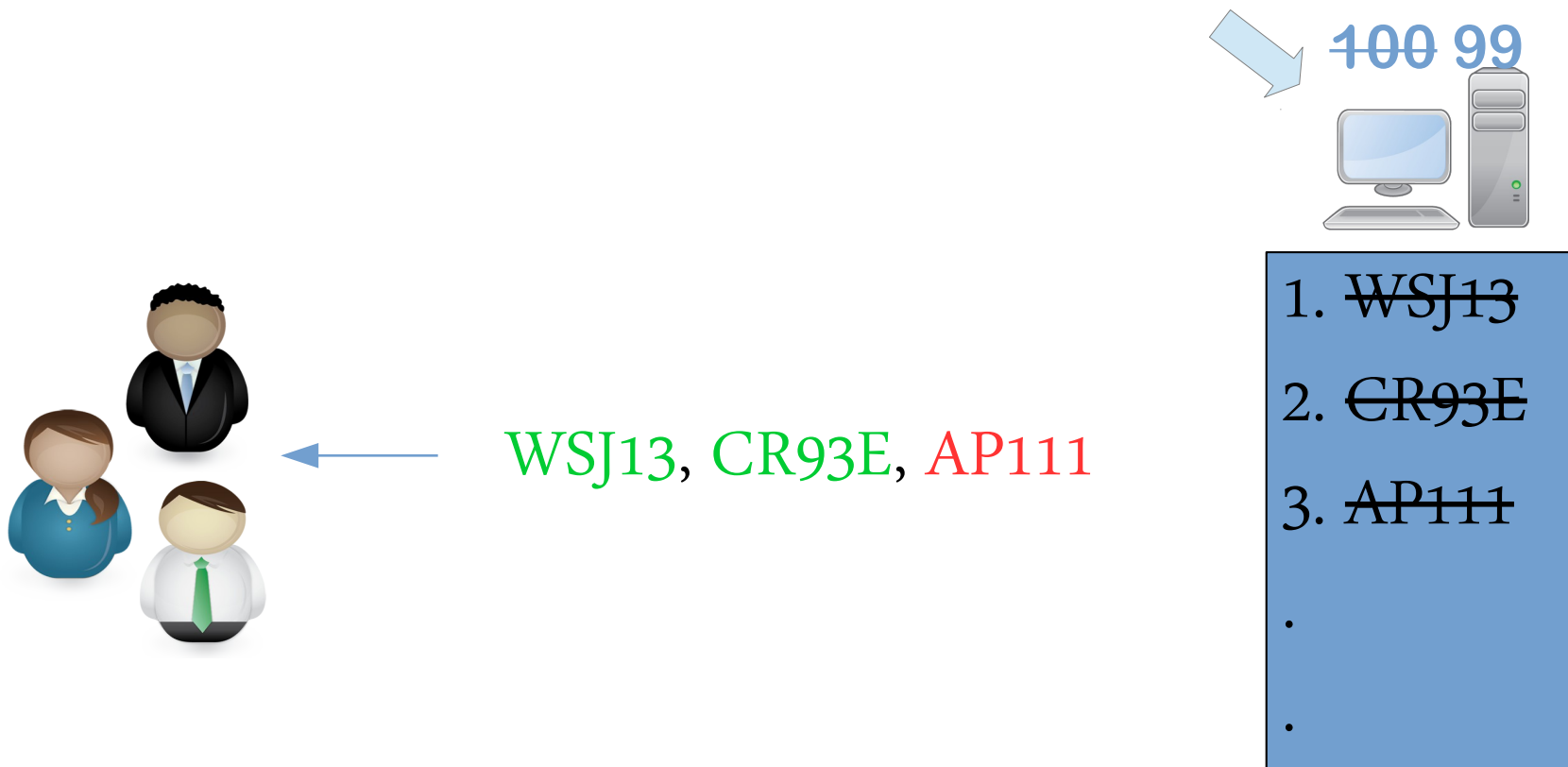


experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

extracts & judges docs from the selected run
stays in the run until a non-rel doc is found

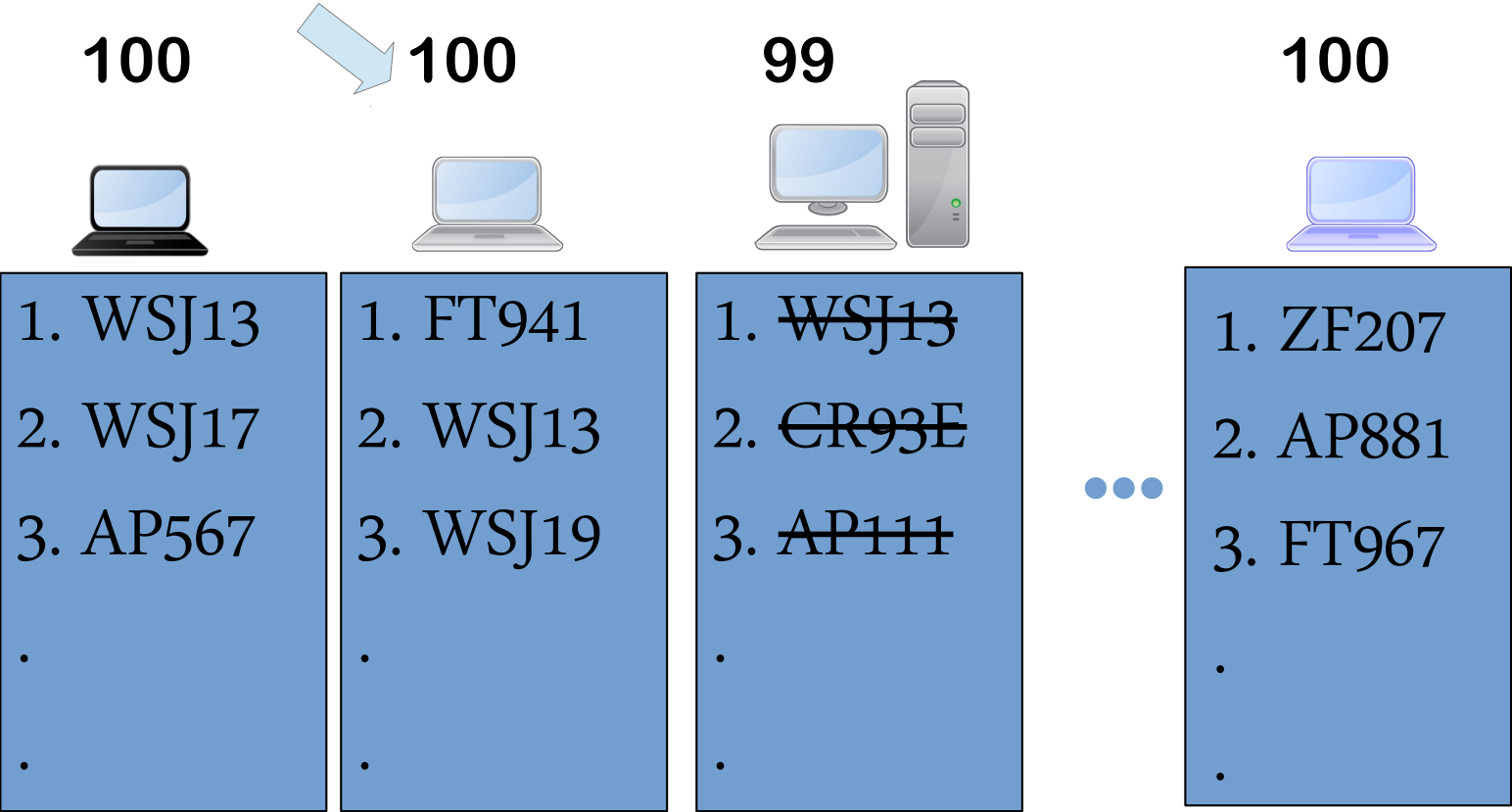
when a non-rel doc is found, priority is decreased



experiments: baselines

MoveToFront (MTF) (Cormack et al 98)

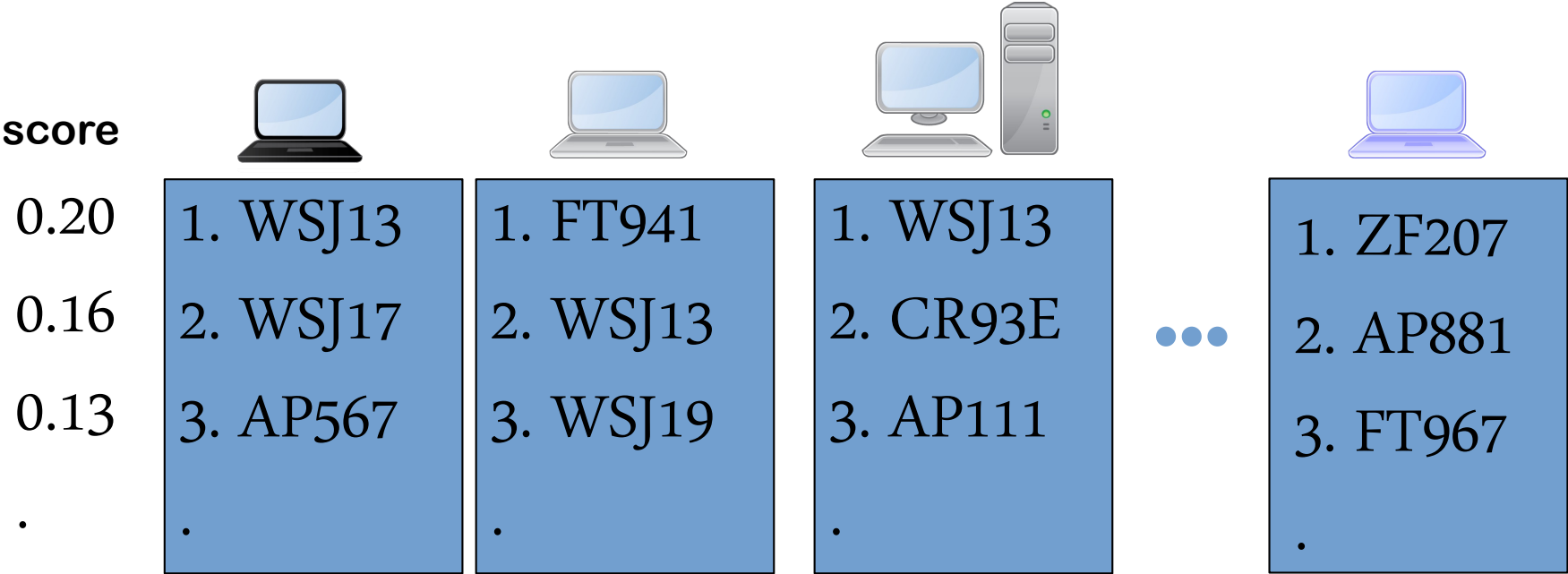
and we **jump again** to another max priority run



experiments: baselines

Moffat et al.'s method (A) (Moffat et al 2007)

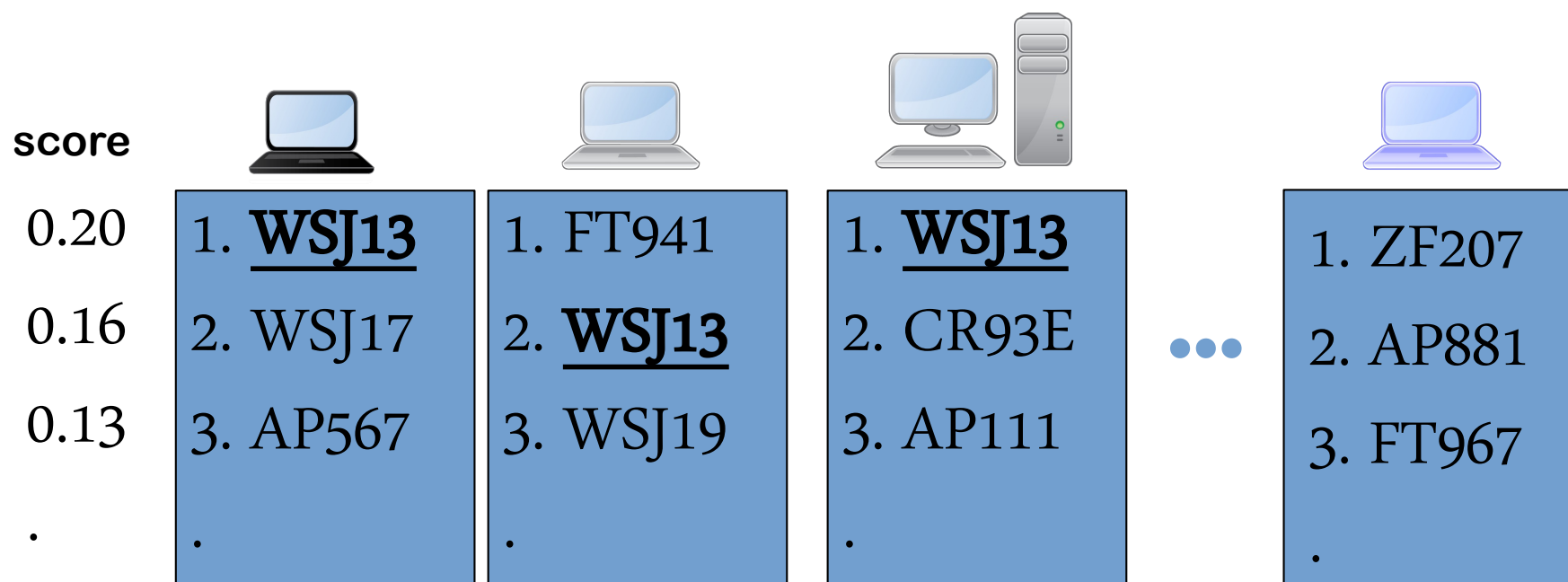
based on **rank-biased precision (RBP)**
sums a rank-dependent score for each doc



experiments: baselines

Moffat et al.'s method (A) (Moffat et al 2007)

based on **rank-biased precision (RBP)**
sums a rank-dependent score for each doc



WSJ13: $0.20 + 0.16 + 0.20 + \dots$

all docs are ranked by decreasing accumulated score
and the ranked list defines the order in which docs are judged

experiments: baselines

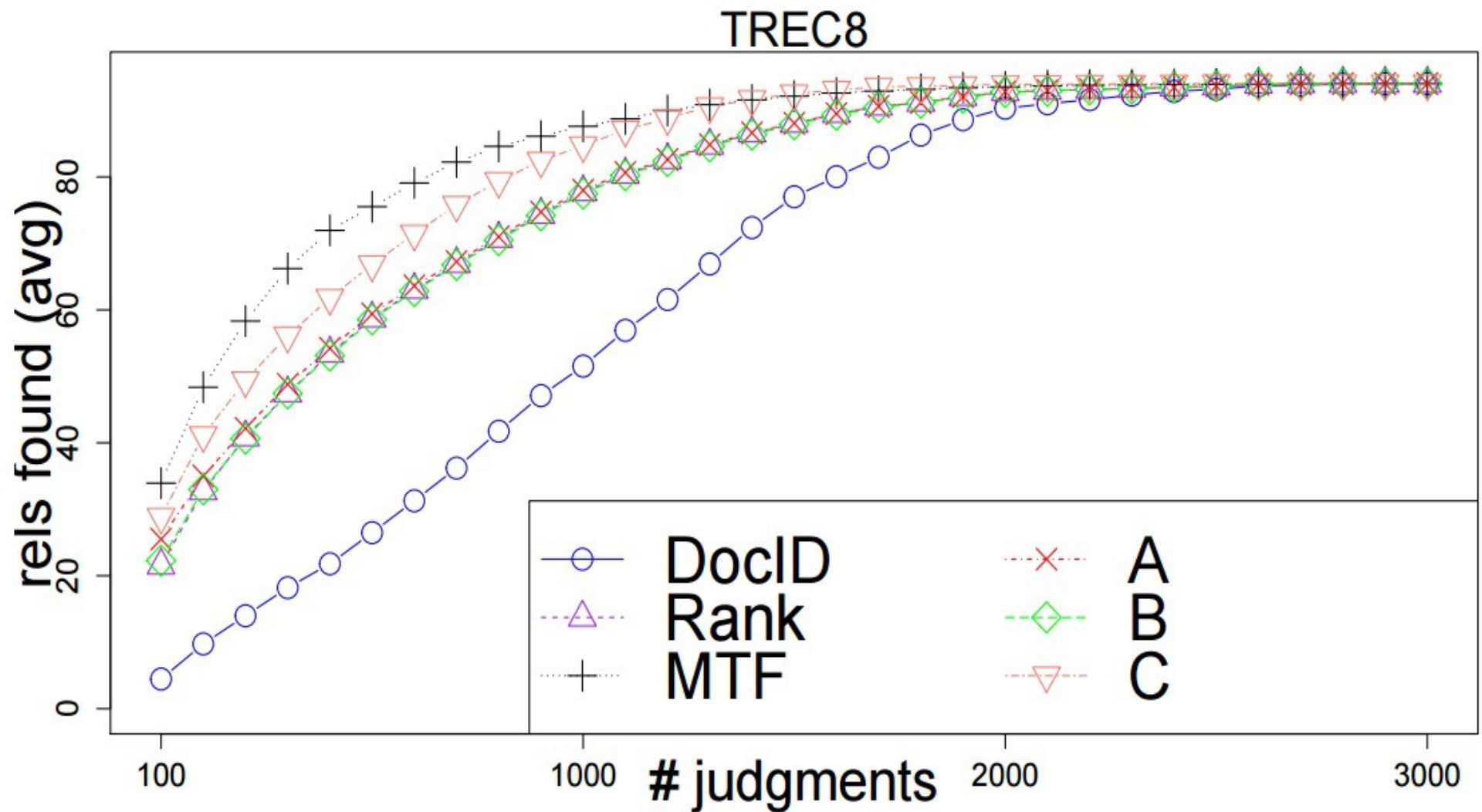
Moffat et al.'s method (B) (Moffat et al 2007)

evolution over A's method
considers not only the rank-dependent doc's
contributions but also the *runs' residuals*
promotes the selection of docs from *runs with many
unjudged docs*

Moffat et al.'s method (C) (Moffat et al 2007)

evolution over B's method
considers not only the rank-dependent doc's and the residuals
promotes the selection of docs from *effective runs*

experiments: baselines



MTF: best performing baseline

experiments: MTF vs bandit-based models

Method	Number of judgements							all
	100	300	500	700	900	1100	2000	
<i>TREC5</i>								
MTF	27.66	49.5	63.54	72.04	78.64	84.58	99.58	109.9
BLA	23.46	45.1	59.36	69.82	77.34	82.7	97.58	109.9
MM	27.76	53.54	68.18	77.96	84.18	88.74	101.42	109.9
RANDOM	20.94	41.48	53.38	63.42	71.28	76.36	93.92	109.9
UCB	20.82	46.42	58.56	67.5	74.44	79.8	96.4	109.9
ϵ_n -GREEDY	21.1	46.7	59.96	69.48	76.82	82.26	96.88	109.9
<i>TREC6</i>								
MTF	31.96	55.7	66.68	75.82	82.04	86.28	91.8	
BLA	24.94	46.42	60.62	70.4	78.84	84.56	91.8	
MM	32.12	56.1	68.98	78.06	83.16	87.24	91.8	
RANDOM	25.56	46.9	59.98	69.7	77.4	83.82	91.8	
UCB	27.86	48.96	62.36	71.38	79.14	84.9	91.8	
ϵ_n -GREEDY	27.6	50.8	63.12	71.84	78.8	84.44	91.8	
<i>TREC7</i>								
MTF	35	58.04	70.58	78.52	83.48	86.94	92.7	92.84
BLA	27.64	49.8	62.3	71.42	78.3	83.16	91.58	92.84
MM	34.62	56.4	70	78.18	83	86.36	92.4	92.84
RANDOM	27.48	50.74	62.86	71.86	78.44	83.44	91.3	92.84
UCB	30.32	52.4	64.44	72.44	79.32	83.68	91.06	92.84
ϵ_n -GREEDY	28	53.8	65.06	73.54	79.22	83.02	91.2	92.84
<i>TREC8</i>								
MTF	34.06	58.48	71.78	79.22	84.5	87.58	93.22	94.04
BLA	27.14	50.42	64.9	73.96	80.36	84.96	93.36	94.04
MM	34.4	59.34	72.9	80.82	85.56	88.8	93.54	94.04
RANDOM	26.94	50.58	63.9	72.58	79.28	83.48	92.58	94.04
UCB	29.86	52.9	65.92	74.06	80.52	85.12	93.4	94.04
ϵ_n -GREEDY	28.16	53.66	66.76	74.88	80.6	84.88	93.2	94.04

experiments: MTF vs bandit-based models

Method	Number of judgements							all
	100	300	500	700	900	1100	2000	
<i>TREC5</i>								
MTF	27.66	49.5	63.54	72.04	78.64	84.58	99.58	109.9
BLA	23.46	45.1	59.36	69.82	77.34	82.7	97.58	109.9
MM	27.76	55.34	68.74	78.74	88.74	98.74	101.42	109.9
RANDOM	20.94	38.94	53.94	63.94	73.94	83.94	93.92	109.9
UCB	28.94	48.94	63.94	74.06	80.52	85.12	96.4	109.9
ϵ_n -GREEDY	28.94	48.94	63.94	74.06	80.52	85.12	96.4	109.9
Random: weakest approach								
BLA/UCB/ϵ_n-greedy are suboptimal								
(sophisticated exploration/exploitation trading not needed)								
MTF and MM: best performing methods								
<i>TREC6</i>								
MTF	34.06	58.46	72.9	80.82	85.56	88.8	93.22	94.04
BLA	27.14	50.42	64.9	73.96	80.36	84.96	93.36	94.04
MM	34.4	59.34	72.9	80.82	85.56	88.8	93.54	94.04
RANDOM	26.94	50.58	63.9	72.58	79.28	83.48	92.58	94.04
UCB	29.86	52.9	65.92	74.06	80.52	85.12	93.4	94.04
ϵ_n -GREEDY	28.16	53.66	66.76	74.88	80.6	84.88	93.2	94.04

Random: weakest approach

BLA/UCB/ ϵ_n -greedy are suboptimal
 (sophisticated exploration/exploitation trading
 not needed)

MTF and MM: best performing methods

improved bandit-based models

**MTF: forgets quickly about past rewards
(a single non-relevance doc triggers a jump)**



**non-stationary
bandit-based
solutions:**

**not all historical
rewards count the
same**

**MM-NS and BLA-NS
non-stationary
variants of MM and
BLA**

stationary bandits

Beta(α, β), $\alpha, \beta=1$

rel docs add 1 to α
non-rel docs add 1 to β

(after n iterations) ▽

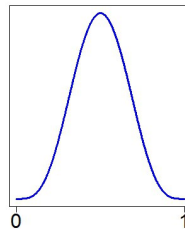
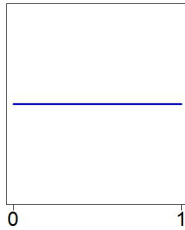
Beta(α_n, β_n)

$$\alpha_n = 1 + jrel_s$$
$$\beta_n = 1 + jret_s - jrel_s$$

$jrel_s$: # judged relevant docs (retrieved by s)

$jret_s$: # judged docs (retrieved by s)

all judged docs count the same



non-stationary bandits

Beta(α, β), $\alpha, \beta=1$

$$jrel_s = \text{rate} * jrel_s + rel_d$$
$$jret_s = \text{rate} * jret_s + 1$$

(after n iterations) ▽

Beta(α_n, β_n)

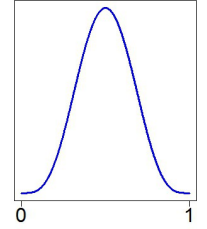
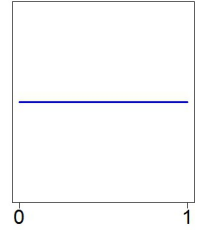
$$\alpha_n = 1 + jrel_s$$
$$\beta_n = 1 + jret_s - jrel_s$$

rate > 1: weights more early relevant docs

rate < 1: weights more late relevant docs

rate = 0: only the last judged doc counts
(BLA-NS, MM-NS)

rate = 1: stationary version



experiments: improved bandit-based models

Method	Number of judgements							all
	100	300	500	700	900	1100	2000	
<i>TREC5</i>								
MTF	27.66	49.5	63.54	72.04	78.64	84.58	99.58	109.9
BLA	23.46	45.1	59.36	69.82	77.34	82.7	97.58	109.9
BLA-NS	22.8	44.8	58.74	68.78	76.04	81.44	97.4	109.9
MM	27.76	53.54	68.18	77.96	84.18	88.74	101.42	109.9
MM-NS	30	56.76	70.96	79.06	85.18	89.42	101.32	109.9
<i>TREC6</i>								
MTF	31.96	55.7	66.68	75.82	82.04	86.28	91.8	
BLA	24.94	46.42	60.62	70.4	78.84	84.56	91.8	
BLA-NS	25.58	46.68	60.44	70	76.7	83.16	91.8	
MM	32.12	56.1	68.98	78.06	83.16	87.24	91.8	
MM-NS	33.5	58.2	69.72	77.9	83.48	87.44	91.8	
<i>TREC7</i>								
MTF	35	58.04	70.58	78.52	83.48	86.94	92.7	92.84
BLA	27.64	49.8	62.3	71.42	78.3	83.16	91.58	92.84
BLA-NS	27.8	50.14	62.54	70.34	76.92	81.56	90.28	92.84
MM	34.62	56.4	70	78.18	83	86.36	92.4	92.84
MM-NS	36.8	62.42	74.42	81.74	85.82	88.32	92.58	92.84
<i>TREC8</i>								
MTF	34.06	58.48	71.78	79.22	84.5	87.58	93.22	94.04
BLA	27.14	50.42	64.9	73.96	80.36	84.96	93.36	94.04
BLA-NS	27.12	49.5	63.68	72.06	77.56	82.54	92.42	94.04
MM	34.4	59.34	72.9	80.82	85.56	88.8	93.54	94.04
MM-NS	36.96	64.62	77.3	82.5	86.34	89.2	93.6	94.04

multi-arm bandits: **formal & effective** framework for doc adjudication in a pooling-based evaluation

it's good to react quickly to non-relevant docs
(non-stationary variants)

it's not good to increasingly reduce exploration
(UCB, ϵ_n -greedy)

future work

query-related
variabilities

hierarchical
bandits

stopping
criteria

metasearch



reproduce our experiments & test new ideas!

http://tec.citius.usc.es/ir/code/pooling_bandits.html

(our R code, instructions, etc)

Pooling - Bandits

This document provides all details needed to reproduce the experiments reported in the paper [D. Losada, J. Parapar, A. Barreiro. “Feeling Lucky? Multi-armed Bandits for Ordering Judgements in Pooling-based Evaluation”. ACM Symposium on Applied Computing, 2016.](#)

Any scientific publication derived from the use of this software should explicitly refer to this ACM SAC paper.

Next, we explain the data used for experimentation and [provide our R code](#), which implement all pooling strategies.

Data

We used four TREC collections (<http://trec.nist.gov>): TREC5, TREC6, TREC7 and TREC8.

NIST kindly provided the runs that contributed to the pools of the adhoc tasks of TREC5, TREC6, TREC7 and TREC8 (http://trec.nist.gov/data/intro_eng.html).

The pooled runs are archived by NIST within a password protected area. If you want to reproduce our experiments you need to request access to the protected area (follow the instructions given at <http://trec.nist.gov/results.html>).

- **TREC5**

- 101 runs in the pool (77 adhoc + 24 other).

The **77 adhoc runs** are: input.anu5aut1 input.anu5aut2 input.anu5man4 input.anu5man6 input.brkly15 input.brkly16 input.brkly17 input.brkly18 input.city96a1 input.city96a2 input.CLCLUS input.CLTHES input.colm1 input.colm4 input.Cor5A1se input.Cor5A2cr input.Cor5M1le input.Cor5M2rf input.Ctifr1 input.Ctifr2 input.DCU961 input.DCU962 input.DCU963 input.DCU964 input.DCU969 input.DCU96C input.DCU96D input.erliA1 input.ETHal1 input.ETHas1 input.ETHme1 input.fscIt3 input.fscIt4 input.genrl1 input.genrl2 input.genrl3 input.genrl4 input.glair4 input.gmu96au1 input.gmu96au2 input.gmu96ma1 input.gmu96ma2 input.ibmgd1 input.ibmgd2 input.ibmge1 input.ibmge2 input.ibms96a input.ibms96b input.INQ301 input.INQ302 input.KUSG2 input.KUSG3 input.LNaDesc1 input.LNaDesc2 input.LNmFull1 input.LNmFull2 input.mds001 input.mds002 input.mds003 input.Mercure-al input.Mercure-as input.MONASH input.pircsAAL input.pircsAAS input.pircsAM1 input.pircsAM2 input.sdmix1 input.sdmix2 input.umcpa1 input.uncis1 input.uncis2 input.UniNE7 input.UniNE8 input.uwgcx0 input.uwgcx1 input.vtwnA1 input.vtwnB1

The **other 24 runs** are: input.anu5mrg0 input.anu5mrg1 input.anu5mrg7 input.CLATMC input.CLATMN input.CLPHR0 input.CLPHR1 input.CLPHR2 input.fscIt3m input.genlp1 input.genlp2 input.genlp3 input.genlp4 input.MTRa961 input.sbase1 input.sbase2 input.UniNE0 input.UniNE9 input.xerox_nlp1 input.xerox_nlp2 input.xerox_nlp3 input.xerox_nlp4 input.xerox_nlp5 input.xerox_nlp6

Feeling *Lucky*? Multi-armed bandits for Ordering Judgements in Pooling-based Evaluation

David E. Losada



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